

Foundations of R Software

Lecture 12

Basics of Calculations

⋮

Matrices

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Matrix

Matrices are important objects in any calculation.

A matrix is a rectangular array with p rows and n columns.

An element in the i -th row and j -th column is denoted by X_{ij} (book version) or $X[i, j]$ ("program version"), $i = 1, 2, \dots, n, j = 1, 2, \dots, p$.

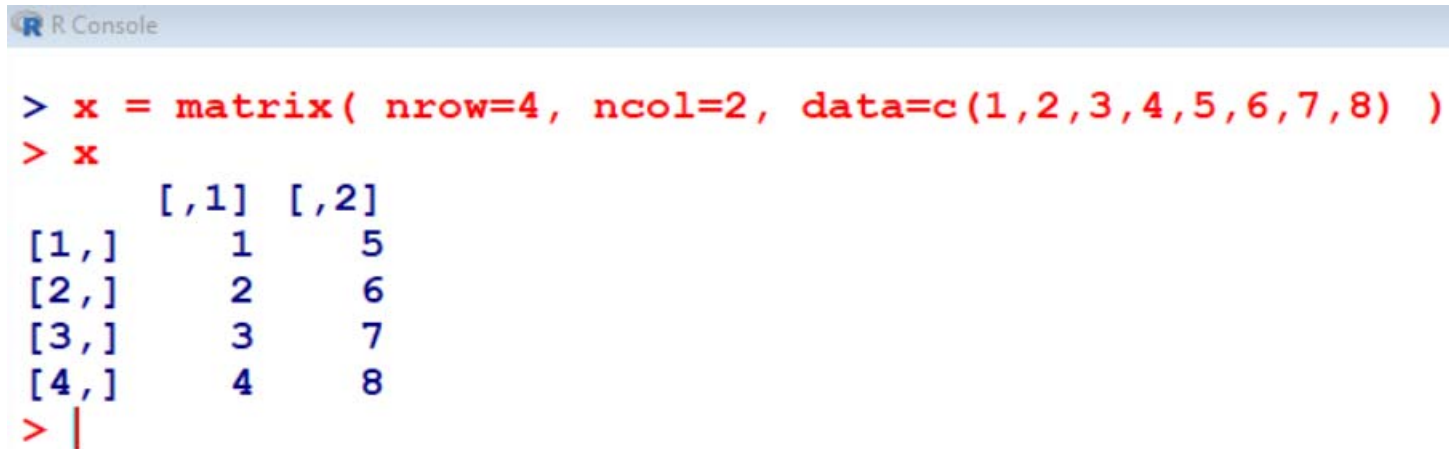
An element of a matrix can also be an object, for example a string.
However, in mathematics, we are mostly interested in numerical matrices, whose elements are generally real numbers

In R, a 4×2 -matrix X can be created with a following command:

```
> x = matrix( nrow=4, ncol=2,  
              data=c(1,2,3,4,5,6,7,8) )
```

```
> x
```

	[,1]	[,2]
[1,]	1	5
[2,]	2	6
[3,]	3	7
[4,]	4	8



The screenshot shows an R console window with the following text:

```
R Console  
> x = matrix( nrow=4, ncol=2, data=c(1,2,3,4,5,6,7,8) )  
> x
```

	[,1]	[,2]
[1,]	1	5
[2,]	2	6
[3,]	3	7
[4,]	4	8

The prompt character is followed by a vertical bar, indicating the command is still being entered.

Matrix parameters

We see:

The parameter **nrow** defines the row number of a matrix.

The parameter **ncol** defines the column number of a matrix.

The parameter **data** assigns specified values to the matrix elements.

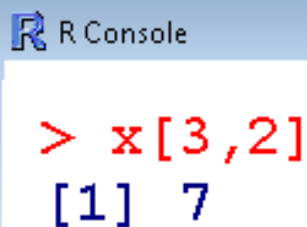
The data values from the parameters are written column-wise in matrix.

Accessing any element of a matrix

```
> x
      [,1] [,2]
[1,]    1    5
[2,]    2    6
[3,]    3    7
[4,]    4    8
```

One can access a single element of a matrix with `x[i,j]` :

```
> x[3,2]
[1] 7
```



```
R Console
> x[3,2]
[1] 7
```

Entering data column wise in a matrix

In case, the data has to be entered column wise, then a 4×2 -matrix

X can be created with

```
> x = matrix( nrow=4, ncol=2,  
              data=c(1,2,3,4,5,6,7,8))
```

OR

```
x = matrix( nrow=4, ncol=2,  
            data=c(1,2,3,4,5,6,7,8), byrow = FALSE)
```

```
> x
```

	[, 1]	[, 2]
[1,]	1	5
[2,]	2	6
[3,]	3	7
[4,]	4	8

Entering data row wise in a matrix

In case, the data has to be entered row wise, then a 4×2 -matrix X can be created with

```
> y = matrix( nrow=4, ncol=2,  
              data=c(1,2,3,4,5,6,7,8), byrow = TRUE)
```

```
> y
```

	[, 1]	[, 2]
[1,]	1	2
[2,]	3	4
[3,]	5	6
[4,]	7	8

Entering data row wise and column wise in a matrix

R Console

```
> x = matrix( nrow=4, ncol=2, data=c(1,2,3,4,5,6,7,8) )
```

```
> x
```

	[,1]	[,2]
[1,]	1	5
[2,]	2	6
[3,]	3	7
[4,]	4	8

```
> y = matrix( nrow=4, ncol=2, data=c(1,2,3,4,5,6,7,8), byrow = TRUE )
```

```
> y
```

	[,1]	[,2]
[1,]	1	2
[2,]	3	4
[3,]	5	6
[4,]	7	8

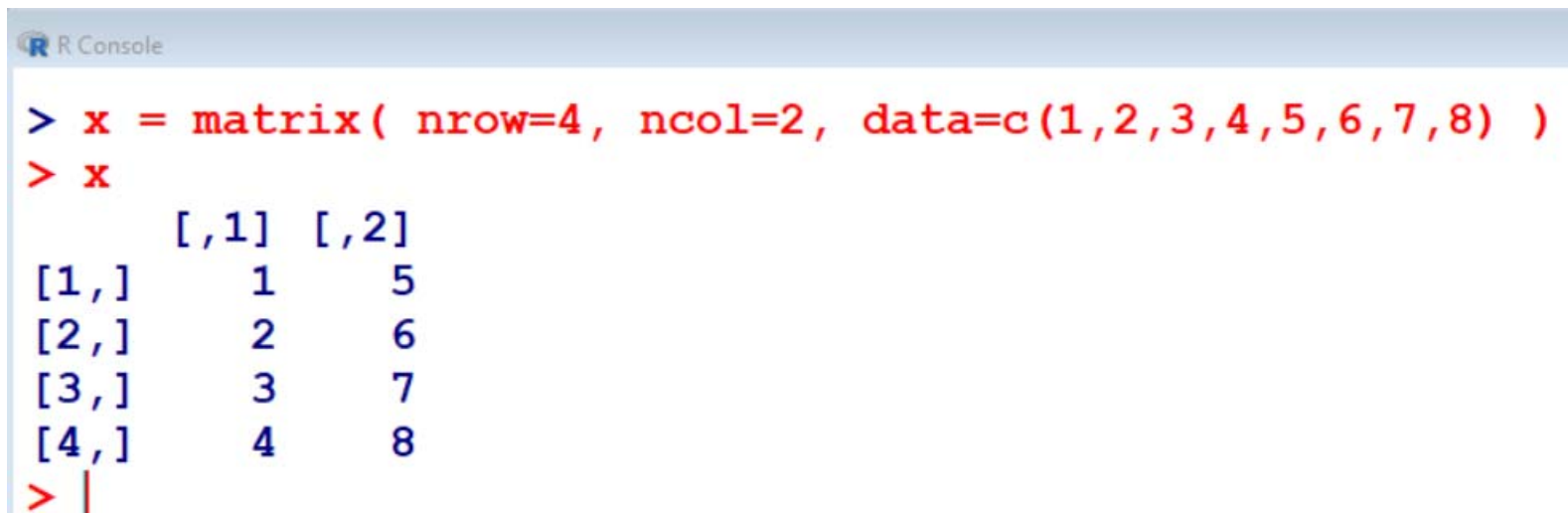
```
> |
```

In R, a 4×2 -matrix X can be created with a following command:

```
> x = matrix( nrow=4, ncol=2,  
              data=c(1,2,3,4,5,6,7,8) )
```

```
> x
```

	[,1]	[,2]
[1,]	1	5
[2,]	2	6
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[4,]	4	8



The screenshot shows an R console window with the following text:

```
R Console  
> x = matrix( nrow=4, ncol=2, data=c(1,2,3,4,5,6,7,8) )  
> x  
      [,1] [,2]  
[1,]    1    5  
[2,]    2    6  
[3,]    3    7  
[4,]    4    8  
> |
```

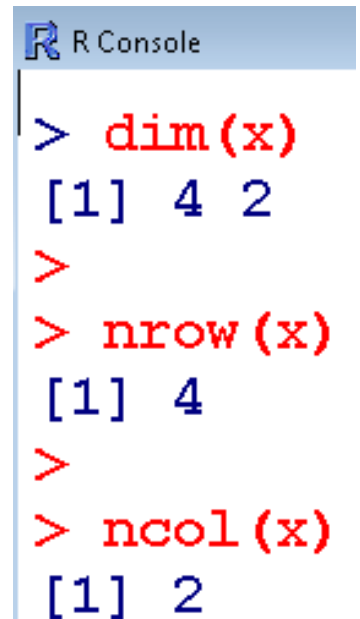
Properties of a Matrix

We can get specific *properties* of a matrix:

```
> dim(x) # tells the dimension of matrix  
[1] 4 2
```

```
> nrow(x) # tells the number of rows  
[1] 4
```

```
> ncol(x) # tells the number of columns  
[1] 2
```

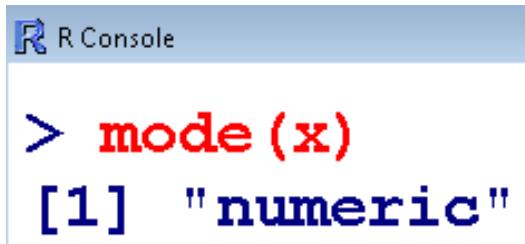
A screenshot of an R console window with a blue header bar containing the R logo and the text "R Console". The console shows three lines of R code and their corresponding outputs. The first line is "> dim(x)" in red, followed by the output "[1] 4 2" in blue. The second line is ">" in red. The third line is "> nrow(x)" in red, followed by the output "[1] 4" in blue. The fourth line is ">" in red. The fifth line is "> ncol(x)" in red, followed by the output "[1] 2" in blue.

```
> dim(x)  
[1] 4 2  
>  
> nrow(x)  
[1] 4  
>  
> ncol(x)  
[1] 2
```

Properties of a Matrix

> mode(x) **# Informs the type or storage mode of an object, e.g., numerical, logical etc.**

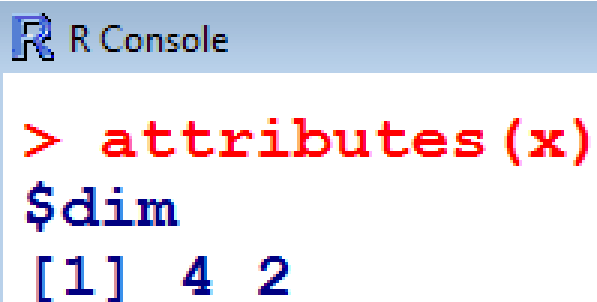
[1] "numeric"



```
R Console
> mode(x)
[1] "numeric"
```

attributes provides all the attributes of an object

> attributes(x) **#Informs the dimension of matrix**
\$dim [1] 4 2



```
R Console
> attributes(x)
$dim
[1] 4 2
```

Help on the Object "Matrix"

To know more about these important objects, we use R–help on "matrix".

```
> help("matrix")
```

matrix package:base R Documentation

Matrices

Description:

'matrix' creates a matrix from the given set of values.

'as.matrix' attempts to turn its argument into a matrix.

'is.matrix' tests if its argument is a (strict) matrix. It is generic: you can write methods to handle specific classes of objects, see Internal Methods.

Then we get an overview on how a matrix can be created and what parameters are available:

Usage:

```
matrix(data [= NA, nrow = 1, ncol = 1, byrow = FALSE,  
        dimnames = NULL)  
as.matrix(x)  
is.matrix(x)
```

Arguments:

data: an optional data vector.

nrow: the desired number of rows

ncol: the desired number of columns

byrow: **logical**. If '**FALSE**' (the default) the matrix is filled by columns, otherwise the matrix is filled by rows.

dimnames: A '**dimnames**' attribute for the matrix: a '**list**' of length 2.

x: an R object.

Then, the meaning of each parameter is explained:

Details:

If either of `'nrow'` or `'ncol'` is not given, an attempt is made to infer it from the length of `'data'` and the other parameter.

If there are too few elements in `'data'` to fill the array, then the elements in `'data'` are recycled. If `'data'` has length zero, `'NA'` of an appropriate type is used for atomic vectors and `'NULL'` for lists.

`'is.matrix'` returns `'TRUE'` if `'x'` is a matrix (i.e., it is `_not_` a `'data.frame'` and has a `'dim'` attribute of length 2) and `'FALSE'` otherwise.

`'as.matrix'` is a generic function. The method for data frames will convert any non-numeric/complex column into a character vector using `'format'` and so return a character matrix, except that all-logical data frames will be coerced to a logical matrix.

Finally, references and cross-references are displayed...

References:

Becker, R. A., Chambers, J. M. and Wilks, A. R. (1988) *The New S Language*. Wadsworth & Brooks/Cole.

See Also:

`'data.matrix'`, which attempts to convert to a numeric matrix.

.. as well as an example:

Examples:

```
is.matrix(as.matrix(1:10))  
data(warpbreaks)  
!is.matrix(warpbreaks) # data.frame, NOT matrix!  
warpbreaks[1:10,]  
as.matrix(warpbreaks[1:10,]) #using  
as.matrix.data.frame(.) method
```