

# Unit 9 - Week 7

## Course outline

### How to access the portal?

### Week-0

### Week 1

### Week 2

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### Week 7

● Lecture 25: Energy Transfers: Fluid Simulations using Spectral Method

● Lecture 26: Energy Transfers: Fluid Simulations - Dealiasing

● Lecture 27: Kolmogorov's Theory: Energy Spectrum and Flux

● Lecture 28: Kolmogorov's Theory: Insights and its Verification with Direct Numerical Simulation

● Lecture Slides

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## Assignment 7

The due date for submitting this assignment has passed.  
As per our records you have not submitted this assignment.

**Due on 2019-09-18, 23:59 IST.**

1) In a juice making machine, a fruit-flavour is mixed in 1 kg of water ( $\nu = 10^{-6} \text{ m}^2/\text{s}$ ). The machine consumes 300 W power. What will be the approximate size of the smallest eddies in the flow induced by the machine? **1 point**

- 1 mm  
 0.01 mm  
 10 mm  
 cannot estimate with the given information

No, the answer is incorrect.  
Score: 0

Accepted Answers:  
0.01 mm

2) Approximate values of Kolmogorov time ( $\tau_\eta$ ) and velocity ( $u_\eta$ ) scales for the problem 1 are : **1 point**

- $\tau_\eta = 0.0001 \text{ s}$  and  $u_\eta = 0.1 \text{ m/s}$   
  $\tau_\eta = 0.0001 \text{ s}$  and  $u_\eta = 0.1 \text{ mm/s}$   
  $\tau_\eta = 0.1 \text{ s}$  and  $u_\eta = 0.01 \text{ m/s}$   
  $\tau_\eta = 1 \text{ s}$  and  $u_\eta = 1 \text{ m/s}$

No, the answer is incorrect.  
Score: 0

Accepted Answers:  
 $\tau_\eta = 0.0001 \text{ s}$  and  $u_\eta = 0.1 \text{ m/s}$

3) How many grid points  $N$  (approximately) are required (in all three directions) to perform the Direct Numerical Simulation of a turbulent flow with Reynolds number  $\text{Re} = 2.2 \times 10^5$ ? **1 point**

- $N = 10^5$   
  $N = 10^4$   
  $N = 10^3$   
  $N = 10^2$

No, the answer is incorrect.  
Score: 0

Accepted Answers:  
 $N = 10^4$

4) Choose a property of turbulence which is not due to Kolmogorov's theory of turbulence. **1 point**

- In the inertial range energy spectrum scales  $E(k) \sim k^{-5/3}$   
 Bottleneck effect in the energy spectrum  
 Energy flux is constant in the inertial range  
 Smallest length scale in the turbulence is  $\eta \sim (\nu^3/\epsilon)^{1/4}$

No, the answer is incorrect.  
Score: 0

Accepted Answers:  
Bottleneck effect in the energy spectrum

5) For a fully-developed turbulent flow which is forced at large scales, the energy dissipation rate ( $\epsilon$ ) can be estimated as: **1 point**

- $\epsilon \sim U^3/L$   
  $\epsilon \sim U^2/L$   
  $\epsilon \sim \nu(U^2/L^2)$   
 None of these

No, the answer is incorrect.  
Score: 0

Accepted Answers:  
 $\epsilon \sim U^3/L$

6) In a fully-developed three-dimensional homogeneous isotropic turbulence, energy transfer is: **1 point**

- from large to small scales (forward cascade) and non-local  
 from small to large scales (inverse cascade) and local  
 can be both forward and inverse cascade, and local and non-local  
 always forward and local

No, the answer is incorrect.  
Score: 0

Accepted Answers:  
always forward and local

7) Consider a fully-developed turbulent flow with  $\nu = 0$  (Euler turbulence). Which one of the following statements is **incorrect** for this flow? **1 point**

- It is an equilibrium phenomenon.  
 Energy of every mode are equal, that leads to energy spectrum scaling  $E(k) \sim k^2$ .  
 Energy is transferred from large to small scales.  
 No energy transfer takes place among various modes.

No, the answer is incorrect.  
Score: 0

Accepted Answers:  
Energy is transferred from large to small scales.

8) Pao's conjecture  $E(k)/\Pi(k) = K_{K0}\epsilon^{-1/3}k^{-5/3}$  is useful: **1 point**

- in developing a model for the energy spectrum in both inertial and the dissipation range  
 in explaining the bottleneck effect in the energy spectrum  
 in explaining the local nature of energy transfer in a fully developed 3D homogeneous isotropic turbulence  
 None of these

No, the answer is incorrect.  
Score: 0

Accepted Answers:  
in developing a model for the energy spectrum in both inertial and the dissipation range

9) Consider a decaying turbulence with a constraint:  $u^2 \ell^3 = \text{constant}$ , where  $\ell$  is the integral length scale. Also note that for a fully developed turbulence at very high Reynolds number  $\epsilon \sim (u^3/\ell)$ . What will be the decay law for this type of turbulence? **1 point**

- $u^2 \sim t^{-6/5}$   
  $u^2 \sim t^{-10/7}$   
  $u^2 \sim t^{-1}$   
 decay law for turbulence depends on viscosity

No, the answer is incorrect.  
Score: 0

Accepted Answers:  
 $u^2 \sim t^{-6/5}$

10) Which one of the following statements is correct for a laminar flow (low Reynolds number flows)? **1 point**

- Energy spectrum scaling is very close to exponential nature  $E(k) \sim \exp(-bk)$ , where  $b$  is a constant.  
 Energy spectrum scales  $E(k) \sim k^2$ .  
 Energy flux is constant.  
 Energy flux is zero.

No, the answer is incorrect.  
Score: 0

Accepted Answers:  
Energy spectrum scaling is very close to exponential nature  $E(k) \sim \exp(-bk)$ , where  $b$  is a constant.