

## FEM & CONSTITUTIVE MODELLING IN GEOMECHANICS

**PROF. K RAJAGOPAL** Department of Civil Engineering IIT Madras

**PRE-REQUISITES :** Exposure to Mechanics courses & Shear strength of soils

INTENDED AUDIENCE : Senior level UG Civil Engineering & all PG level Civil Engineering students in geotechnical

engineering stream

INDUSTRY SUPPORT : Most design companies working in Geotechnical Engineering like L&T ECC, AFCONS, HCC, Keller,

Golder Associates, etc

## **COURSE OUTLINE :**

The course will introduce the students to both theoretical and practical aspects of finite element methods applicable to geotechnical engineering. The course will start from the fundamental aspects of matrix structural analysis and move into finite element techniques through variational principles. Special focus of this course will be on topics related to geotechnical problems like modelling of infinite soil media, construction and excavation sequences, jointed mass, and nonlinear analysis techniques. Fundamentals of different topics of isoparametric computations and nonlinear & elastic plastic analysis are explained through simple to use computer programs and detailed flow-charts.

## **ABOUT INSTRUCTOR :**

The Instructor is a Professor of Civil Engineering at IIT Madras. He has taught the subject of finite elements and constitutive modelling for more than 25 years at the institute. He has guided several Masters and Doctoral students on these and related topics. He had also organized several national and international training programs on use of finite element techniques in geotechnical engineering

## **COURSE PLAN :**

**Week 1:** Introduction to course, introduction to matrix algebra, concepts of finite element analysis through prismatic elements (spring, bar & beam elements) and matrix structural analysis

Week 2: Variational principles & Rayleigh-Ritz procedures in structural mechanics as a prelude to finite element techniques

Week 3: Continuum, stress & strain states, equations of equilibrium, compatibility & linear elastic constitutive equations, derivation of equilibrium equations for continuum, Plane stress, plane strain and axisymmetric and 3-d stress states

**Week 4:** Generalized Coordinate methods for deriving shape functions, Lagrange methods for shape functions 3-node CST element for finite element analysis and some simple calculations using this element

Week 5: Numerical integration techniques, Isoparametric transformations, shape functions in isoparametric space, Patch test & convergence

Week 6: Isoparametric element calculations - numerical examples & computer programs for different computations like stiffness matrix, load vector due to self-weight, stresses, etc.

**Week 7:** In situ stress states in soil medium, Simulation of construction and excavation sequences in finite element analysis, Joint elements for simulating discontinuities in geologic medium

Week 8: Infinite elements for simulating semi-infinite soil domains subjected to static and dynamic loading

**Week 9:** Stress and strain tensors & invariants,Introduction to nonlinear finite element techniquesDifferent types of constitutive models **Week 10:** Nonlinear constitutive models like variable moduli models, Hyperbolic models,>Mohr Coulomb model, stress correction methods & numerical procedures

Week 11: Elastic Plastic constitutive models Simulation of dilation of soils Hardening soil models for excavation problems

Week 12: Undrained and drained response of soils Consolidation analysis of soils Introduction to simulation of impact and dynamic loading

Introduction to nonlinear finite element techniques

Different types of constitutive models

Week 10: Nonlinear constitutive models like variable moduli models, Hyperbolic models, Mohr Coulomb model, stress correction methods & numerical procedures

Week 11: Elastic-Plastic constitutive models

Simulation of dilation of soils

Hardening soil models for excavation problems

Week 12: Undrained and drained response of soils Consolidation analysis of soils Introduction to simulation of impact and dynamic loading