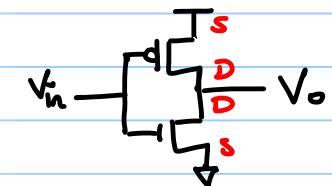
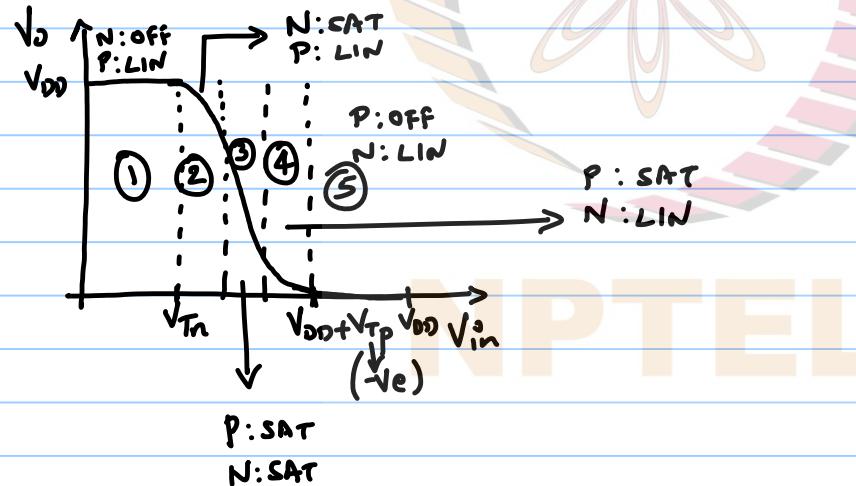


28/08/2019

EE5311  
MODULE-3 : THE INVERTER

VOLTAGE TRANSFER CHARACTERISTICS (VTC)



$$I_{DSn} = -I_{DSp}$$

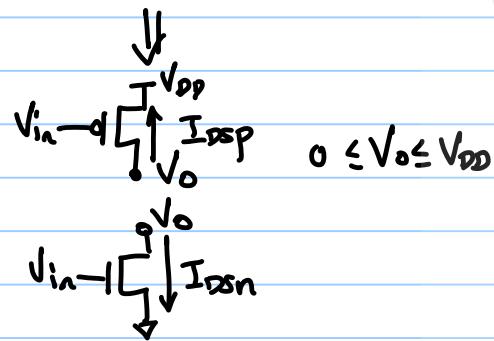
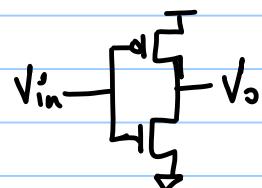
$$V_{GSn} = V_{in}$$

$$V_{DSn} = V_o$$

$$V_{GSp} = V_{in} - V_{DD}$$

$$V_{DSp} = V_o - V_{DD}$$

## LOAD LINE ANALYSIS



$$I_{DSN} = -I_{DOP}$$

$$V_{GSN} = V_{in}$$

$$V_{DSN} = V_o$$

$$V_{ASP} = V_{in} - V_{DD}$$

$$V_{DOP} = V_o - V_{DD}$$

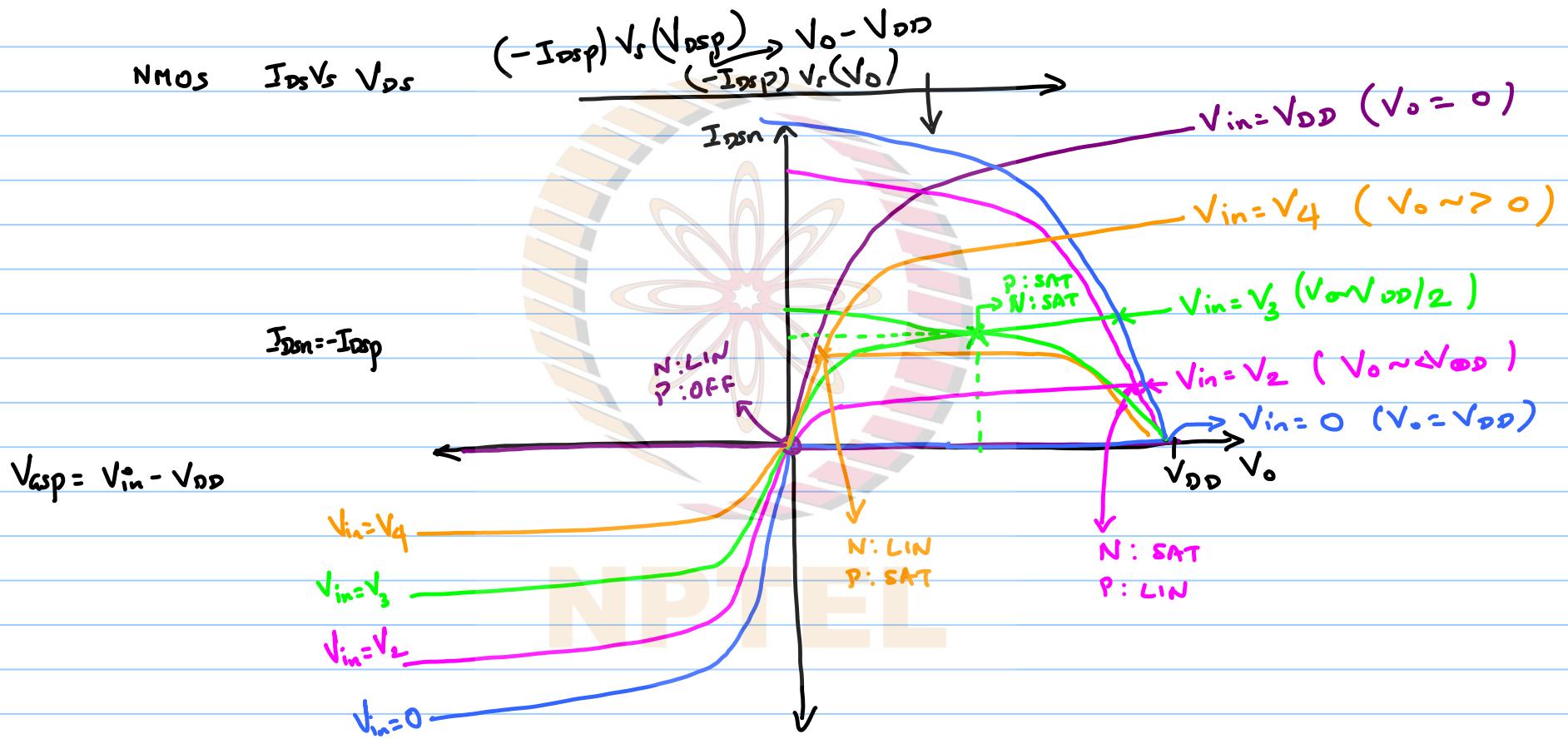
SWEET 'V<sub>o</sub>' WITH V<sub>in</sub> as a param.

$$V_n = V_1, V_2, V_3, V_4, V_5$$

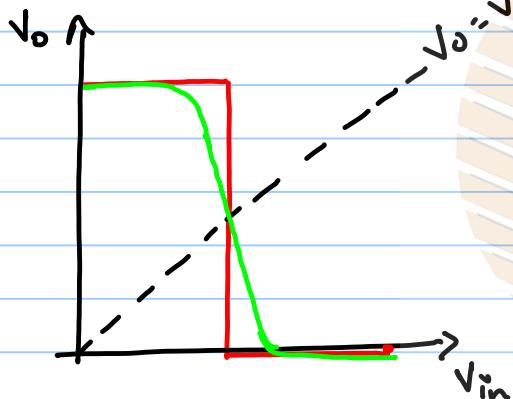
$$\leq V_{in}$$

Bottom  
in  
sat

$$> V_{DD} + V_{TP}$$



### TRIP POINT



Assume :  $\lambda_N \approx \lambda_P$  one in Vel sat region  
 $\lambda_n = \lambda_p = 0$

$$V_{DSN} = V_{in} = V_m$$

$$V_{DNP} = V_o = V_m$$

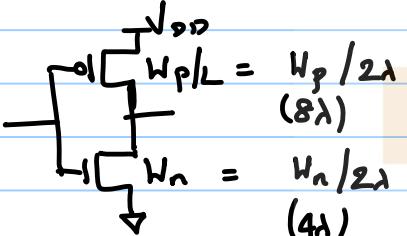
$$V_{CSN} = V_{in} - V_{DD} = V_m - V_{DD}$$

$$V_{CSP} = V_o - V_{DD} = V_m - V_{DD}$$

$$I_{DSN} = k_i \frac{W_n}{L} V_{DSATN} \left( V_m - V_{TN} - \frac{V_{DSATN}}{2} \right)$$

$$I_{DNP} = k_p \frac{W_p}{L} V_{DSATP} \left( V_m - V_{DD} - V_{TP} - \frac{V_{DSATP}}{2} \right)$$

$$(I_{DSN} = -I_{DNP})$$



$$\text{IN } 180 \text{ nm: } 2\lambda = 180 \text{ nm.}$$

$\lambda \rightarrow$  NOT SAME AS CLM ( $\lambda_N, \lambda_P$ )

$$\Rightarrow K_n' \frac{W_n}{L} V_{DSATn} \left( V_M - V_{Tn} - \frac{V_{DSATn}}{2} \right) = - K_p' \frac{W_p}{L} V_{DSATp} \left( V_M - V_{DD} - V_{Tp} - \frac{V_{DSATp}}{2} \right)$$

$$\gamma = \frac{K_p' W_p V_{DSATp}}{K_n' W_n V_{DSATn}} \quad (+ve \text{ no.})$$

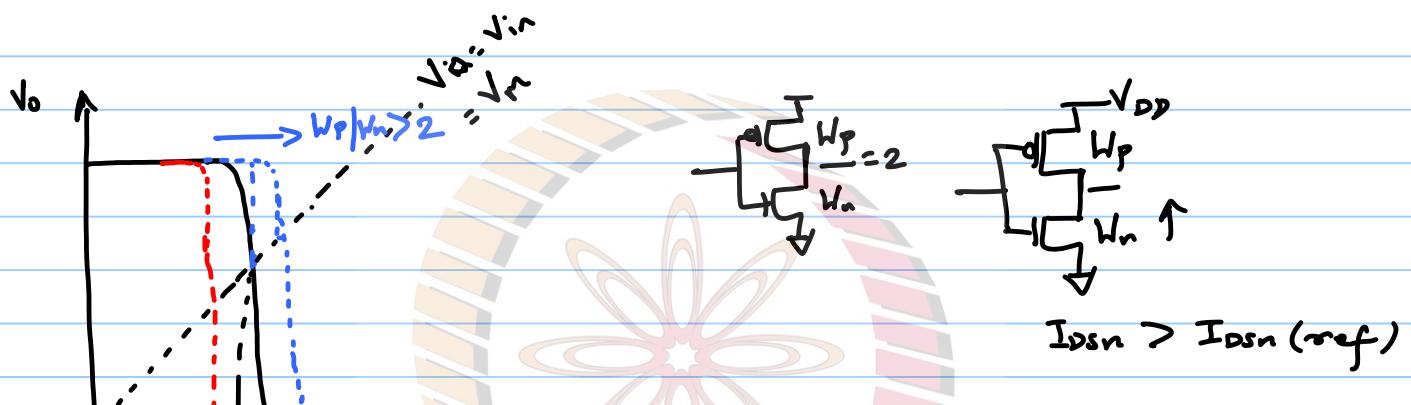
$$\therefore V_M = \frac{\left( V_{Tn} + \frac{V_{DSATn}}{2} \right) + \gamma \left( V_{DD} + V_{Tp} + \frac{V_{DSATp}}{2} \right)}{1 + \gamma}$$

$$V_{DSATn} = -V_{DSATp}, \quad V_{Tn} = -V_{Tp}$$

$$(W_p/W_n) = K_n'/|K_p'| \approx 2$$

$$\Rightarrow \gamma = 1$$

$$\Rightarrow V_M = \frac{V_{DD}}{2}$$



### LONG CHANNEL DEVICES

$$V_{in} = V_o = V_m$$

$$I_{DSN} = -I_{Dsp}$$

$$I_{DSN} = \frac{1}{2} k_n' \frac{W_n}{L} (V_m - V_{Tn})^2$$

$$I_{Dsp} = \frac{1}{2} k_p' \frac{W_p}{L} (V_m - V_{DD} - V_{Tp})^2$$

$$I_{DSn} = -I_{DSp}$$

$$\Rightarrow K_n^i W_n (V_M - V_{Tn})^2 = -K_p^i W_p (V_M - V_{DD} - V_{Tp})^2$$

$$\Rightarrow \gamma = \sqrt{\frac{-K_p^i W_p}{K_n^i W_n}}$$

$$\Rightarrow (V_M - V_{Tn}) = \pm \gamma (V_M - V_{DD} - V_{Tp})$$

$$\Rightarrow V_M (1 + \gamma) = V_{Tn} + \gamma (V_{DD} + V_{Tp})$$

$$\therefore V_M = \frac{V_{Tn} + \gamma (V_{DD} + V_{Tp})}{1 + \gamma}$$