

## **Module 8 : Robot vision II**

### **Lecture 29 : Image enhancements, histogram Equalisation & specification, discrete transformations**

#### **Objectives**

In this course you will learn the following

- Machine Vision
- Enhancement
- Histogram Equalization
- Histogram specification
- Image Enhancement

#### **Machine Vision**

- Image Acquisition
- Relationship between 'image' coordinates and 'world' coordinates
- Basic concepts - Neighborhood, distance connectivity
- Image processing – Spatial domain (Smoothing both gray level & binary), Frequency domain
- Enhancement.

#### **Enhancement**

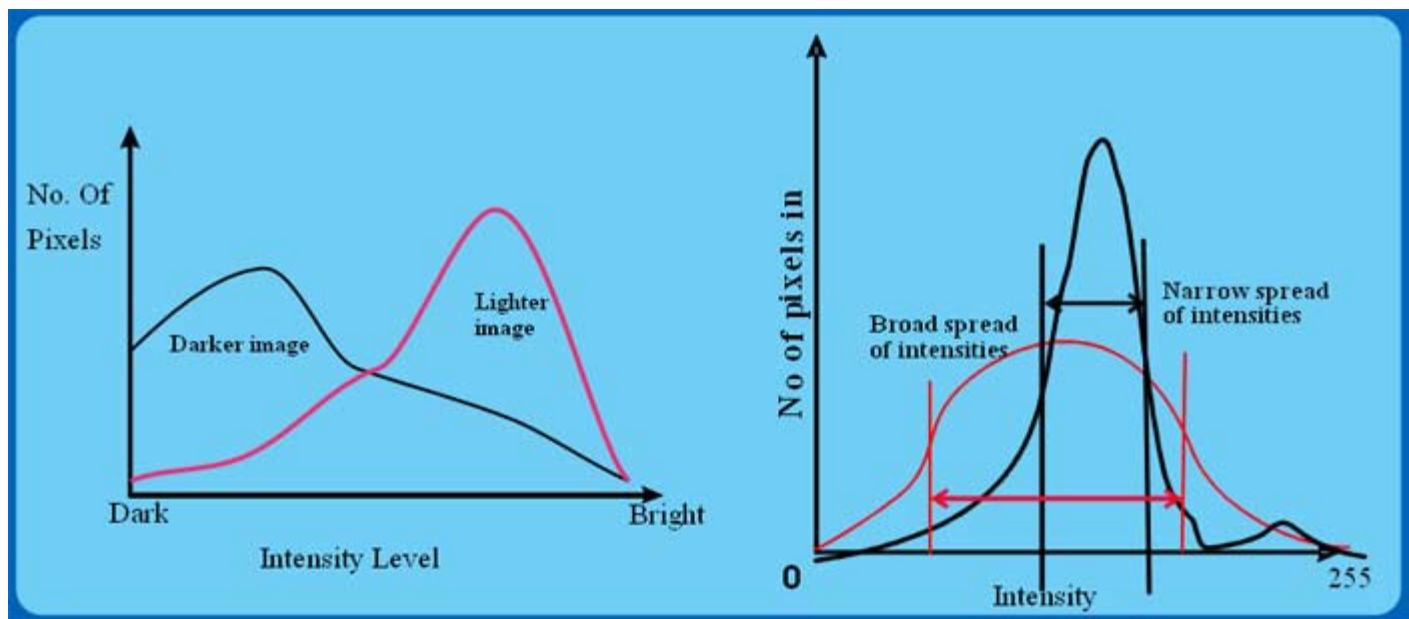


Figure 29.1

Intensity transformations

$$S = T(r)$$

$$s = T(r)$$

$$0 \leq r \leq 1$$

$$0 \leq s \leq 1$$

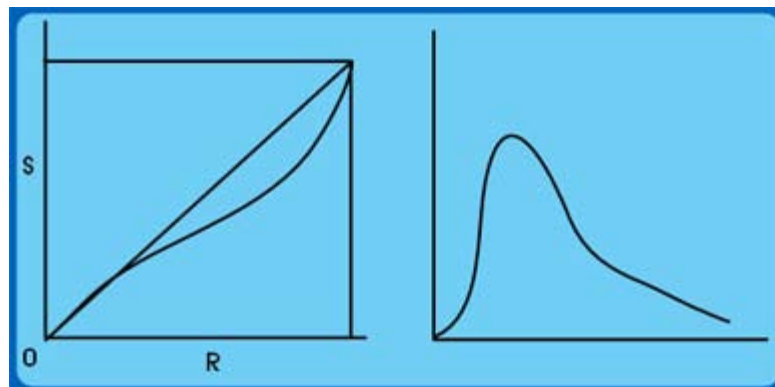


Figure 29.2

Let  $T$  be monotonically increasing function and single valued. Then  $\text{inv}(T)$  exists.

Continuous intensity levels. Histogram  $\rightarrow$  PDF (Refer Figure 29.3)

### Histogram Equalization

$$p_s(s) = \left[ p_r(r) \frac{dr}{ds} \right]_{r=T^{-1}(s)}$$

$$\frac{ds}{dr} = p_r(r) \Rightarrow ds = p_r(r) dr$$

$$s = \int_0^r p_r(w) dw = T(r)$$

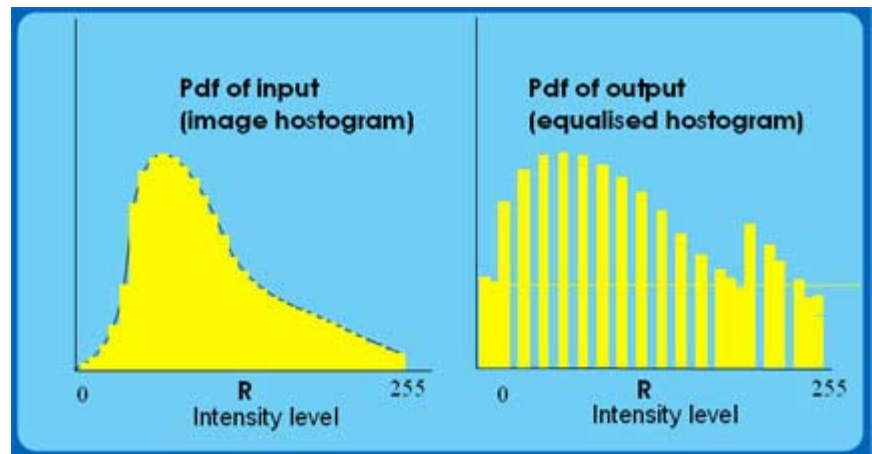


Figure 29.3 Intensity Level

### Example

$$s = T(r)$$

$$r = T^{-1}(s)$$

$$\begin{aligned} p_s(s) &= p_r(r) \left. \frac{dr}{ds} \right|_{r=T^{-1}(s)} \\ &= 2(1-r) \left. \frac{d(1-\sqrt{1-s})}{ds} \right|_r \\ &= \frac{2\sqrt{1-s}}{2\sqrt{1-s}} = 1 \end{aligned}$$

$$p_r(r) = 2(1-r)$$

$$T = \int_0^r 2(1-w)dw = \left[ 2w - \frac{2w^2}{2} \right]_0^r$$

$$s = -r^2 + 2r \Rightarrow r = 1 - \sqrt{1-s}$$

### Discrete

$$p_r(r_k) = \frac{n_k}{n}$$

Histogram – plot of

$p_r(r_k)$  vs.  $r_k$

$$s_k = \sum_{j=0}^k \frac{n_j}{n} = T(r_k)$$

where,  $p_r$  : probability of a pixel being of gray level  $k$ .

$n_k$  : no. of pixels belonging to gray level  $k$ .

$n$ : Total no. of pixels

### Example

| k | $r_k$ | $n_k$ | $p_r(r_k)$ |      |
|---|-------|-------|------------|------|
| 0 | 0     | 790   | 0.19       | 0.19 |
| 1 | 1/7   | 1023  | 0.25       | 0.44 |
| 2 | 2/7   | 850   | 0.21       | 0.65 |
| 3 | 3/7   | 656   | 0.16       | 0.81 |
| 4 | 4/7   | 329   | 0.08       | 0.89 |

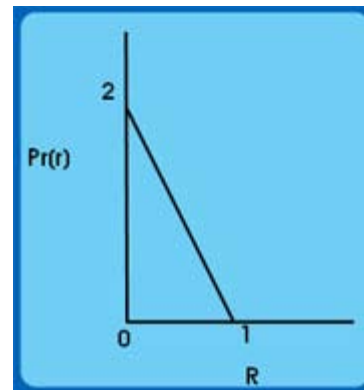


Figure 29.4

|   |     |     |      |      |
|---|-----|-----|------|------|
| 5 | 5/7 | 245 | 0.06 | 0.95 |
| 6 | 6/7 | 122 | 0.03 | 0.98 |
| 7 | 1   | 81  | 0.02 | 1.00 |

**Histogram specification**

$P_r(r)$  original Image pdf

$P_z(z)$  desired out image pdf

$$s = T(r) = \int_0^r p_r(w)dw \quad - \text{ equalizes } s$$

$$z = G^{-1}(s) = G^{-1}(T(r))$$

$$v = G(z) = \int_0^z p_z(w)dw \quad - \text{ equalizes } z$$

**Image Enhancement**

$$G_x = \frac{\partial f}{\partial x} \approx f(x,y) - f(x-1,y)$$

$$G_y = \frac{\partial f}{\partial y} \approx f(x,y) - f(x,y-1)$$

$$= f(x-1,y+1) - f(x-1,y-1) + 2f(x,y+1) - 2f(x,y-1) + f(x+1,y+1) - f(x+1,y-1)$$

$$g(x,y) = \begin{matrix} 1 \\ 0 \end{matrix}$$

otherwise

$G_y =$

|    |   |   |
|----|---|---|
| -1 | 0 | 1 |
| -2 | 0 | 2 |
| -1 | 0 | 1 |

SOBEL MASK  
OPERATOR

|    |    |    |
|----|----|----|
| -1 | -2 | -1 |
| 0  | 0  | 0  |
| 1  | 2  | 1  |

**Recap**

In this course you have learnt the following

- Machine Vision

- Enhancement
- Histogram Equalization
- Histogram specification
- Image Enhancement

Congratulations, you have finished Lecture 29. To view the next lecture select it from the left hand side menu of the page.