## A Basic Course in Real Analysis -Video course

## **COURSE OUTLINE**

It is a first level course on Functional Analysis. The motto is to familiarize the students with basic concepts, principles and methods of Functional analysis and its applications.

## **COURSE DETAIL**

Module	Learning Units	Lectures	
Module I	<ol> <li>Dedekind Theory of Irrational numbers:-         <ul> <li>Rational numbers, section of Rational numbers, Irrational numbers, real Numbers, Dedekind Theorem, The Continuum Exercise- Tutorial</li> </ul> </li> <li>Cantor's Theory of Irrational numbers:-         <ul> <li>Cantor's Theory, Convergent sequence of real numbers, Equivalence of the definition of Dedekind &amp; Cantor</li> </ul> </li> <li>Sets of Points-         <ul> <li>The upper &amp; lower bounds, l.u.b. &amp; g.l.b. of sets, limiting point, Weierstrass Theorem, Derived sets, Countable &amp; Non constable sets, Cardinal numbers, Open &amp; Closed sets, Closure of a set, Perfect set, Heine-Borel Theorem</li> </ul> </li></ol>	14	Pre-requisites: • Nil. Additional Reading: • Nil. Hyperlinks: • Nil. Coordinators: Prof. P.D. Srivastava Department of Mathema Kharagpur
Module II	1. Limit of Sequences of Real Numbers:-	13	



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## **Mathematics**

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		<ul> <li>Bounded sequences, Null sequences, Monotone sequences, Convergent sequences, Fundamental theorems on limit, limit sup, limit inf of sequences, Ratio Test &amp; other Tests, Cauchy theorems, Cauchy Convergence Criteria Exercises- Tutorial</li> </ul>		
		2. Infinite Series of Real numbers:-		
		<ul> <li>Introduction of infinite series, Tests for its convergence, Absolute convergence, Conditional convergence</li> </ul>		
		3. Limit of functions		
		<ul> <li>Concepts of Limit of functions, Limit Theorems, Some extension of Limit Concepts, Exercises- Tutorials</li> </ul>		
ĺ	Module	1. Continuity of Functions:-	9	
	III	<ul> <li>Cauchy's and Heine's definitions of continuity, Properties of Continuous functions, Uniform continuity, Absolute continuity, Discontinuous Functions, Types of Discontinuities</li> </ul>		
		2. Differentiability:-		
		<ul> <li>Concept of Derivatives, Rolle's theorem, Mean value theorem, L' Hospital Rule, Taylors Theorem Exercises- Tutorial</li> </ul>		
	Module IV	1. Riemann Integration / Reimann- Stieltjes Intergral:-	8	
		• The Upper and lower R-integrals, Integrable (R) functions, Properties of definite and indefinite integral, Mean value theorems, Absolute convergence, convergence, Test for improper integrals. Definition & Existence of the Reimann- Stieltjes Integral & its properties Exercise, Tutorial		

References:	
1. W. Rudin - Principles of Mathematica Analysis - Mc. Graw Hill Int. Edition (3rd)	
2. Robert G. Bartle and Donald R. Shebert - Introduction to Real Analysis - Wiley India, 3rd ed.	
<ol> <li>Sterling K. Berberian - A First course in Real Analysis - 1994, Springer Verlag, Ny. Inc.</li> </ol>	
4. N. Saran - Theory of Function of Real Variable	
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