

# Week 1 Practice Assignment

Sanjeev Patil

PhD scholar

Dept. of Metallurgical and Materials Engineering

IIT – Madras

**NOC22 MM11**

**Fundamentals of Electronic Materials and Devices**

**Jan 2022**



# Prerequisites

- Calculator
- Attempted sample problems

1. Unknown element X has resistivity  $10^{11} \Omega\text{m}$  at 300 K. Is X

- a) Conductor
- b) Insulator
- c) Semiconductor

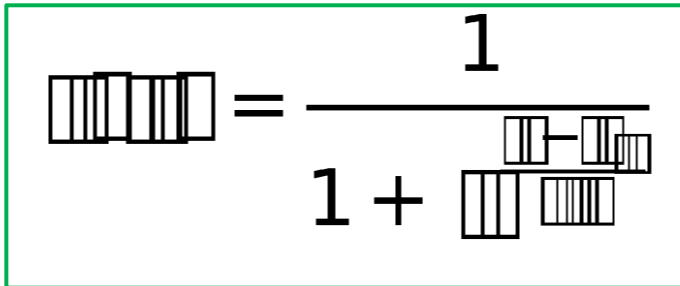
2. Unknown material Y has band gap of 1.5 eV. Is Y

- a) Conductor
- b) Insulator
- c) Semiconductor

# Problem 1

1) In a metal, at some temperature  $T$ , the probability of finding an electron **0.2 eV above the Fermi energy** is **1%** of the probability of finding the electron at the Fermi energy. What is the approximate value of  $T$ ? Give your answer in K and use the FEG model.

- 200
- 310
- 440
- 600


$$f = \frac{1}{1 + e^{\frac{E - E_F}{kT}}}$$

$$E - E_F = 0.2 \text{ eV}$$

$$k = 1.38 \times 10^{-23} \text{ m}^2 \cdot \text{kg} \cdot \text{s}^{-2} \cdot \text{K}^{-1}$$

$$\frac{1}{1 + e^{\frac{0.2}{kT}}} = 0.01 \times \frac{1}{1 + e^0}$$

Tip: take care to convert eV to J

$$T = 439 \text{ K}$$

# Problem 2

2) What is the density of states ( $g(E)$ ) of a free electron gas (FEG) metal at an energy of 3 eV? Give your answer in units of  $J^{-1}m^{-3}$

$9.5 \times 10^{46}$

$7.3 \times 10^{46}$

$2.9 \times 10^{44}$

$1.4 \times 10^{40}$

$$g(E) = 8\pi\sqrt{2} \left(\frac{m_e}{h^2}\right)^{3/2} E_F^{1/2}$$

$$m_e = 9.1 \times 10^{-31} \text{ kg}; h = 6.6 \times 10^{-34} \text{ m}^2 \cdot \text{kg} \cdot \text{s}^{-1}$$

$$g(E) = 7.34 \times 10^{46} \text{ J}^{-1} \text{ m}^{-3}$$

# Problem 4

4) In a FEG metal, what is the probability of finding an electron 25 meV **above** the Fermi energy? Take temperature to be 300 K.

- 0.27
- 0.37
- 0.63
- 0.73

$$f(E) = \frac{1}{1 + e^{\frac{E - E_F}{kT}}}$$

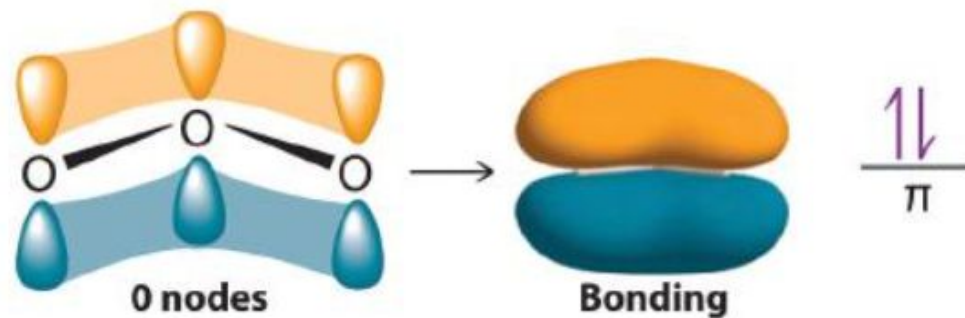
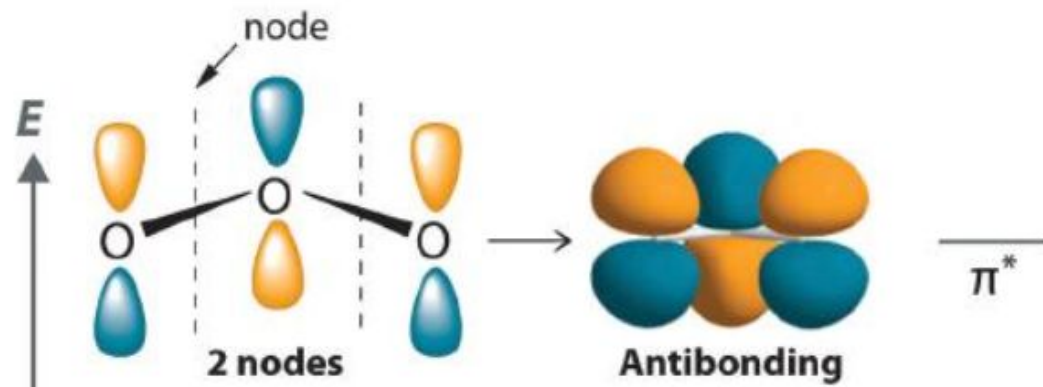
$$E - E_F = 0.025 \text{ eV}$$

$$f(E) = \frac{1}{1 + e^{\frac{E - E_F}{kT}}}$$

$$f(E) = 0.27$$

Tip:  $kT = 0.025 \text{ eV}$  for simpler calculation

# Problem 3



Possible  $2p_z$  interactions

Molecular orbitals

Energy levels

Tip:  $n$  atomic orbitals =  $(n-1)$  nodes