




Module 6: Diffusion Flame

Lecture 32: The Temperature Profile

The Lecture Contains:

-  [The Temperature Profile](#)
-  [Droplet Burning Time](#)
-  [Droplet Combustion in Convective Environment](#)

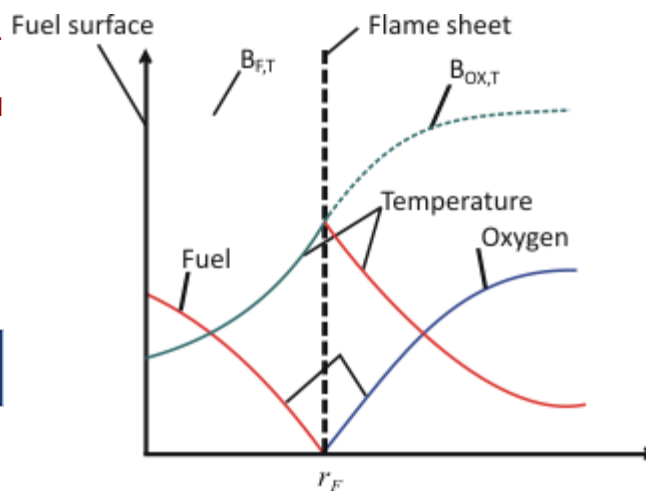
 [Previous](#) [Next](#) 

The Temperature Profile

- No oxygen exists in the inner flame region.
- No fuel exists in the outer region of flame.
- Using the transfer function for fuel and oxidizer,

Temperature profile for the inner region,

$$\frac{\dot{m}_F'' r_s^2}{\rho \alpha} \frac{1}{r} = \ln \left[\frac{C_p(T_\infty - T_s) + \Delta \hat{H}_c f Y_{O_{x,\infty}} + Q_v}{C_p(T - T_s) + Q_v} \right]$$



(Figure 32.1)

Rearranging the above equation,

$$C_p(T - T_s) = [C_p(T_\infty - T_s) + \Delta \hat{H}_c f Y_{O_{x,\infty}} + Q_v] \times \exp[-(\dot{m}_F'' r_s^2)/\rho \alpha r] + \Delta \hat{H}_c - Q_v$$

Temperature profile for the outer region,

$$C_p(T - T_s) = [C_p(T_\infty - T_s) - \Delta \hat{H}_c + Q_v] \times \exp[-(\dot{m}_F'' r_s^2)/\rho \alpha r] + \Delta \hat{H}_c - Q_v$$

◀ Previous Next ▶

Droplet Burning Time

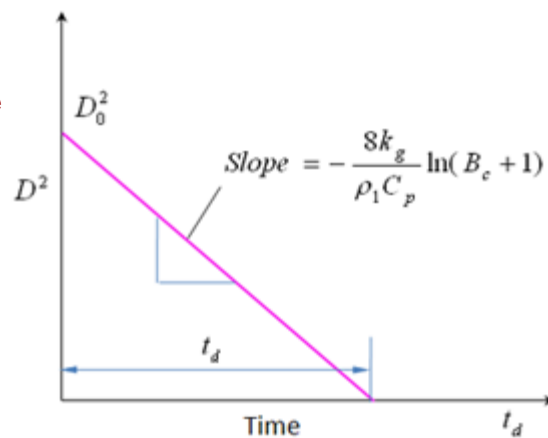
Importance of droplet burning time:

Essential for desining combustion chamber

For complete combustion, residence time > life time of largest droplet in spray.

Factors dictating residence time of droplet:

- Air stream velocity
- Droplet velocity
- Fuel injection angle
- Combustor geometry



(Figure 32.2)

Continuity equation at the surface of the droplet:

$$-\frac{dm_D}{dt} = -\dot{m}_F \quad \text{-----(1)}$$

Droplet mass is evaluated as follows,

$$m_D = \rho_1 V = \rho_1 \pi D^3 / 6 \quad \text{-----(2) Where, D is the droplet diameter at any instant}$$

◀ Previous Next ▶

Droplet Burning Time (Contd.)

Recall,

$$\dot{m}_F'' = \frac{\rho a}{r_g} \ln(B_c + 1)$$

(3)

Using (1) & (2) in (3),

$$D \frac{dD}{dt} = \frac{-4k_g}{\rho_l C_p} \ln(B_c + 1)$$

(4)

Expressing droplet diameter in terms of D^2 ,

$$\frac{dD^2}{dt} = \frac{-8k_g}{\rho_l C_p} \ln(B_c + 1)$$

(5)

Burning constant for typical hydrocarbons

Fuel	k 10 ⁻⁷ m ² /s (Calculated)	k 10 ⁻⁷ m ² /s (Measured)
Ethyl alcohol	9.3	8.1
N-Heptane	14.2	9.7
ISO-Octane	14.4	9.5
Kerosene	9.7	9.6
Benzene	11.2	9.7
Toluene	11.1	6.6

In this expression, D^2 varies linearly with time (See figure 32.3). Slope of the plot is the burning rate constant, K

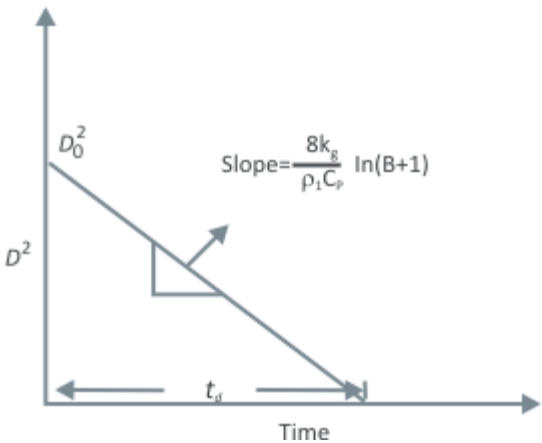
$$K = \frac{8k_g}{\rho_l C_p} \ln(B_c + 1)$$

----- (6)

Integrating (5) with time,

$$D^2(t) = D_0^2 - Kt$$

is D^2 law



(Figure 32.3)

Module 6: Diffusion Flame

Lecture 32: The Temperature Profile

Droplet Combustion in Convective Environment

In practical devices, both free and forced convection will prevail,

Flow past the fuel droplet for $Re > 20$

- Front portion of the droplet – Boundary layer.
- Rear portion – Wake region

In practical devices, forced convection is more predominant

Boundary condition at the droplet surface,

$$\bar{h}_c \Delta T = \rho_s V_s \Delta \hat{H}_V = \frac{\dot{m}_F}{4\pi r_s^2} \Delta \hat{H}_V = \frac{\rho \alpha}{T_s} \ln(1 + B_c) \Delta \hat{H}_V \quad \text{-----}(1)$$

Where,

$$\Delta T \approx \frac{f_{stoil} Y_{O_{2,\infty}} \Delta \hat{H}_C}{C_p} + (T_\infty + T_s) \quad \text{-----}(2)$$

\bar{h}_c - Convective heat transfer coefficient

Combining the above two expressions,

$$\bar{h}_c \left(\frac{f_{stoil} Y_{O_{2,\infty}} \Delta \hat{H}_C + C_p (T_\infty + T_s)}{C_p} \right) = \frac{\rho \alpha}{T_s} \ln(1 + B_c) \Delta \hat{H}_V = \frac{k_g}{C_p T_s} \ln(1 + B_c) \Delta \hat{H}_V \quad \text{-----}(3)$$

◀ Previous Next ▶

Droplet Combustion in Convective Environment

Rearranging the above equation,

$$\frac{\bar{h}_c r_s}{k_g} = \frac{\ln(1 + B_c)}{f_{stoic} Y_{O_2, \infty} \Delta \bar{H}_C + C_p (T_\infty + T_s) / \Delta \bar{H}_V} \quad \text{-----(4)}$$

$$N_{u_{r_s}} = \frac{\ln(1 + B_c)}{B_c} \quad \text{-----(5)}$$

For high Reynolds number,

$$N_{u_{r_s}} = \frac{\ln(1 + B_c)}{B_c} [1 + 0.39 Pr^{0.33} Re_{r_s}^{0.5}] \quad \text{-----(6)}$$

For unit Prandtl number, $Re \gg Pr$,

$$N_{u_{r_s}} = 0.39 Re_{r_s}^{0.5} \frac{\ln(1 + B_c)}{B_c} \quad \text{-----(7)}$$

◀ Previous Next ▶

Droplet Combustion in Convective Environment

$$\frac{\bar{h}_c r_s}{k_g} = \frac{\rho_s V_s r_s}{\mu} \frac{\Delta \hat{H}_v}{[f_{stoic} Y_{O_2, \infty} \Delta \hat{H}_c + C_p (T_\infty + T_s)]} \frac{C_p \mu}{k_g} = \frac{\rho_s V_s r_s Pr}{\mu B_c} \quad \text{-----}(8)$$

Then Eq. (7) becomes,

$$\frac{\rho_s V_s r_s}{\mu} = 0.39 Re_{r_s}^{0.5} \ln(1 + B_c)$$

- The above expression would not provide accurate prediction
- Wake region behind the droplet is not considered here.
- For predicting the experimental data, the above expression is modified as,

$$\frac{\rho_s V_s r_s}{\mu} = 0.39 Re_{r_s}^{0.5} \frac{\ln(1 + B_c)}{B_c^{0.15}} \quad \text{-----}(9)$$

Under convective condition, laminar droplet burning rate follows $D^{3/2}$

◀ Previous Next ▶