## Advanced Matrix Theory and Linear Algebra for Engineers - Video course

## COURSE OUTLINE

Introduction, Vector Spaces, Solutions of Linear Systems, Important Subspaces associated with a matrix, Orthogonality, Eigenvalues and Eigenvectors, Diagonalizable Matrices, Hermitian Matrices, General Matrices, Jordan Canonical form (Optional)*, Selected Topics in Applications (Optional)*

COURSE DETAIL

| Module <br> No. | Topic/s | Hours |
| :---: | :---: | :---: |
| 1 | Introduction: <br> 1. First Basic Problem - Systems of Linear equations Matrix Notation - The various questions that arise with a system of linear eqautions <br> 2. Second Basic Problem - Diagonalization of a square matrix - The various questions that arise with diagonalization | 3 |
| 2 | Vector Spaces <br> 1. Vector spaces <br> 2. Subspaces <br> 3. Linear combinations and subspaces spanned by a set of vectors <br> 4. Linear dependence and Linear independence <br> 5. Spanning Set and Basis <br> 6. Finite dimensional spaces <br> 7. Dimension | 6 |
| 3 | Solutions of Linear Systems <br> 1. Simple systems <br> 2. Homogeneous and Nonhomogeneous systems <br> 3. Gaussian elimination <br> 4. Null Space and Range <br> 5. Rank and nullity <br> 6. Consistency conditions in terms of rank <br> 7. General Solution of a linear system <br> 8. Elementary Row and Column operations <br> 9. Row Reduced Form <br> 10. Triangular Matrix Factorization | 6 |
| 4 | Important Subspaces associsted with a matrix <br> 1. Range and Null space <br> 2. Rank and Nullity <br> 3. Rank Nullity theorem <br> 4. Four Fundamental subspaces <br> 5. Orientation of the four subspaces | 4 |



NP-TEL

## Coordinators:

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| 5 | Orthogonality <br> 1. Inner product <br> 2. Inner product Spaces <br> 3. Cauchy - Schwarz inequality <br> 4. Norm <br> 5. Orthogonality <br> 6. Gram - Schmidt orthonormalization <br> 7. Orthonormal basis <br> 8. Expansion in terms of orthonormal basis - Fourier series <br> 9. Orthogonal complement <br> 10. Decomposition of a vector with respect to a subspace and its orthogonal complement - Pythagorus Theorem | 5 |
| :---: | :---: | :---: |
| 6 | Eigenvalues and Eigenvectors <br> 1. What are the ingredients required for diagonalization? <br> 2. Eigenvalue - Eigenvector pairs <br> 3. Where do we look for eigenvalues? - characteristic equation <br> 4. Algebraic multiplicity <br> 5. Eigenvectors, Eigenspaces and geometric multiplicity | 5 |
| 7 | Diagonalizable Matrices <br> 1. Diagonalization criterion <br> 2. The diagonalizing matrix <br> 3. Cayley-Hamilton theorem, Annihilating polynomials, Minimal Polynomial <br> 4. Diagonalizability and Minimal polynomial <br> 5. Projections <br> 6. Decomposition of the matrix in terms of projections | 5 |
| 8 | Hermitian Matrices <br> 1. Real symmetric and Hermitian Matrices <br> 2. Properties of eigenvalues and eigenvectors <br> 3. Unitary/Orthoginal Diagonalizbility of Complex Hermitian/Real Symmetric matrices <br> 4. Spectral Theorem <br> 5. Positive and Negative Definite and Semi definite matrices | 5 |
| 9 | General Matrices <br> 1. The matrices $A A^{\top}$ and $A^{T A}$ <br> 2. Rank, Nullity, Range and Null Space of $A A^{\top}$ and $A^{\top} A$ <br> 3. Strategy for choosing the basis for the four fundamental subspaces <br> 4. Singular Values <br> 5. Singular Value Decomposition <br> 6. Pseudoinverse and Optimal solution of a linear system of equations <br> 7. The Geometry of Pseudoinverse | 5 |
| 10 | Jordan Cnonical form* <br> 1. Primary Decomposition Theorem <br> 2. Nilpotent matrices <br> 3. Canonical form for a nilpotent matrix <br> 4. Jordan Canonical Form <br> 5. Functions of a matrix | 5 |

1. Optimization and Linear Programming
2. Network models
3. Game Theory
4. Control Theory
5. Image Compression
