

NPTEL COURSE ON
MATHEMATICS IN INDIA:
FROM VEDIC PERIOD TO MODERN TIMES

LECTURE 2

Vedas and Sulbasūtras - Part 1

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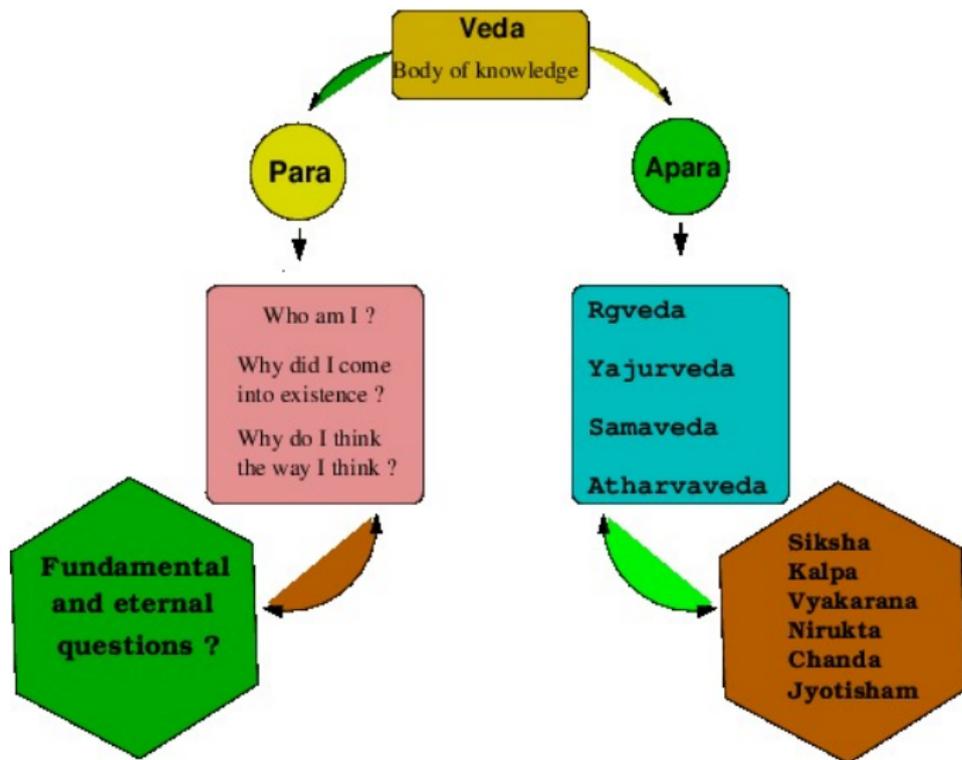
Outline

Mathematics in the Antiquity: *Vedas* and *Śulbasūtras* – Part 1

- ▶ Introduction
- ▶ Mathematical references in *Vedas*
- ▶ What are *Śulbasūtra* texts?
- ▶ What does the word *Śulbasūtra* mean?
- ▶ Qualities of a *Śulbakāra*
- ▶ Finding the cardinal directions
- ▶ Methods for obtaining perpendicular bisector
- ▶ Bodhāyana method of constructing a square
- ▶ The *Śulba* theorem (Bodhāyana & Mānava version)
- ▶ A few triplets listed in *Śulbasūtras* (general principle?)
- ▶ Applications of *Śulba* theorem

Introduction

Broad classification of Knowledge – *Muṇḍaka-Upaniṣad*



Mathematical references in Vedas

Citations that unambiguously point to the decimal system being in vogue

- ▶ In *Kṛṣṇa-Yajur-Veda* we find an interesting passage wherein a sequence of **ascending** numbers appear in the context of offering veneration to Agni (Fire God).

सकृत्ते अग्ने नमः । द्विस्ते नमः । त्रिस्ते नमः । ...

दशकृत्वस्ते नमः । शतकृत्वस्ते नमः । आसहस्रकृत्वस्ते नमः ।

अपरिमितकृत्वस्ते नमः ।

नमस्ते अस्तु मा मा हिंसीः ।¹

O fire, salutations unto you once. Salutations twice.

Salutations thrice ...

Salutations ten times. Salutations hundred times.

Salutations a thousand times.

Salutations unto you unlimited times.

My veneration to you, never ever hurt me.

¹ *Taittirīya Āraṇyakam* 4.69.

Mathematical references in Vedas

Citations that unambiguously point to the decimal system being in vogue

- ▶ We find yet another passage presenting a list of powers of 10 starting from hundred (10^2) to a trillion (10^{12}).

शताय स्वाहा सहस्राय स्वाहायुताय स्वाहा नियुताय स्वाहा
प्रयुताय स्वाहार्बुदाय स्वाहा न्यर्बुदाय स्वाहा समुद्राय स्वाहा,
मध्याय स्वाहान्ताय स्वाहा ... परार्धाय स्वाहा²

*Hail to hundred, ... hail to hundred thousand ... hail to
hundred million ... hail to trillion.*

- ▶ We also find a list of odd numbers and multiples of four occurring in *Taittirīya-saṃhitā* (4.5.11):

- ▶ एका च मे तिस्रश्च मे पञ्च च मे ... एकत्रिंशच्च मे
त्रयस्त्रिंशच्च मे
- ▶ चतस्रश्च मेऽष्टौ च मे द्वादश च मे ... चतुश्चत्वारिंशच्च
मेऽष्टाचत्वारिंशच्च मे

² *Taittirīya-saṃhitā* 7.2.49.

Mathematical references in Vedas

Citations that unambiguously point to the decimal system being in vogue

- In the second *Maṇḍala* of *R̥g-veda* we find multiples of ten listed.

ता विंशत्या त्रिंशता या ह्यर्वाक् चत्वारिंशता हरिभिर्युजानः ।

ता पञ्चाशता स्रसेभिरिन्द्र षष्ट्या सप्तत्या सोम पेयम् ॥

अशीत्या नवत्या याह्यर्वाक् शतेन हरिभिरुह्यमानः ।

अयं हि ते ...

[*R̥g-veda* 2.18.5-6.]

O Indra, Please come with twenty, thirty, forty horses ... with sixty, seventy ... carried by hundred horses.

- Elsewhere we find the appearance of an interesting number 3339.

त्रीणि शता त्रीसहस्राण्यग्निं त्रिंशश्च देवा नव चासपर्यन् ।

औक्षन् घृतैरसृणन् बर्हिरस्मा ...

[*R̥g-veda* 3.9.9.]

It is interesting to note that $3339 = 33 + 303 + 3003$, and is also close to 18 years (\approx period of eclipse cycle).

- We also find a *mantra* referring to the notion of infinite (∞).

पूर्णमदः पूर्णमिदं ...

पूर्णस्य पूर्णमादाय पूर्णमेवाव शिष्यते ॥

Mathematics in the *Śulbasūtra* texts

What are these texts, and where do they fall in the Vedic corpus?

- ▶ One of the prime occupations of the vedic people seem to have been **performing sacrifices**, for which altars of prescribed shapes and sizes were needed.
- ▶ Recognizing that manuals would be greatly helpful in constructing such altars, the vedic priests have composed a class of texts called *Śulba-sūtras*.
- ▶ These texts (earliest of which is dated prior to 800 BCE), form a part of much larger corpus known as *Kalpasūtras* that include:
 - ▶ **श्रौत** – Employed in rituals associated with societal welfare.
 - ▶ **गृह्य** – Rituals related to household.
 - ▶ **धर्म** – Duties³ and General code of conduct.
 - ▶ **शुल्ब** – Geometry of the construction of fire-altar.

³ *Ādi Śaṅkara* in his commentary on *Upaniṣads* defines the term *dharmā* as *anuṣṭheyānām sāmānyavacanam*.

The extant Śulbasūtras

- ▶ So far seven different Śulbasūtra texts have been identified by scholars. They are:
 1. *Baudhāyana Śulbasūtra*
 2. *Āpastamba Śulbasūtra*
 3. *Kātyāyana Śulbasūtra*
 4. *Mānava Śulbasūtra*,
 5. *Maitrāyana Śulbasūtra*
 6. *Vāraha Śulbasūtra* and
 7. *Vādhūla Śulbasūtra*
- ▶ Of them, *Bodhāyana Śulbasūtra* is considered to be the most ancient one.⁵ (prior to 800 BCE).
- ▶ It also presents a **very systematic and detailed** treatment of several topics that are skipped in later texts.
- ▶ It is made up of **three chapters** constituting about 520 *sūtras* (113 + 83 + 323).

⁵This assessment is based upon the style, completeness, and certain **archaic** usages that are not that frequently found in later texts.

Commentaries on *Śulbasūtras*

The table below presents a list of some of the important commentaries on three 'earlier' *Śulbasūtras*:

<i>Śulbasūtra</i>	Name of the comm.	Author
Bodhāyana	<i>Śulbadīpikā</i>	Dvārakānātha Yajvā
	<i>Śulba-mīmāṃsā</i>	Venkaṭeśvara Dīkṣita
Āpastamba	<i>Śulbavyākhyā</i>	Kapardisvāmin
	<i>Śulbapradīpikā</i>	Karavindasvāmin
	<i>Śulbapradīpa</i>	Sundararāja
	<i>Śulbabhāṣya</i>	Gopāla
Kātyāyana	<i>Śulbasūtravivṛtti</i>	Rāma/Rāmacandra
	<i>Śulbasūtravivarāṇa</i>	Mahīdhara
	<i>Śulbasūtrabhāṣya</i>	Karka

Qualities of a Śulbakāra

- ▶ Mahīdhara (c. 17th cent) in his *vivṛti* on *Kātyāyanaśulbasūtra* succinctly describes the qualities of a śulbakāra.

सङ्ख्याज्ञः परिमाणज्ञः समसूत्रनिरञ्छकः ।

समसूत्री भवेद्विद्वान् शुल्बवित् परिपृच्छकः ॥

शास्त्रबुद्धिविभागज्ञः परशास्त्रकुतूहलः ।

शिल्पिभ्यः स्थपतिभ्यश्चाप्याददीत मतीः सदा ॥

तिर्यङ्गान्याश्च सर्वार्थः पार्श्वमान्याश्च योगवित् ।

करणीनां विभागज्ञः नित्योद्युक्तश्च सर्वदा ॥

A śulbakāra must be **versed in arithmetic**, **versed in mensuration**, ... must be an inquirer, quite knowledgeable in one's own discipline, **must be enthusiastic in learning other disciplines**, always willing to learn from [practising] sculptors and architects ... and **one who is always industrious**.

- ▶ The above anonymous citation clearly brings forth the point that a śulbakāra, is **far more than a mere geometer**.

Topics covered in the *Baudhāyana-śulbasūtra*

Sanskrit name	Their English equivalent
रेखामानपरिभाषा	Units of linear measurement
चतुरश्रकरणोपायः	Construction of squares, rectangles, etc.
करण्यानयनम्	Obtaining the surds/Theorem of the square of the diagonal
क्षेत्राकारपरिणामः	Transformation of geometrical figures
नानाविधवेदिविहरणम् ⁶	Plan for different sacrificial grounds (<i>dārśa</i> , <i>paśubandha</i> , <i>śutrāmaṇi</i> , <i>agniṣṭoma</i> etc.)
अग्नीनां प्रमाणक्षेत्रमानम्	Areas of the sacrificial fires/altars
इष्टकसङ्ख्यापरिमाणादिकथनम्	Specifying the number of bricks used in the construction of altars including their sizes and shapes.
इष्टकोपधाने शैत्यादिनिर्णयः	Choosing clay, sand, etc. in making bricks
इष्टकोपधानप्रकारः	Process of manufacturing the bricks
श्येनचिदाद्वाकारनिरूपणम्	Describing the shapes of <i>śyenaciti</i> , etc.

⁶In fact the text commences with the *sūtra*

अथेमे ऽग्निचयाः । (Now we describe the fire altars).

Expression for the surds given in *Śulbasūtra* texts

- ▶ Besides presenting the details related to the construction of altars—that generally possess a bilateral symmetry—the *Śulba-sūtra* texts also present different interesting approximations for surds.
- ▶ The motivation for presenting estimates of surds could be traced to the attempts of vedic priests
 - ▶ to solve the problem of “squaring a circle” and vice versa
 - ▶ to construct a square whose area is n times the area of a give square, and so on.
- ▶ The expressions for surds presented in the form

$$N = N_0 + \frac{1}{n_1} + \frac{1}{n_1 n_2} + \frac{1}{n_1 n_2 n_3} + \dots,$$

can be understood in different ways, of which we will describe the Geometrical construction.

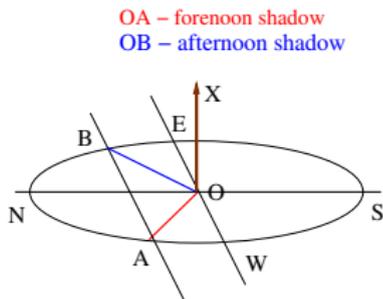
Topics that we plan to discuss

- ▶ Finding the cardinal directions using *śanku*.
- ▶ Construction of perpendicular bisectors.
- ▶ Construction of **rectilinear** (square, trapezia, etc.) and **curvilinear** (circles, *vedis*, etc.) geometrical objects.
- ▶ **Enunciation of geometric principles** and practical application of them. We demonstrate it with
 - ▶ **Transformation of one geometrical object into another** by applying these principles.
 - ▶ Obtaining **the value of surds** by means of geometrical construction.
- ▶ **Estimating the value** of surds (in the form of a sequence of rational numbers).
- ▶ Construction of altars (*citis*) of different sizes and shapes (falcons, tortoise, chariot wheel, and so on).

Determining the east-west line

- ▶ Determining the exact east-west line at a given location, is a pre-requisite for all constructions, be it a residence, a temple, a sacrificial altar or a fire-place.
- ▶ The procedure for its determination is described thus:

समे शङ्कुं निखाय 'शङ्कुसम्मितया रज्ज्वा' मण्डलं परिलिख्य यत्र लेखयोः
शङ्कुग्रच्छाया निपतति तत्र शङ्कु निहन्ति, सा प्राची। [Kt. Su. 1 2]



Fixing a pin (or gnomon) on levelled ground and drawing a circle with a cord measured by the gnomon,⁷ he fixes pins at points on the line (of the circumference) where the shadow of the tip of the gnomon falls. That gives the east-west line (*prācī*).

⁷This prescription implies $r > 2OX$, and has astronomical significance. 

Time from shadow measurement (not in *Śulbasūtras*)

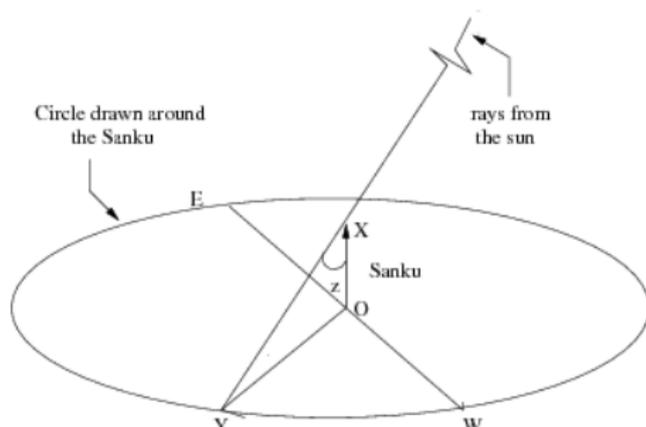


Figure: Zenith distance and the length of the shadow.

$$t = (R \sin)^{-1} \left[\frac{R \cos z}{\cos \phi \cos \delta} \pm R \sin \Delta\alpha \right] \mp \Delta\alpha.$$

If ϕ and δ are known ($\Delta\alpha = f(\phi, \delta)$), then t is known.

Why perform experiment to determine the directions?

- Posing the question – **why not simply look at the sunrise or sunset**, and be with it to find the east? – the commentator Mahīdhara observes:

...तस्य उदयस्थानानां बहुत्वात् प्रतिदिनं भिन्नत्वात् अनियमेन प्राची ज्ञातुं न शक्या । तस्मात् शङ्कुस्थापनेन प्राचीसाधनमुक्तम् । दक्षिणायने चित्रापर्यन्तमर्कोऽभ्युदेति । मेषतुलासङ्क्रान्त्यहे प्राच्यां शुद्धायामुदेति । ततोऽर्कात् प्राचीज्ञानं दुर्घटम् ।

Since **the rising points are many**, **varying from day to day**, the [cardinal] east point **cannot be known** [from the sunrise point]. Therefore it has been prescribed that the east be determined by fixing a *śarīku*. ... **Therefore, simply looking at the sun and determining the east is difficult.**

- Having obtained the east-west direction, the next problem is to find out north-south. How to do that?

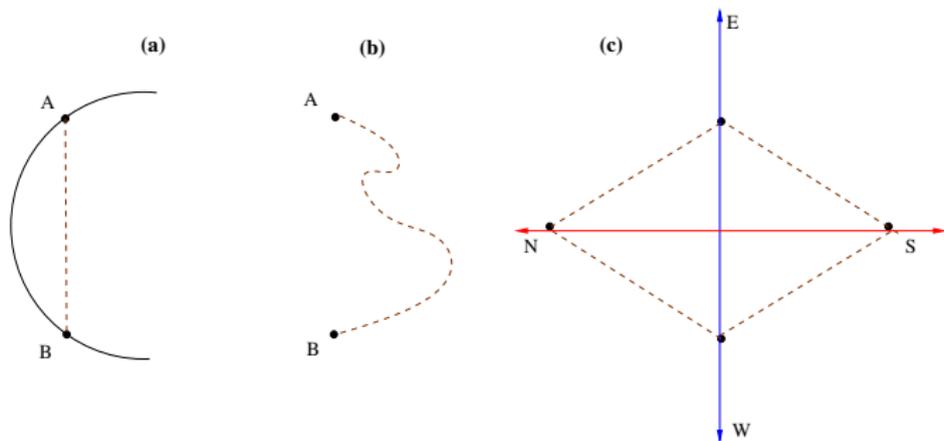
Methods for obtaining perpendicular bisector

- ▶ Two methods have been described for obtaining the perpendicular bisector of a given straight line:
 - ▶ रज्ज्वभ्यसनम् (folding the cord)
 - ▶ मत्स्यचित्रणम् (drawing fish-figure)
- ▶ How to draw a perpendicular bisector using the cord-folding method is discussed by Kātyāyana, in the third *sūtra* right at the beginning of his text.
- ▶ Having obtained *prācī*, getting *udicī* (the north-south line), correctly is extremely important for the construction of various altars **having bilateral symmetry**.

Construction of perpendicular bisector: Cord-folding method

तदन्तरं रज्ज्वाभ्यस्य, पाशौ कृत्वा, शङ्कोः पाशौ प्रतिमुच्य, दक्षिणायम्य मध्ये शङ्कुं निहन्ति। एवमुत्तरतः, सोदीची।

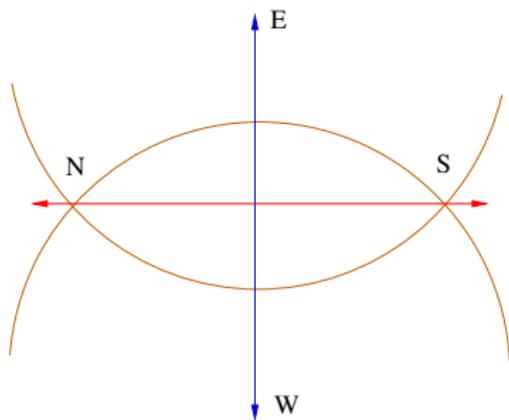
Doubling the cord by a measure of distance between them (*śaṅkus*), ... and stretching (the cord) towards the south, strikes a pin at the middle point



In the figure above, in (a), A and B represent pins along east-west direction to which the cord is tied. In (b), we've doubled the cord AB. (c) represents stretching AB on both sides to get the north-south direction.

Construction of perpendicular bisector: Fish-figure method

- ▶ In this method, as shown in the figure below, having obtained the **east-west direction** by the shadow of the *śarīku*, we mark two points along the east-west line.
- ▶ With those points as centres, and choosing an appropriate radius, **circular arcs** are drawn.
- ▶ The line passing through the intersection points of these two arc gives the **north-south direction**.

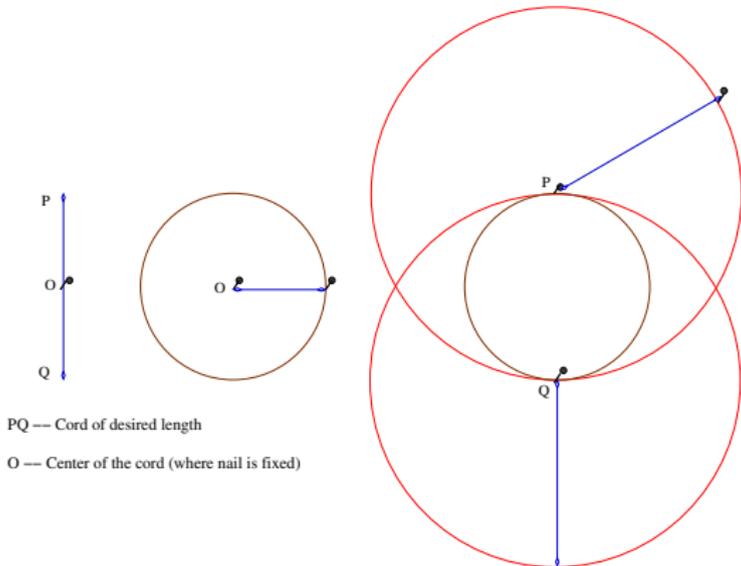


Bodhayana's method of constructing a square

Systematic procedure that involves cord & nails, but **NO OTHER MEASURING DEVICE**

चतुरश्रं चिकीर्षन् यावच्चिकीर्षत् तावतीं रज्जुं उभयतः पाशं कृत्वा मध्ये लक्षणं करोति ।
लेखामालिख्य तस्य मध्ये शङ्कुं निहन्यात् । तस्मिन् पाशौ प्रतिमुच्य लक्षणेन मण्डलं
परिलिखेत् । विष्कम्भान्तयोः शङ्कुं निहन्यात् । पूर्वस्मिन् पाशं प्रतिमुच्य

Desirous of constructing a square, may you take a cord of that length, tie it at both the ends and mark its centre. Draw a line and fix a nail at its centre. Latching the ends ...



Bodhayana's method of constructing a square

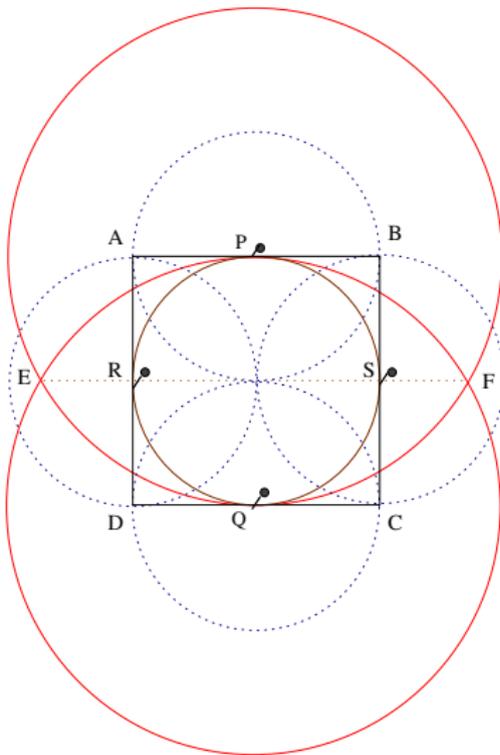
Systematic procedure that involves cord & nails, but NO OTHER MEASURING DEVICE

पाशेन मण्डलम् परिलिखेत्।
एवमपरस्मिन्। ते यत्र
समेयातां, तेन द्वितीयं विष्कम्भं
आयच्छेत्। विष्कम्भान्तयोः शङ्कु
निहन्यात्। पूर्वस्मिन् पाशौ
प्रतिमुच्य लक्षणेन मण्डलं
परिलिखेत्। एवं दक्षिणेन एवं
पश्चात्देवमुत्तरतः। तेषां ये
अन्त्याः संसर्गाः तच्चतुरश्रं
सम्पद्यते।

May you draw a circle.

Similarly on the other side.

From their points of
intersection (E,F), obtain the
second diameter (RS) ...



The Śulva (Pythagorean?) theorem

- ▶ A clear enunciation of the so-called ‘Pythagorean’ theorem — called *bhujā-koṭi-karṇa-nyāya* in the later literature — is described in *Bodhāyana Śulvasūtra* (1.12) as follows:

दीर्घचतुरश्रस्य अक्षण्यारज्जुः⁸ पार्श्वमानी तिर्यङ्मानी च यत्
पृथग्भूते कुरुतः तदुभयं करोति ।

The rope corresponding to the **the diagonal** of a rectangle makes whatever is made by the **lateral** and the **vertical** sides individually.

Terms	their meaning
दीर्घचतुरश्रम्	– Rectangle (lit. longish 4-sided figure)
अक्षण्या रज्जुः	– the diagonal rope
पार्श्वमानी	– the measure of the lateral side
तिर्यङ्मानी	– the measure of the perpendicular side

⁸The word *akṣṇayā* is archaic and hardly occurs in classical literature:

अक्षण्या व्याघारयति । ... तस्मादक्षण्या पशवोऽङ्गानि प्रतितिष्ठन्ति ।

Kātyāyana version of Śulva theorem (with comm.)

- ▶ The Kātyāyana version of the theorem seems to be a redacted form of what appears in *Bodhāyana Śulvasūtra*.

दीर्घचतुरश्रस्य अक्षण्यारञ्जुः तिर्यङ्गानी पार्श्वमानी च यत्
पृथग्भूते कुरुतः तद्भुमयं करोति इति क्षेत्रज्ञानम्। [KSS 2.7]

- ▶ But for swapping two words, there is only one difference; The phrase '*iti kṣetrajñānam*' has been added ⇒ **that this is the most fundamental theorem in geometry to be known** whose knowledge **cannot be dispensed with**.
- ▶ Commenting on this *Mahādhara* observes:

दीर्घचतुरश्रस्य तिर्यङ्गानीपार्श्वमान्यौ रञ्जु पृथग्भूते सत्यौ यत्क्षेत्रं
= यत्फलकं क्षेत्रं समचतुरश्रद्वयं कुरुतः, तद्भुमयमपि मिलितं
दीर्घचतुरश्रस्य अक्षण्या = कोणसूत्रभूता रञ्जुः करोतीति इति
क्षेत्रज्ञानम् = क्षेत्रमानप्रकारो ज्ञातव्यः।

Mānava version of the *Śulva* theorem

- ▶ The presentation of the theorem in *Mānava-śulvasūtra* differs from *Bodhāyana Śulvasūtra* both in form and in style.
- ▶ Here it is given in the form of a verse as follows:

आयामं आयामगुणं विस्तारं विस्तरेण तु ।
समस्य वर्गमूलं यत् तत् कर्णं तद्विदो विदुः ॥

Terms	their meaning
आयामं आयामगुणं	– the length multiplied by itself
विस्तारं विस्तरेण तु	– and indeed the breadth by itself
समस्य वर्गमूलं	– the square root of the sum
तत् कर्णम्	– that is hypotenuse
तद्विदो विदुः	– those versed in the discipline say so

- ▶ Using modern notation the result may be expressed as:

$$\sqrt{\text{āyāma}^2 + \text{vistāra}^2} = \text{karṇa}.$$

Some 'Pythagorean' triplets listed in *Śulbasūtras*

- ▶ In the very next *sūtra* following the statement of the theorem, Bodhāyana illustrates it with a few examples:

तासां त्रिकचतुष्कयोः, द्वादशिकपञ्चिकयोः, पञ्चदशिकाष्टिकयोः,
सप्तिकचतुर्विंशिकयोः, द्वादशिकपञ्चत्रिंशिकयोः,
पञ्चदशिकषट्त्रिंशिकयोः इत्येतासु उपलब्धिः। [BSS 1.13]

$$\begin{aligned}3^2 + 4^2 &= 5^2 \\5^2 + 12^2 &= 13^2 \\15^2 + 8^2 &= 17^2 \\7^2 + 24^2 &= 25^2 \\12^2 + 35^2 &= 37^2 \\15^2 + 36^2 &= 39^2\end{aligned}$$

What is interesting to note is the use of the phrase

इत्येतासु उपलब्धिः।

[the general rule stated above] is quite evident in these pairs.

Is there a rationale behind the choice of these examples?

- ▶ A few triplets listed in the *Āśvalāyana-śulbasūtra* includes:

(15, 20, 25) (16, 12, 20)

Rationale behind the choice of examples

Conjecture put forth by Datta (pp. 133-136)

- ▶ One of the Kātyāyana-sūtras presents the relation

$$na^2 = \left(\frac{n+1}{2}\right)^2 a^2 - \left(\frac{n-1}{2}\right)^2 a^2$$

- ▶ Substituting $n = m^2$, and $a = 1$, we at once get

$$m^2 + \left(\frac{m^2-1}{2}\right)^2 = \left(\frac{m^2+1}{2}\right)^2. \quad (1)$$

- ▶ Here, putting $m = 3, 5, 7$ immediately $\rightsquigarrow (3,4,5), (5,12,13), (7,24,25)$.
- ▶ Rewriting the above equation in the form

$$(2m)^2 + (m^2 - 1)^2 = (m^2 + 1)^2, \quad (2)$$

and substituting $m = 2, 4, 6 \rightsquigarrow (3,4,5), (8,15,17), (12,35,37)$.

- ▶ How about the other example of Bodhāyana (15,36,39)?

Principle behind generating right-rational triangles

Described by Āpastamba in the context *Saumikī-vedī*

त्रिकचतुष्कयोः पञ्चिका अक्षणयारज्जुः । तामिः त्रिरभ्यस्तामिः अंसौ ।

चतुरभ्यस्तामिः श्रेणी ।

[ASS 5.3]

द्वादशिकपञ्चिकयोः त्रयोदशिका अक्षणयारज्जुः । तामिः अंसौ । द्विरभ्यस्तामिः

श्रेणी ।

[ASS 5.3]

$$\begin{aligned} 3^2 + 4^2 &= 5^2 \\ (3 + 3.3)^2 + (4 + 3.4)^2 &= (5 + 3.5)^2 \quad (A) \\ 12^2 + 16^2 &= 20^2 \\ (3 + 4.3)^2 + (4 + 4.4)^2 &= (5 + 4.5)^2 \quad (B) \\ 15^2 + 20^2 &= 25^2 \\ 5^2 + 12^2 &= 13^2 \\ (5 + 2.5)^2 + (12 + 2.12)^2 &= (13 + 2.13)^2 \quad (C) \\ 15^2 + 36^2 &= 39^2 \end{aligned}$$

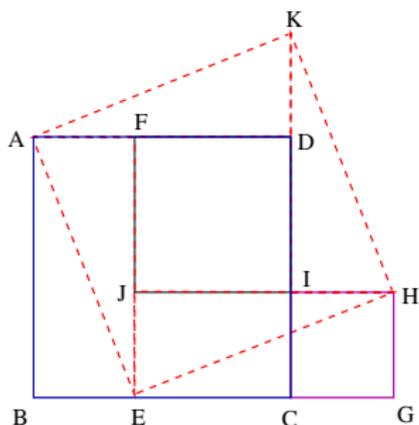
It seems Āpastamba has invoked the principle that if (a, b, c) satisfies the relation $a^2 + b^2 = c^2$, then (ma, mb, mc) also satisfies the same relation—where m is an arbitrary rational number.

Constructing a square that is sum of unequal squares

An application of the *Sūlba*-theorem

नानाचतुरश्रे समस्यन् कनीयसः करण्या वर्षीयसो वृध्रमुल्लिखेत् । वृध्रस्य
अक्षण्यारज्जुः समस्यतोः पार्श्वमानी भवति । (BSS 1.50)

Desirous of combining different squares, may you mark the rectangular portion of the larger [square] with a side (*karanyā*) of the smaller one (*kanīyasah*). The diagonal of this rectangle (*vrddhra*) is the side of the sum of the two [squares].

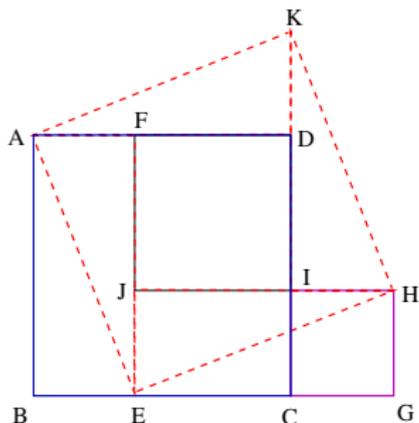


- ▶ The term *vrddhra* in the above *sūtra* refers to the rectangle ABEF.
- ▶ Asking us to mark this rectangle, all that the text says is the cord AE *akṣṇayārajjuḥ* gives the side of the sum of the squares.
- ▶ In other words,

$$\begin{aligned} AE^2 &= ABCD + CGHI \\ &= AB^2 + CG^2 \\ &= AB^2 + BE^2. \end{aligned}$$

Implication of the above construction ?

- ▶ Scholars trained in the Euclidean tradition, puzzled by the mere statement of theorem, without the so called 'proofs' always wondered whether the Śulbakāras knew the proof of Śulba-theorem, or was it purely based on empirical guess work?
- ▶ Though Śulvakāras do not give explicit proofs, it is quite implicit in the procedures described by them. In fact, the previous description of construction clearly forms an example of that.



- ▶ In the figure, ABCD and CGHI are the two squares to be combined. E is a point on BC such that $CG = BE$.
- ▶ ABEF is the rectangle that is formed. Now the sum of the two squares may be expressed as

$$\begin{aligned} ABCD + CGHI &= ABE + AEF + EHJ + EGH + FDIJ \\ &= KIH + AEF + EHJ + ADK + FDIJ \\ &= AEHK, \end{aligned}$$

which unambiguously proves the theorem.

Thanks!

THANK YOU

More about *Śulbasūtras* in the next lecture!