

## Unit 5 - Branch cuts of the square root function

### Course outline

How to access the portal?

Week0

Introduction to complex variables

Important theorems in complex variables

Branch cuts of the square root function

• Infinite and finite branch cuts.

• Finite Branch Cut.

• Infinite branch cut example

• Contour integration: rectangular contour

• Finite square root branch cut.

• Example on finite branch cut.

○ Quiz : Week3 Assessment

○ Week3 Assessment Solution

The inverse Laplace transform

## Week3 Assessment

The due date for submitting this assignment has passed.  
As per our records you have not submitted this assignment.

**Due on 2019-08-21, 23:59 IST.**

1) Compute the integral  $\int_c z dz$  along the straight line from the origin to  $(2 + 2i)$

1 point

- $4i$   
  $4$   
  $2\sqrt{2}$   
  $2\sqrt{2}i$

No, the answer is incorrect.

Score: 0

Accepted Answers:  
 $4i$

2) Given the complex function  $f(z) = \frac{\cos z}{z^5}$ . The singular point 'a' and the order of the pole at  $z = a$  are

1 point

- $a = \pi/2, 4$   
  $a = \pi/2, 5$   
  $a = 0, 4$   
  $a = 0, 5$

No, the answer is incorrect.

Score: 0

Accepted Answers:  
 $a = 0, 5$

3) Given the complex function  $f(z) = \frac{\cos z}{z^5}$ . Find the residue at the only singular point.

1 point

- $\frac{4}{4!}$   
  $\frac{5}{5!}$   
  $\frac{1}{5!}$   
  $\frac{2}{5!}$

No, the answer is incorrect.

Score: 0

Accepted Answers:  
 $\frac{5}{5!}$

4) Consider  $J = \oint_C \frac{\cos z}{z^2} dz$ , where C is the contour defined by a circle  $|z - 1| = 0.5$ . The value of J equals to

1 point

- $0$   
  $\frac{\pi i}{4}$   
  $\frac{\pi i}{12}$   
  $\frac{\pi i}{6}$

No, the answer is incorrect.

Score: 0

Accepted Answers:  
 $0$

5) Consider  $J = \oint_C \frac{\cos z}{z^2} dz$ , where C is the contour defined by a circle  $|z - 0.4| = 0.5$ . The value of J equals to

1 point

- $0$   
  $\frac{\pi i}{4}$   
  $\frac{\pi i}{12}$   
  $\frac{\pi i}{6}$

No, the answer is incorrect.

Score: 0

Accepted Answers:  
 $\frac{\pi i}{12}$

6) Consider  $J = \oint_C \frac{\cos z}{z^2} dz$ , where C is the contour defined by a circle  $|z - 0.4| = 10$ . The value of J equals to

1 point

- $0$   
  $\frac{\pi i}{8}$   
  $\frac{\pi i}{6}$   
  $\frac{\pi i}{12}$

No, the answer is incorrect.

Score: 0

Accepted Answers:  
 $\frac{\pi i}{12}$

7) Compute the integral  $J = \int_a^b z dz + \int_c^d z dz$ , where  $a = 0, b = 2, c = 2 + 2i$  are the points on the complex plane.

1 point

- $4i$   
  $4$   
  $2\sqrt{2}$   
  $2\sqrt{2}i$

No, the answer is incorrect.

Score: 0

Accepted Answers:  
 $4i$

8) Consider  $f(z) = \frac{5z^2+17}{z^3-2z^2+4z-8}$ . The singular points for  $f(z)$  are

1 point

- $2, 2i$   
  $2, -2i$   
  $2i, -2i$   
 All of the above

No, the answer is incorrect.

Score: 0

Accepted Answers:  
All of the above

9) Consider  $J = \oint_C \frac{5z^2+17}{z^3-2z^2+4z-8} dz$ , where C is the contour defined by a circle  $|z - 5| = 1$ . The value of J equals to

1 point

- $2\pi i$   
  $\pi i$   
  $0$   
 None of the above

No, the answer is incorrect.

Score: 0

Accepted Answers:  
 $0$

10) Consider  $J = \oint_C \frac{5z^2+17}{z^3-2z^2+4z-8} dz$ , where C is the contour defined by a circle  $|z - 3| = 3$ . The value of J equals to

1 point

- $0$   
  $\frac{37\pi i}{4}$   
  $\frac{37\pi i}{3}$   
  $\frac{37\pi i}{2}$

No, the answer is incorrect.

Score: 0

Accepted Answers:  
 $\frac{37\pi i}{4}$

11) Consider  $J = \oint_C \frac{5z^2+17}{z^3-2z^2+4z-8} dz$ , where C is the contour defined by a circle  $|z - (1 + i)| = 3$ . The value of J equals to

1 point

- $\frac{(7i-3)\pi}{8}$   
  $\frac{(7i+3)\pi}{8}$   
  $0$   
  $10\pi i$

No, the answer is incorrect.

Score: 0

Accepted Answers:  
 $\frac{(7i+3)\pi}{8}$

12) Consider  $J = \oint_C \frac{5z^2+17}{z^3-2z^2+4z-8} dz$ , where C is the contour defined by a circle  $|z| = 3$ . The value of J equals to

1 point

- $\frac{37\pi i}{4}$   
  $2\pi i$   
  $0$   
  $10\pi i$

No, the answer is incorrect.

Score: 0

Accepted Answers:  
 $10\pi i$

13) Compute the integral  $\int_c z dz$  along a contour C, that is composed of a straight line from the origin to  $2\sqrt{2}i$ . And then along a circular arc from  $2\sqrt{2}i$  to  $(2 + 2i)$  with centre at the origin.

1 point

- $i$   
  $0$   
  $2i$   
  $4i$   
  $0$

No, the answer is incorrect.

Score: 0

Accepted Answers:  
 $4i$

14) The value of  $J = \int_0^{\infty} \frac{z}{z^2+8} dz$  equals to

1 point

- $\frac{\pi}{3\sqrt{3}}$   
  $\frac{\pi}{2\sqrt{2}}$   
  $\frac{\pi\sqrt{3}}{3}$   
  $\frac{\pi\sqrt{2}}{3}$

No, the answer is incorrect.

Score: 0

Accepted Answers:  
 $\frac{\pi}{3\sqrt{3}}$

15) The value of  $J = \int_0^{\infty} \frac{1}{\sqrt{5x}(1+25x^2)} dx$  equals to

1 point

- $\frac{\pi}{\sqrt{3}}$   
  $\frac{\pi}{\sqrt{10}}$   
  $\pi\sqrt{\frac{3}{2}}$   
  $\frac{\pi}{5\sqrt{2}}$

No, the answer is incorrect.

Score: 0

Accepted Answers:  
 $\frac{\pi}{5\sqrt{2}}$

16) The value of  $J = \int_0^{\infty} \frac{1}{\sqrt{x}(1+x^2)} dx$  equals to

1 point

- $\frac{\pi}{\sqrt{3}}$   
  $\frac{\pi}{3\sqrt{3}}$   
  $\frac{3\pi}{\sqrt{3}}$   
  $\pi$

No, the answer is incorrect.

Score: 0

Accepted Answers:  
 $\frac{\pi}{\sqrt{3}}$

17) The value of  $J = \int_0^{\infty} \frac{1}{(1+x^2)} dx$  equals to

1 point

- $\pi$   
  $\frac{\pi}{3\sqrt{3}}$   
  $\frac{2\pi}{3\sqrt{3}}$   
  $\frac{3\pi}{\sqrt{3}}$

No, the answer is incorrect.

Score: 0

Accepted Answers:  
 $\frac{2\pi}{3\sqrt{3}}$

18) Compute the integral  $J = \oint_C z dz$  along a closed contour C, that is composed of three straight lines : 0 to 2, 2 to  $(2 + 2i)$  and  $(2 + 2i)$  to 0 in the anti - clockwise direction.

1 point

- $4i$   
  $0$   
  $2\sqrt{2}$   
  $2\sqrt{2}i$

No, the answer is incorrect.

Score: 0

Accepted Answers:  
 $0$