

INFORMATION THEORY

PROF. HIMANSHU TYAGI Department of Electrical Engineering **IISc Bangalore**

TYPE OF COURSE COURSE DURATION : 12 weeks (20 Jul' 20 - 9 Oct' 20) EXAM DATE : 18 Oct 2020

: New | Elective | UG/PG

PRE-REQUISITES: Undergraduate level probability (sets and events, probability distributions, probability density functions, probability mass functions, random variables, expected value, variance, popular probability laws, Markov inequality, Chebyshev inequality, central limit theorem, law of large numbers)

INTENDED AUDIENCE: Senior undergraduate and graduate students interested in probability, statistics ,communication, theoretical computer science, machine learning, quantum information and statistical physics

INDUSTRIES APPLICABLE TO : Not Available

COURSE OUTLINE :

This is a graduate level introductory course in Information Theory where we will introduce the mathematical notion of information and justify it by various operational meanings. This basic theory builds on probability theory and allows us to quantitatively measure the uncertainty and randomness in a random variable as well as information revealed on observing its value. We will encounter quantities such as entropy, mutual information, total variation distance, and KL divergence and explain how they play a role in important problems in communication, statistics, and computer science. Information theory was originally invented as a mathematical theory of communication, but has since found applications in many areas ranging from physics to biology. In fact, any field where people want to evaluate how much information about an unknown is revealed by a particular experiment,

information theory can help. In this course, we will lay down the foundations of this fundamental field.

ABOUT INSTRUCTOR:

Prof. Himanshu Tyagi is an Assistant Professor of Indian Institute of Sciences.

COURSE PLAN :

Week 1: Introduction to entropy as a measure of uncertainty and randomness

Week 2: Binary hypothesis testing: bayes optimal binary hypothesis testing and total variation distance,

Neyman-Pearson formulation, Stein & lemma and KL divergence

Week 3: Measures of information and their properties: Chain rule and additivity, concavity, and variational

formulae

Week 4:Data processing inequality, Pinsker's inequality, and Fano's inequality

Week 5: Data compression: variable length source coding theorems and entropy

Week 6: Human code, Shannon-Fano-Elias code, arithmetic code, hash tables

Week 7: Universal compression

Week 8: Channel coding: Channel capacity theorem, sphere packing bound, maximal code construction

Week 9: Random coding and ML decoding

Week 10: LDPC and Polar codes

Week 11: Quantization

Week 12: Minmax lower bounds in statistics