

Module 3: Physics of Combustion

Lecture 13: Transport properties for gas mixture

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Transport properties for gas mixture

Viscosity of gas mixture

Wassilijewa equation

$$\mu_{mix} = \sum_{i=1}^N \frac{X_i \mu_i}{\sum_{j=1}^N X_j A_{ij}} \quad A_{ij} = \frac{\left[1 + \left(\frac{\mu_i}{\mu_j} \right)^{0.5} \left(\frac{MW_i}{MW_j} \right)^{0.25} \right]}{\left[8 \left(1 + \frac{MW_i}{MW_j} \right) \right]^{0.5}}$$

Mason and Saxena modification

 μ_i is the viscosity of the pure component X_i is the mole fraction of the i^{th} component

Thermal Conductivity of gas mixture

Wassilijewa equation

$$k_{mix} = \sum_{j=1}^N \frac{X_j k_j}{\sum_{j=1}^N X_j A_{ij}} \quad A_{ij} = \frac{\left[1 + \left(\frac{k_i}{k_j} \right)^{0.5} \left(\frac{MW_i}{MW_j} \right)^{0.25} \right]^2}{\left[8 \left(1 + \frac{MW_i}{MW_j} \right) \right]^{0.5}}$$

Mason and Saxena modification

 k_i is the thermal conductivity of the pure component

Diffusion Coefficient of any component in a gas mixture

Wilke equation

$$D_i = \frac{1 - X_i}{\sum_{j=1 \neq i}^N \frac{X_j}{D_{ij}}}$$

$$D_i = 262.8 \times 10^{-9} \sqrt{\frac{T^3 \frac{MW_i + MW_j}{2MW_i MW_j}}{P \sigma_{ij}^2 \Omega_D}}$$

Where,

 σ_{ij} is the collision diameter in \AA P is the pressure (Bar) MW_i is the molecular weight of the components Ω_D is the collision integral

$$\Omega_D = (44.54 \times T_{ij}^{*-4.909} + 1.911 \times T_{ij}^{*1.575})^{0.1}$$

 k_B = Boltzman's constant ε_o = Intermolecular potential

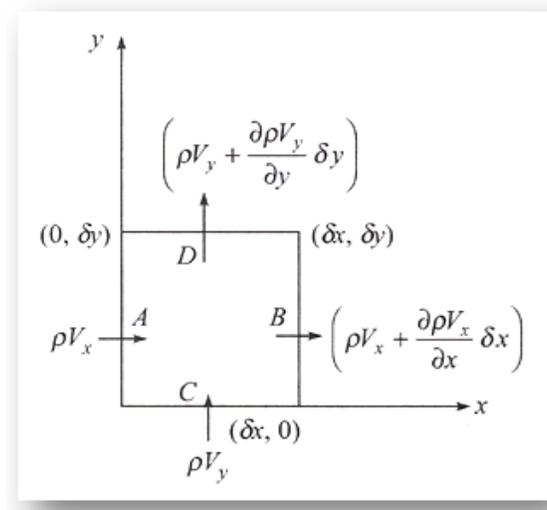
$$T_{ij}^* = \sqrt{T_i^* T_j^*}$$

$$T_i^* = \frac{T}{\varepsilon_o / k_B}$$

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Mass conservation equation

Principle of mass conservation



$$\left\{ \begin{array}{l} \text{Rate of mass accumulation} \\ \text{in fluid element} \end{array} \right\} = \text{----- (1)}$$

$$\left\{ \begin{array}{l} \text{Rate of mass into} \\ \text{fluid element} \end{array} \right\} - \left\{ \begin{array}{l} \text{Rate of mass out of} \\ \text{fluid element} \end{array} \right\}$$

$$\text{Rate of accumulation in fluid element} = \frac{\partial \rho}{\partial t} (\delta x \times \delta y \times 1) \text{----- (2)}$$

$$\text{Rate of mass in fluid element across face A} = \rho V_x (\delta y \times 1) \text{----- (3)}$$

$$\text{Rate of mass leaving fluid element across face B} = \left(\rho V_x + \frac{\partial (\rho V_x)}{\partial x} \delta x \right) \times (\delta y \times 1) \text{----- (4)}$$

$$\text{The net efflux in x-direction} = \frac{\partial (\rho V_x)}{\partial x} \times (\delta x \times \delta y) \text{----- (5)}$$

$$\text{The net efflux in y-direction} = \frac{\partial (\rho V_y)}{\partial y} \times (\delta x \times \delta y) \text{----- (6)}$$

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Substituting (2), (5) and (6) in (1)

$$\frac{\partial \rho}{\partial t} + \frac{\partial(\rho V_x)}{\partial x} + \frac{\partial(\rho V_y)}{\partial y} = 0$$

Differential form of continuity equation

In vector notation,

$$\frac{\partial \rho}{\partial t} + \nabla \cdot \rho \mathbf{V} = 0$$

Where,

∇ is the gradient operator

$\nabla \cdot (\rho \mathbf{V})$ is the divergence of $\rho \mathbf{V}$

For incompressible flow,

$$\frac{\partial V_x}{\partial x} + \frac{\partial V_y}{\partial y} = 0$$

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