

Switched Mode Power Conversion

Transformers

Devices for Efficient Power Conversion

Switches

Inductors

Transformers

Capacitors

Switched Mode Power Conversion

Transformers

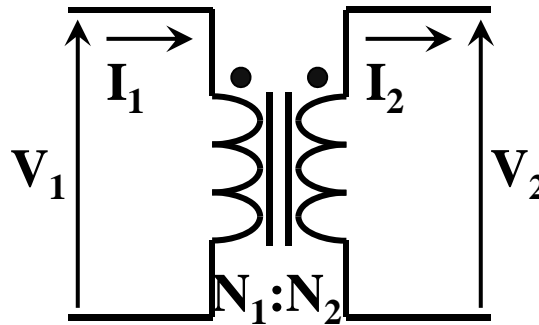
**Transformers Match Voltage Levels.
Ideally They Do Not Store Energy.**

**In Power Converters, Transformers
Provide Electrical Isolation as Well.**

Switched Mode Power Conversion

Transformers

Transformers Match Voltage Levels.

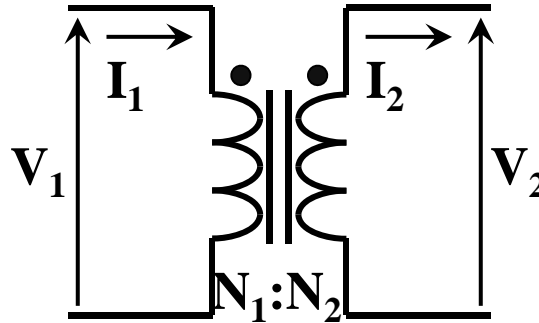


$$\frac{V_1}{V_2} = \frac{N_1}{N_2}$$

Switched Mode Power Conversion

Transformers

Transformers Provide Electrical Isolation

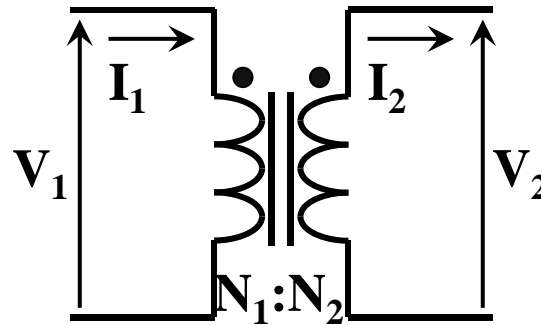


$$\frac{V_1}{V_2} = \frac{N_1}{N_2}$$

Switched Mode Power Conversion

Transformers

Efficiency of Power Conversion is Unity



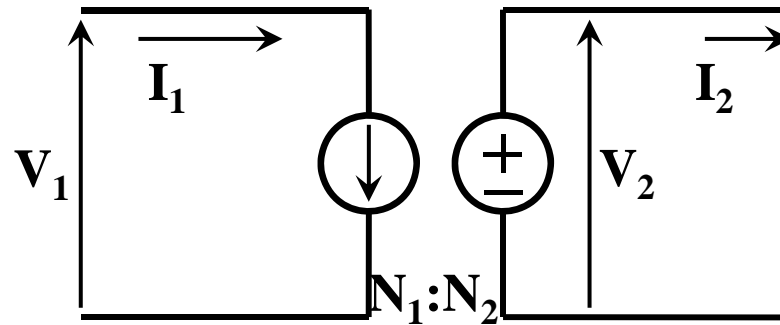
$$V_1 I_1 = V_2 I_2$$

$$\frac{V_1}{V_2} = \frac{I_2}{I_1} = \frac{N_1}{N_2}$$

Switched Mode Power Conversion

Transformers

Circuit Schematic



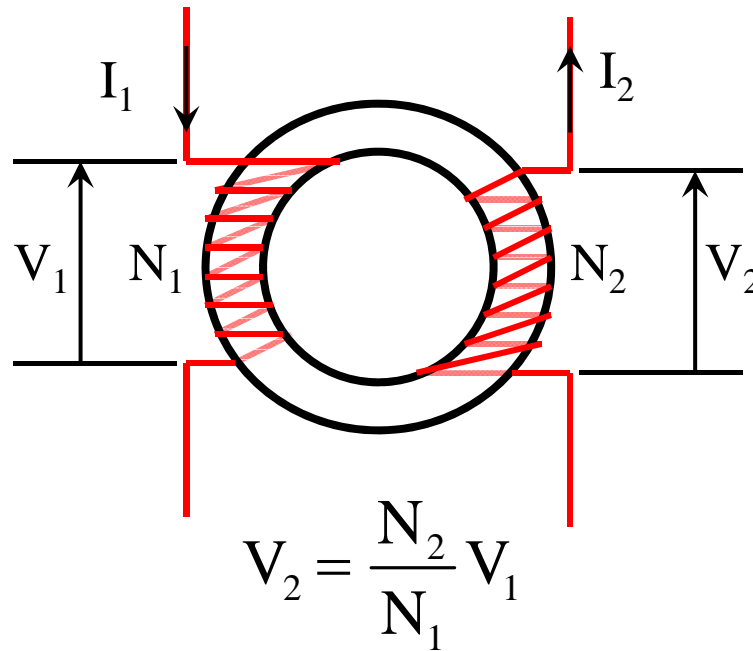
$$V_2 = \frac{N_2}{N_1} V_1$$

$$I_1 = \frac{N_2}{N_1} I_2$$

Switched Mode Power Conversion

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Magnetic Circuit

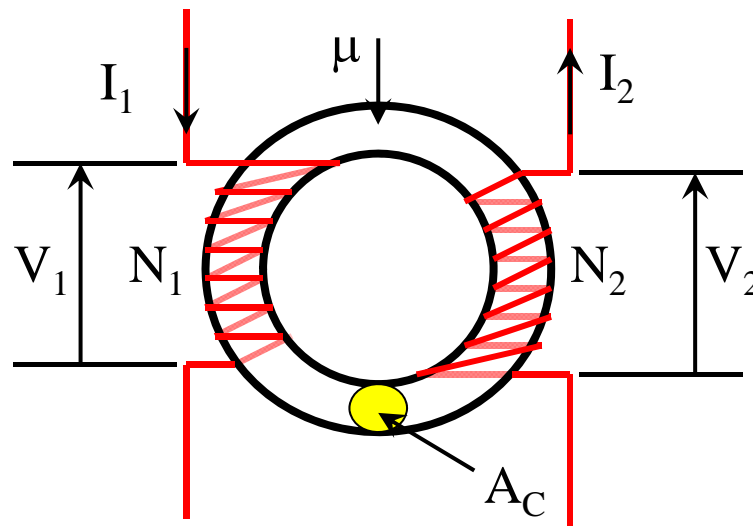


$$I_1 = \frac{N_2}{N_1} I_2$$

Switched Mode Power Conversion

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Magnetic Circuit

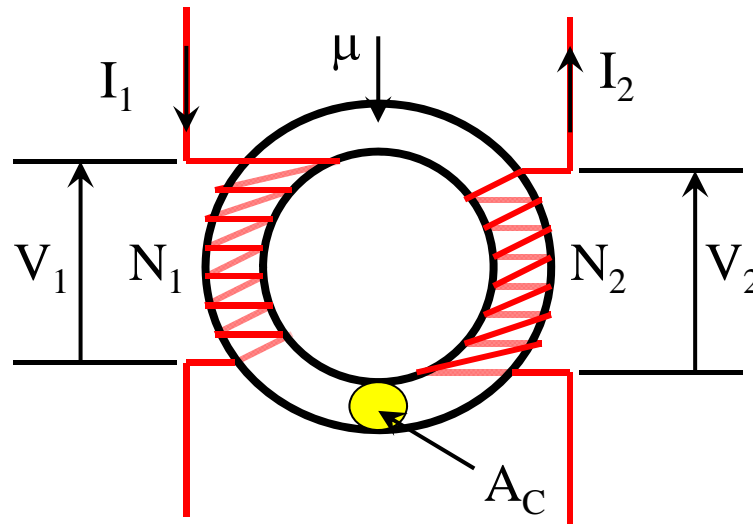


Transformer Does Not Store Energy
The Core Reluctance is Ideally Zero

Switched Mode Power Conversion

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Magnetic Circuit

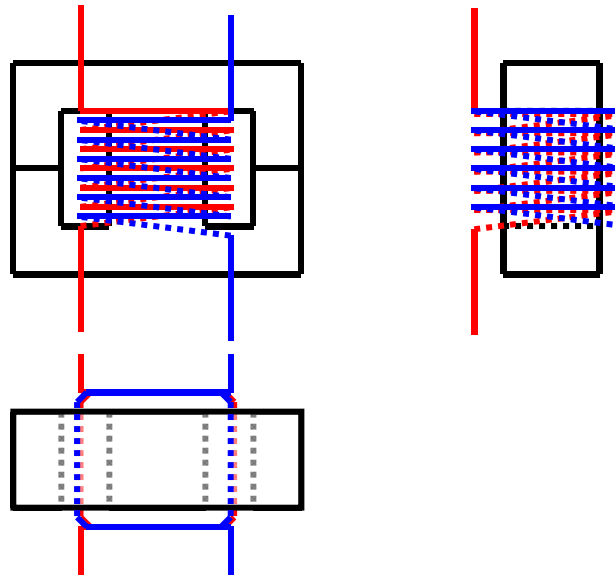


Core Shape is Chosen for Convenience

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Magnetic Circuit

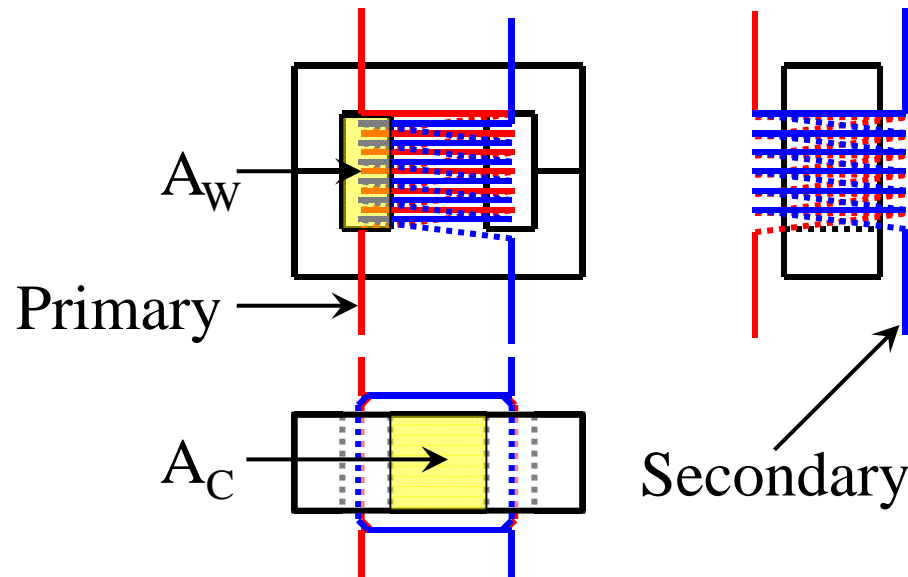


EE Cores

Switched Mode Power Conversion

Transformers

Magnetic Circuit

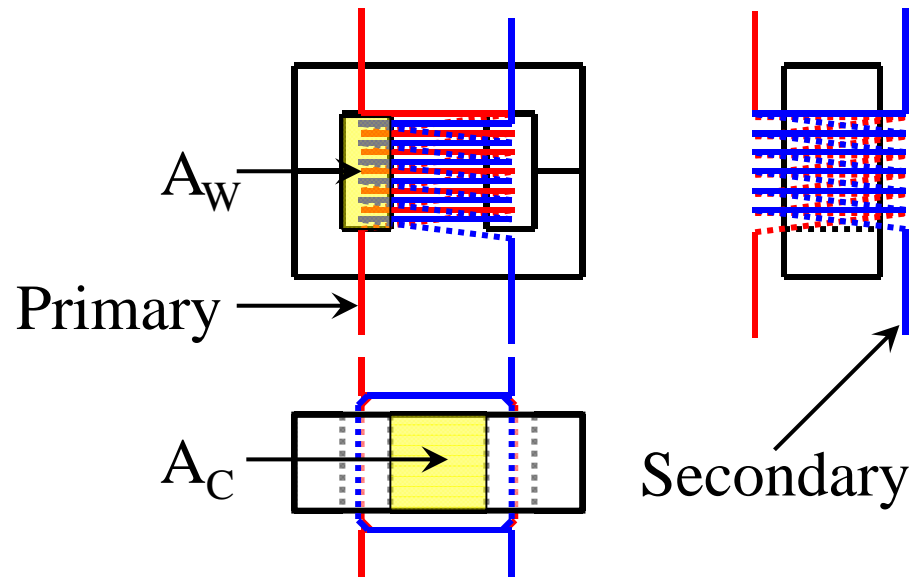


Window Accommodates Both Primary & Secondary
Core Links Both Primary & Secondary

Switched Mode Power Conversion

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Voltage Equation

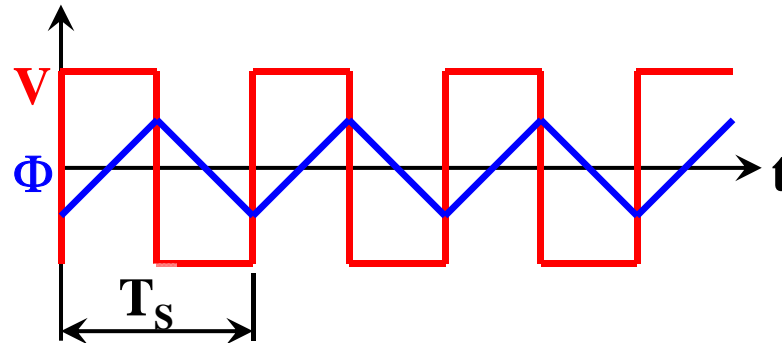


$$V_1 = N_1 \frac{d\Phi}{dt}; V_2 = N_2 \frac{d\Phi}{dt}$$

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Flux Waveform – Square Wave Primary Voltage



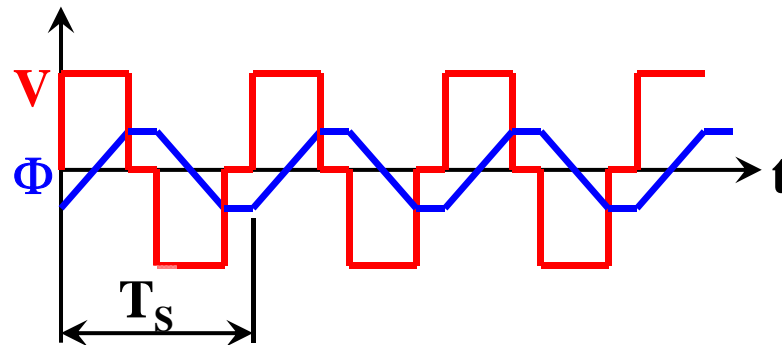
$$V = N \frac{d\Phi}{dt}$$

Flux Swings Symmetrically Between $-\Phi_m$ and $+\Phi_m$

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Quasi-Square Wave Primary Voltage



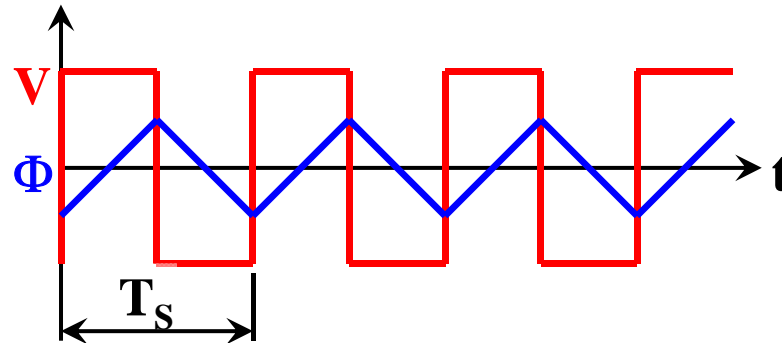
$$V = N \frac{d\Phi}{dt}$$

Flux Swings Symmetrically Between $-\Phi_m$ and $+\Phi_m$
Notice the Dwell Time in Flux

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Voltage – Core Area Equation



$$V = N \frac{2\Phi_m}{T_s / 2} = N * 4 * B_m * A_C * f_s$$

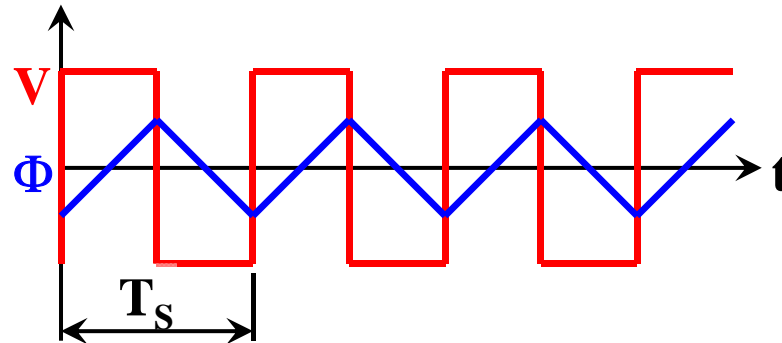
$$V_1 = N_1 * 4 * B_m * A_C * f_s ; V_2 = N_2 * 4 * B_m * A_C * f_s$$

Flux Swings Symmetrically Between $-\Phi_m$ and $+\Phi_m$

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Voltage – Core Area Equation



$$V_1 = 4N_1B_mA_Cf_s$$

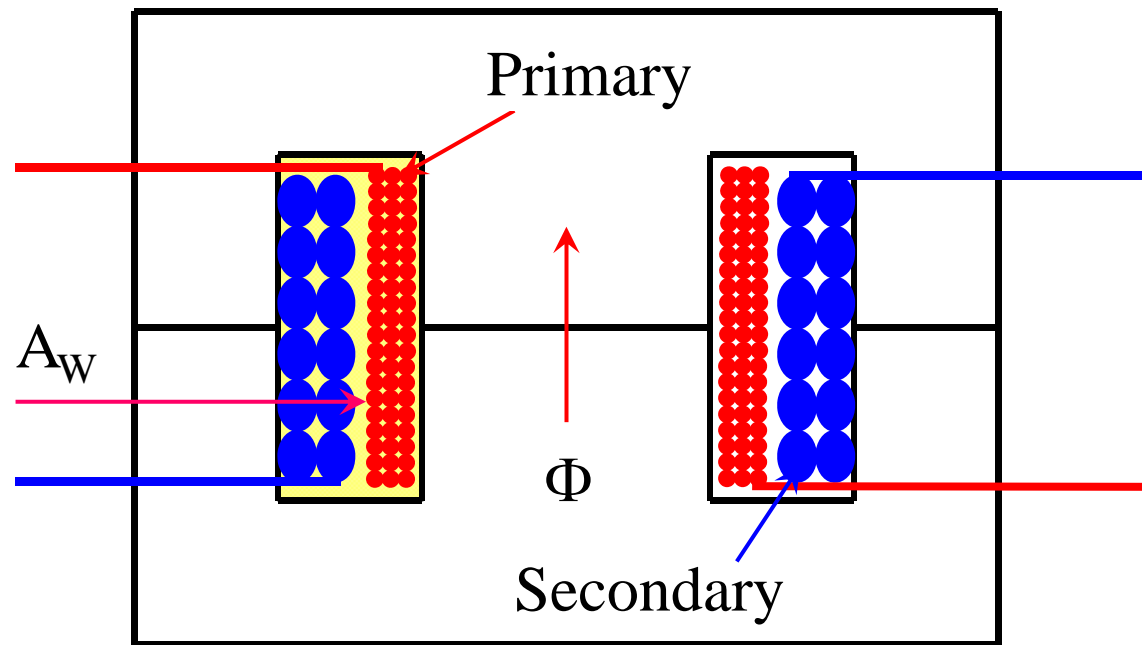
$$V_2 = 4N_2B_mA_Cf_s$$

A_C is a Function of Voltage and Frequency

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Window Space



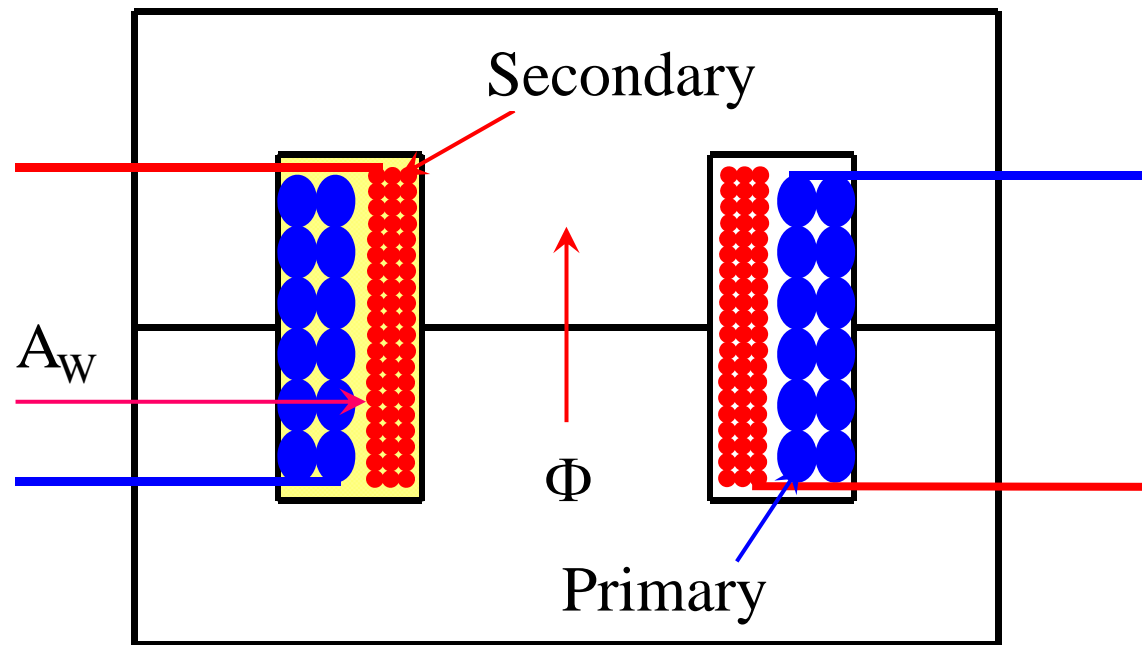
$$N_1 a_1 + N_2 a_2 = k_w A_w$$

A_w is a Function of Conductor Size & No. of Turns

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Window Space



$$N_1 \frac{I_1(\text{rms})}{J} + N_2 \frac{I_2(\text{rms})}{J} = k_w A_w$$

A_w is a Function of rms Currents

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Design Equations

$$V_1 = 4N_1B_mA_Cf_s$$

$V_1/2f_s$ is the Volt-Sec Integral

$2N_1B_mA_C$ is the Flux Linkage

$$2N_1 \frac{I_1(\text{rms})}{J} = k_w A_w$$

Primary Ampere-Turns Equal Secondary Ampere-Turns

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Area-Product Equation

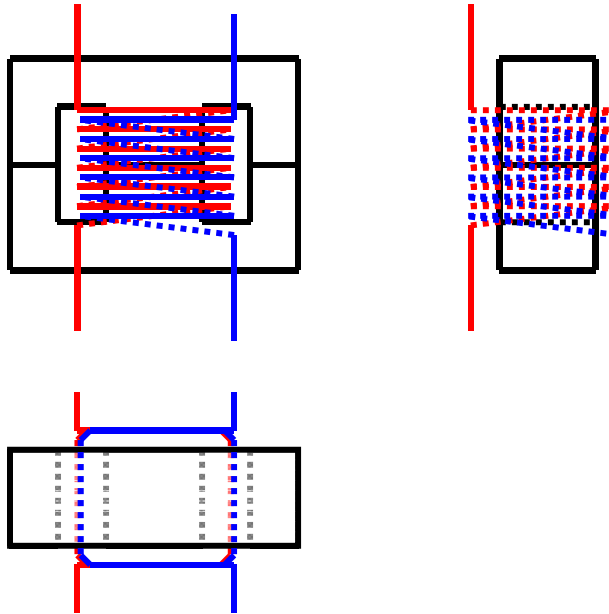
$$V_1 = 4N_1 B_m A_C f_s$$

$$2N_1 \frac{I_1(\text{rms})}{J} = k_w A_w$$

$$A_C A_w = \frac{V_1 I_1(\text{rms})}{2k_w B_m J f_s}$$

Switched Mode Power Conversion

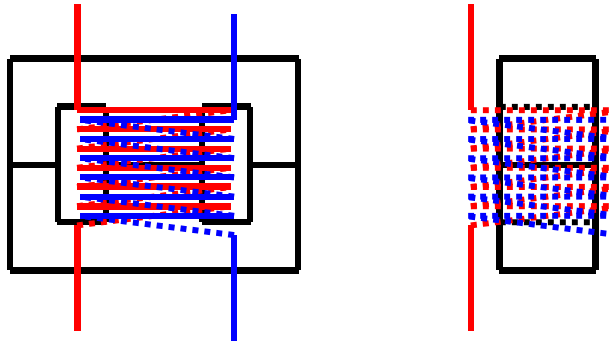
Popular Geometry (EE)



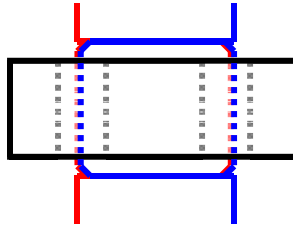
Notice the Low Reluctance (No Air Gap in the Core) Geometry

Switched Mode Power Conversion

Popular Geometry (EE)



$$L_{mp} = \frac{N_1^2}{\mathfrak{R}}$$



$$L_{ms} = \frac{N_2^2}{\mathfrak{R}}$$

On Account of Low Reluctance Magnetic Path
Magnetising Inductance is Infinity Ideally

Switched Mode Power Conversion

ETD Core Series Data

Type Number	$A_C \text{ mm}^2$	$A_W \text{ mm}^2$	$A_C A_W \text{ mm}^4$
ETD 29/16/10	76	128	9728
ETD 34/17/11	97	171	16587
ETD 39/20/13	125	234	29250
ETD 44/22/15	173	279	48267
ETD 49/25/16	211	343	72373
ETD 54/28/19	280	412	115360
ETD 59/31/22	368	473	174064

Standard Cores

ETD

Switched Mode Power Conversion

Few Other Geometries (EE)

Standard Cores

ETD

Low Profile Cores

EFD

Pot Cores

P

Switched Mode Power Conversion

Sample Core Selection

$V_1 = 48 \text{ V} ;$
 $V_2 = 400 \text{ V} ; I_2 = 3 \text{ A} ;$
High Frequency (50 kHz) Application

$$A_c A_w = \frac{400 * 3 * 10^{12}}{2 * 0.35 * 0.2 * 3 * 10^6 * 50000} = 57142 \text{ mm}^4$$

Switched Mode Power Conversion

ETD Core Series Data

Type Number	$A_C \text{ mm}^2$	$A_W \text{ mm}^2$	$A_C A_W \text{ mm}^4$
ETD 29/16/10	76	128	9728
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ETD 54/28/19	280	412	115360
ETD 59/31/22	368	473	174064

Select ETD 49/25/16

N67 Material

Switched Mode Power Conversion

No. of Turns

Type Number	$A_C \text{ mm}^2$	$A_W \text{ mm}^2$	$A_C A_W \text{ mm}^4$
ETD 49/25/16	211	343	72373
N_1	6		
N_2	47		

$$N = \frac{V}{4B_m A_C f_s} = \frac{48}{4 * 0.2 * 211 * 10^{-6} * 50000}$$

Select $N_1 = 6$ Turns ; $N_2 = 47$ Turns

Switched Mode Power Conversion

Wire Size

Type Number	$A_C \text{ mm}^2$	$A_W \text{ mm}^2$	$A_C A_W \text{ mm}^4$
ETD 49/25/16	211	343	72373
N_1	6		
N_2	47		
a_1	8.33 mm^2		
a_2	1 mm^2		

$$a_{w2} = \frac{3}{3} = 1 \text{ mm}^2$$

$$a_{w1} = 8.33 \text{ mm}^2$$

Switched Mode Power Conversion

Wire Size – Skin Effect

Type Number	$A_C \text{ mm}^2$	$A_W \text{ mm}^2$	$A_C A_W \text{ mm}^4$
ETD 49/25/16	211	343	72373
N_1	6		
N_2	47		
a_1	8.33 mm^2		
a_2	1 mm^2		

$$\text{Skin Depth} = \frac{1}{\sqrt{\pi \mu \sigma f}}$$

$$\mu = 4\pi 10^{-7} \text{ H/m}$$

$$\sigma = 59.6 \cdot 10^6 / \Omega - \text{m}$$

For Copper @50 kHz, Skin Depth = 0.29 mm : 0.26 mm² (24 SWG)

Switched Mode Power Conversion

Primary & Secondary Conductors

Type Number	$A_C \text{ mm}^2$	$A_W \text{ mm}^2$	$A_C A_W \text{ mm}^4$
ETD 49/25/16	211	343	72373
N_1	6		
N_2	47		
a_1	8.33 mm^2		
a_2	1 mm^2		

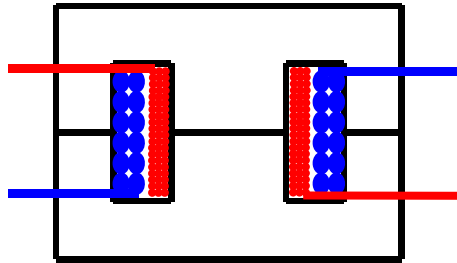
For Secondary 4 wires of 24 SWG in Parallel

For Primary 32 wires of 24 SWG in Parallel

Switched Mode Power Conversion

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Parasitic Resistance



Mean Length of a Turn: 83 mm

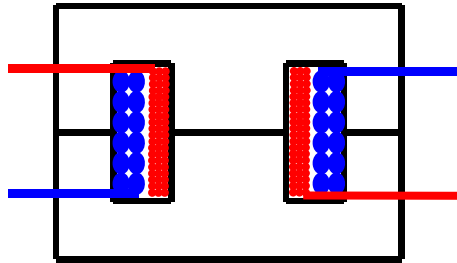
Primary Resistance: 10 $\mu\Omega$

Secondary Resistance: 629 $\mu\Omega$

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Core Loss



Loss at 0.2 T at 100 kHz: 15.5 W

Loss at 0.2 T at 50 kHz: 7.75 W

Core Loss Resistance: 297 Ω

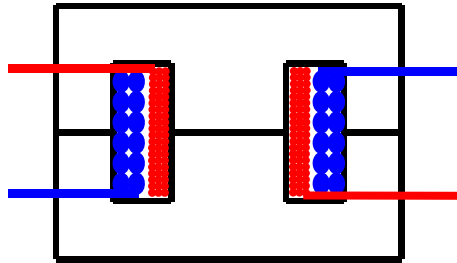
ETD 49/25/16

N67 Material

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Magnetising Inductance



$$l_e = 114 \text{ mm} ; A_C = 211 \text{ mm}^2 ; \mu_r = 1590$$

$$\text{Reluctance} = 270405 \text{ /H}$$

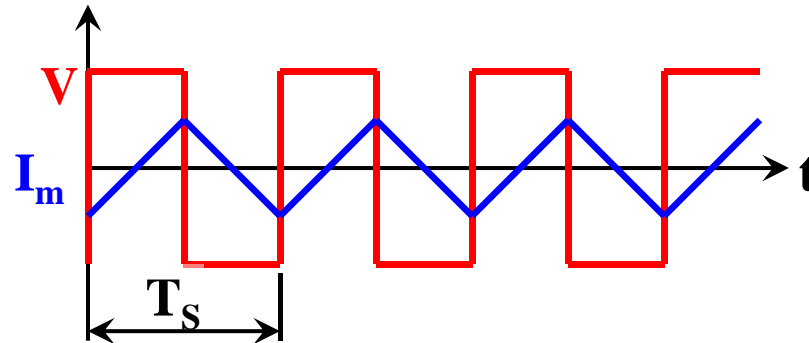
Primary Inductance: 0.133 mH

Secondary Inductance: 8.17 mH

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Primary Magnetising Current Peak



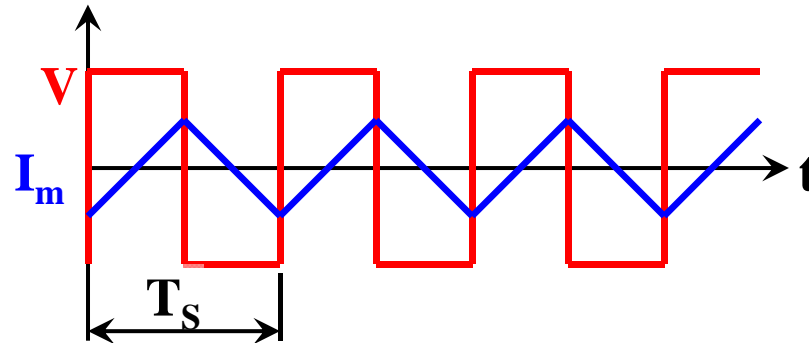
$$I_m(\text{peak}) = \frac{48}{2 * 0.133\text{m}} 10\mu = 1.8\text{A}$$

Magnetising Current Peak << Primary Current

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Stored Energy in the Core



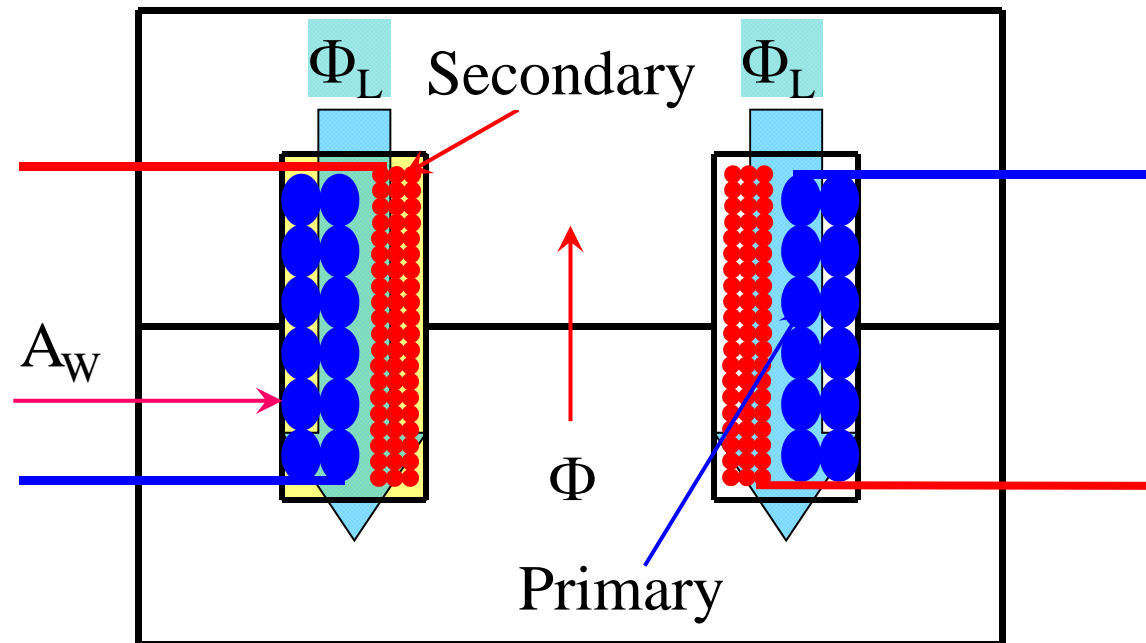
$$E_m = \frac{L_m}{2} I_m^2 = 0.5 * 0.133 \text{ m} * 1.8^2 = 0.22 \text{ mJ}$$

Stored Energy in the Core = 0.22 mJ

Switched Mode Power Conversion

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Leakage Energy in the Window

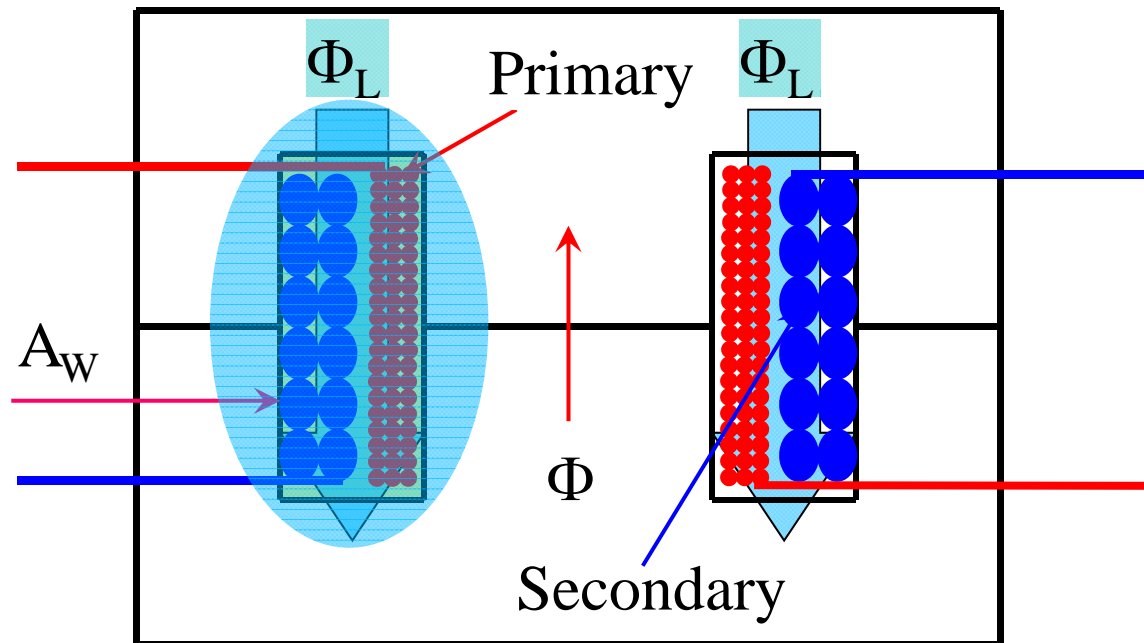


Leakage is Another Non-ideality in the Magnetic Circuit

Switched Mode Power Conversion

Transformers

Leakage Energy in the Window



Leakage is Another Non-ideality in the Magnetic Circuit

Switched Mode Power Conversion

Transformers

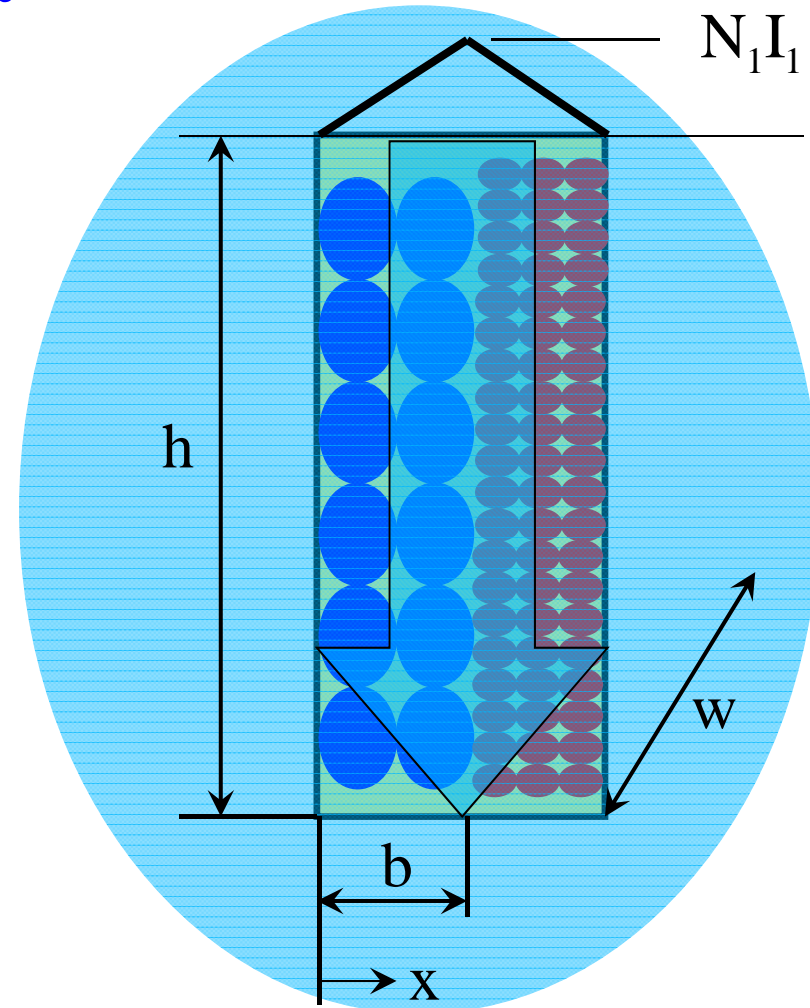
Leakage Energy in the Window

$$H(x) = \frac{N_1 I_1}{h} \frac{x}{b}$$

$$B(x) = \frac{\mu_o N_1 I_1}{h} \frac{x}{b}$$

$$L_\ell = \frac{\mu_o}{I_1^2} \iiint H^2(x) dv$$

$$dv = 2 h w dx$$



Switched Mode Power Conversion

Transformers

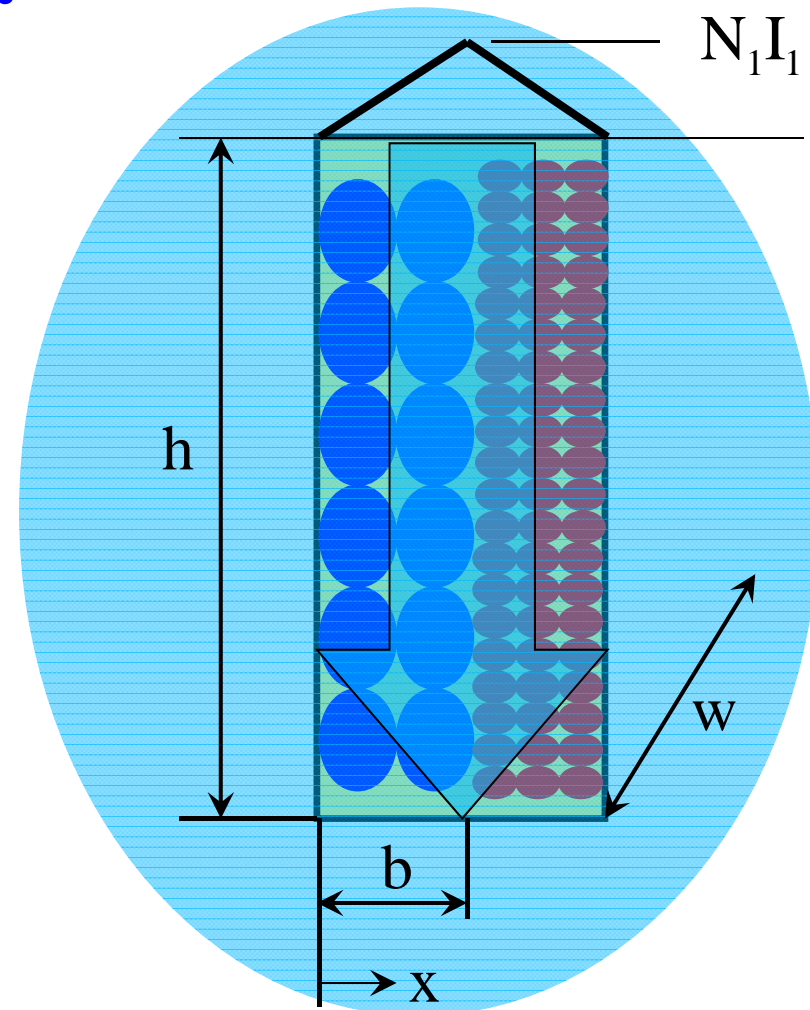
Leakage Energy in the Window

$$L_{\ell} = \frac{\mu_o N_1^2}{h^2} \frac{2}{b^2} h w \int_0^b x^2 dx$$

$$L_{\ell} = \frac{2\mu_o N_1^2 b w}{3 * h}$$

$$0.07 \mu H \ll 133 \mu H$$

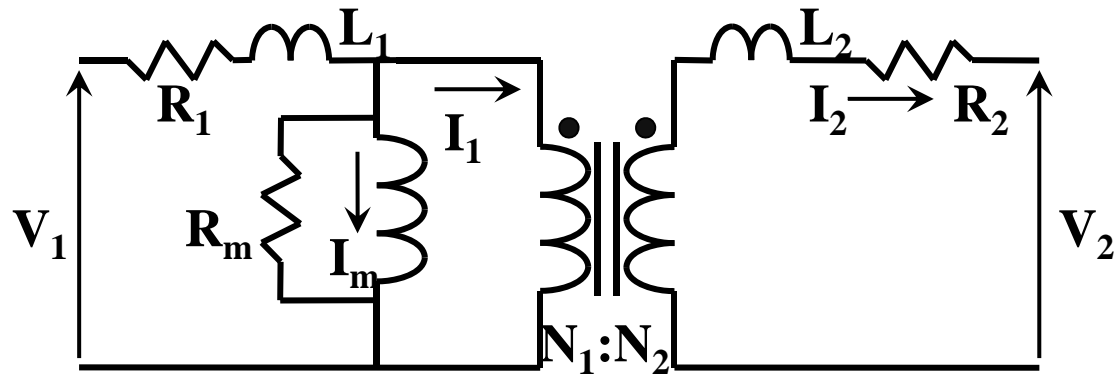
$$L_{pu} = 6.1 \mu H$$



Switched Mode Power Conversion

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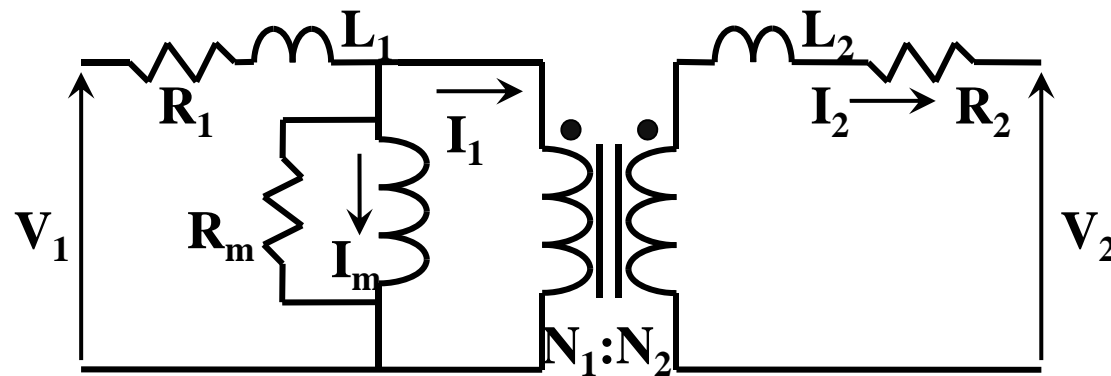
Circuit Model with Dominant Non-idealities



Switched Mode Power Conversion

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Measurement of Circuit Parametes



Open Circuit & Short Circuit Test

Switched Mode Power Conversion

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Devices for Efficient Power Conversion

Switches

Inductors

Transformers

Capacitors

Switched Mode Power Conversion

Capacitors

Devices for Efficient Power Conversion

Switches
Inductors
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