

Indexing and Searching Techniques in Databases



Course Name **Indexing and Searching
Techniques in Databases**

Department of Computer Science and
Engineering

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Module 1: Basics and Background

Lecture 1: Basic Database Queries

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The Lecture Contains:

- General Setting
- Exact match query or Point query
- Extended setting
- Similarity search
- Example of similarity search

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General setting

- Database D of n objects

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General setting

- Database D of n objects
- Each object has k dimensions

$$O_i = \{O_{i,1}, \dots, O_{i,k}\}$$

- No particular database design assumed

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General setting

- Database D of n objects
- Each object has k dimensions

$$O_i = \{O_{i,1}, \dots, O_{i,k}\}$$

- No particular database design assumed
- Query Q is an object with the same k dimensions

$$Q = \{Q_1, \dots, Q_k\}$$

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Exact match query or Point query

- **Point query:** Given D and Q , return all objects $O_i \in D$ such that

$$O_i = Q$$

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Exact match query or Point query

- **Point query:** Given D and Q , return all objects $O_i \in D$ such that

$$O_i = Q$$

- The concept of **equality** (operator =) needs to be precisely defined

For example, $O_i = Q$ iff all the d dimensions individually are the same,

$$\text{i.e. } O_i = Q \Leftrightarrow \forall j = \{1, \dots, k\}, O_{i,j} = Q_j$$

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Exact match query or Point query

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- The concept of **equality** (operator $=$) needs to be precisely defined

For example, $O_i = Q$ iff all the d dimensions individually are the same,

$$\text{i.e. } O_i = Q \Leftrightarrow \forall j \in \{1, \dots, k\}, O_{i,j} = Q_j$$

- Equality can be defined over a subset of the k dimensions as well

$$\text{For example, } O_i = Q \Leftrightarrow O_{i,1} = Q_1$$

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Extended setting

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- Distance function $d(O_i, O_j)$ between two objects

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Extended setting

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- Distance function $d(O_i, O_j)$ between two objects
 - If k dimensions are defined, distance function d can be, for example, Euclidean, Manhattan, etc.
 - Can be over a subset of k dimensions

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 - Can be over a subset of k dimensions
 - Otherwise, d can be a metric distance

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 - Otherwise, d can be a metric distance
 - If d is not a metric distance, then the problem is much harder
- Point query: Given D and Q , return all objects $O_i \in D$ such that $d(O_i, Q) = 0$

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Similarity search

- **Range query:** Given D , Q , d and range r , return all objects $T = \{O_i\}$ such that

$$d(O_i, Q) \leq r$$

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Similarity search

- **Range query:** Given D , Q , d and range r , return all objects $T = \{O_i\}$ such that

$$d(O_i, Q) \leq r$$

- **Nearest neighbour (kNN) query:** Given D , Q , d and number of nearest neighbour k , return k objects $T = \{O_i\}$ such that

$$|T| = k \text{ and for any } O_i \in T \text{ and } O_j \notin T, d(O_i, Q) \leq d(O_j, Q)$$

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Similarity search

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- **Window query:** Given D and ranges Q_j^{low}, Q_j^{high} in each dimension $j = 1 \dots k$, return all objects $T = \{O_i\}$ such that

$$\forall j=1 \dots k, Q_j^{low} \leq O_{ij} \leq Q_j^{high}$$

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Example of similarity search

Object	Dim 1	Dim 2
O_1	3	7
O_2	3	6
O_3	5	8
O_4	9	2
Q	4	5

d is Manhattan distance.

Range search: $r = 2$

kNN search: $k = 2$

Example of similarity search

Object	Dim 1	Dim 2	d(.,Q)
O_1	3	7	3
O_2	3	6	2
O_3	5	8	4
O_4	9	2	8
Q	4	5	-

d is Manhattan distance.

Range search: $r = 2$

kNN search: $k = 2$

Range search answer: $T = \{O_2\}$

kNN search answer: $T = \{O_2, O_1\}$