

Module 10: Filtration

Lecture 36: Principles of filtration, constant pressure and volume filtration

☰ Principles of filtration (continued )

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## Module 10: Filtration

## Lecture 36: Principles of filtration, constant pressure and volume filtration

## Principles of filtration (continued)

Case 1: Constant Pressure-drop Filtration

$$v(t) = \frac{q(t)}{A} = \frac{1}{A} \frac{dV}{dt}, \quad \text{where } V = \text{the volume of filtrate collected and} \\ A = \text{filtering area}$$

$$dm = \text{differential mass of the cake} = \rho_p (1-\epsilon) A dL$$

Substituting,

$$dP = \frac{k_1 \mu v (s_p/v_p)^2 (1-\epsilon)}{\rho_p A \epsilon^3} dm$$

Assuming, incompressible cake (Const  $\rho_p, \mu, \epsilon$ )

$$\Delta p_c \text{ (pressure-drop) through cake} = (p_a - p_1)$$

$$= \frac{k_1 \mu v (s_p/v_p)^2 (1-\epsilon)}{\rho_p A \epsilon} m_c, \text{ where, } m_c = \text{total mass of cake.}$$

 $p_1$  = upstream-pressure of filter-media

$$\text{Define, } R = \text{hydraulic resistance} = \frac{\Delta p_c}{\mu_f V}$$

$$\alpha = \text{specific resistance} = R/(m_c/A)$$

$$\alpha = \left( \frac{\Delta p_c A}{\mu_f v m_c} \right) = \left( \frac{k_1 (\Delta p/v_p)^2 (1-\epsilon)}{\epsilon^3 \rho_p} \right) = \text{property of cake}$$

$$\left. \begin{array}{l} \text{If constant } \Delta p - \text{filtration,} \\ \quad v(t) \downarrow \quad m_c \uparrow \\ \text{If constant } V - \text{filtration,} \\ \quad \Delta p_c \uparrow \quad m_c \uparrow \\ \text{overall } \Delta p = \Delta p_c + \Delta p_m \end{array} \right\} \alpha \text{ remainst constant}$$

↓ Pressure-drop through filter medium

$$\Delta p = \mu_f v \left( \frac{m_c \alpha}{A} \right) \text{ hydraulic resistance of filter medium}$$

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Now 'C' as the mass of the particles deposited in the filter per unit volume of the filtrate,

$$m_c(t) = V(t) \times C$$

It can be shown that

$$C = \frac{C_s}{1 - \left(\frac{m_f}{m_c} - 1\right) \frac{C_s}{\rho_f}} \text{ where, } C_s = \text{slurry density} = \frac{\text{mass of solids}}{\text{volume of liquid fed to filter}}$$

If turns out that  $\frac{m_f}{m_c} = \text{property of cake} (= 2 \text{ for calcium carbonate slurry})$

Replacing  $m_c$  and  $v$  in the expression for  $\Delta p$

$$\frac{1}{q} = \frac{dt}{dV} = \frac{\mu_f}{A \Delta p} \left( \frac{\alpha C V}{A} + R_m \right)$$

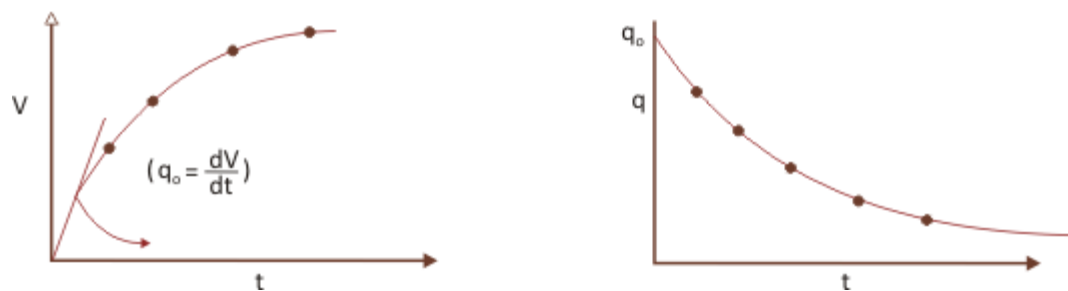
This is the working equation for cake filtration.

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⇒ Case 1: constant-pressure filtration ( $\Delta p = \Delta p_o$ )



(Fig. 36a)

$t = 0, V = 0, \Delta p = \Delta p_o, q = q_o$

$$\frac{1}{q_o} = \left( \frac{dt}{dV} \right)_o = \frac{\mu_f R_m}{A \Delta p_o}$$

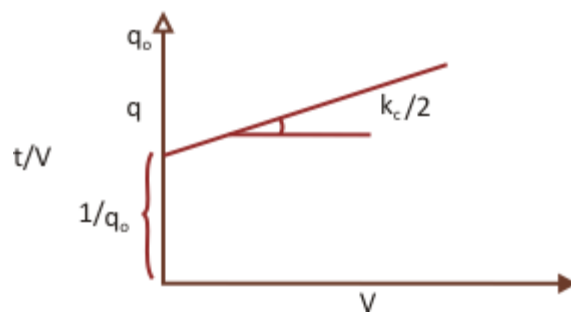
Therefore,  $R_m = \frac{(\Delta p)_o A}{q_o \mu_f}$  (one can calculate  $R_m$  from the initial filtration-data when resistance

due

to cake = 0)

One can also write,

$$\boxed{\frac{1}{q} = \frac{1}{q_o} + K_C V}, \text{ where } K_C = \left( \frac{\mu_f \alpha C}{A^2 \Delta p} \right) = \text{constant (known)}$$



(Fig. 36b)

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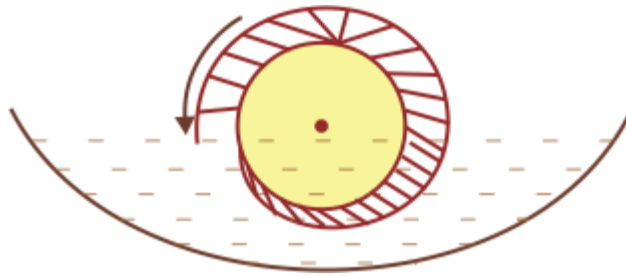
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Or

$$\frac{t}{V} = \frac{1}{q_0} + \frac{K_c}{2} V \quad \text{on integration}$$

The above expression can be integrated to develop an expression for the amount of cake formed over time 't' or the production rate of cake for the rotary- drum filter:



(Fig. 36c)

$$\frac{\dot{m}_c}{A} = \left( \frac{2C \Delta p f \eta}{\alpha \mu} \right)^{1/2}$$

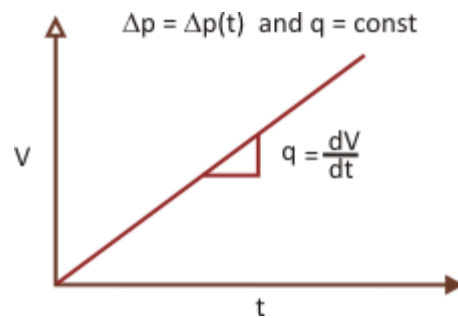
A = Total area of filtration

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## Case 2: Constant Rate Filtration



(Fig. 36d)

$$u = \frac{1}{A} \frac{dV}{dt} = \frac{V}{A t}$$

$$\Delta p = \mu v \left( \frac{m_c \alpha}{A} + R_m \right)$$

Or

$$\Delta p \simeq \frac{\mu_c V^2 \alpha}{t A^2} \quad (\text{neglecting } R_m)$$

$$\frac{\Delta p}{\alpha} = \frac{\mu C}{t} \left( \frac{V}{A} \right)^2 = \mu C t v^2 \quad \text{here, } v \text{ is constant.}$$

$\Delta p$  varies linearly with time.

(Such operation is difficult to run, i.e, keeping volumetric flow rate constant)

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