

Unit 3 - Week 1

Course outline
How to access the portal
Week 1
<input checked="" type="radio"/> Subscript Notation – Part 1 of 2 <input type="radio"/> Subscript Notation – Part 2 of 2 <input type="radio"/> Coordinate Rotation <input type="radio"/> Week 1 Feedback : Transport Phenomena In Materials <input type="radio"/> Quiz : Assignment 1
Week 2
Week 3
Week 4
Week 5
Week 6
Week 7
week 8
Week 9
Week 10
Week 11
Week 12
DOWNLOAD VIDEOS

Assignment 1

The due date for submitting this assignment has passed. **Due on 2019-08-14, 23:59 IST.**
 As per our records you have not submitted this assignment.

Lecture -1 (Subscript notations -I)

1) The number of free subscripts in A_{ijkl} is/are **1 point**

- 1
 2
 3
 4

No, the answer is incorrect. Score: 0

Accepted Answers: 4

2) The maximum number of components possible for A_{ijkl} are **1 point**

- 27
 81
 9
 4

No, the answer is incorrect. Score: 0

Accepted Answers: 81

3) $\frac{\partial p}{\partial x_i}$ can be written in subscript notation as, **1 point**

- p_i
 p_{ii}
 $p_{,i}$
 $p_{,i}$
 $p_{,i}$

No, the answer is incorrect. Score: 0

Accepted Answers: $p_{,i}$

4) The tensorial order of the quantity $S_{ijkl}\delta_{ij}$ is **1 point**

- 1
 2
 3
 6

No, the answer is incorrect. Score: 0

Accepted Answers: 2

5) Consider $A = \begin{bmatrix} 1 & 2 & 0 \\ 0 & 3 & 0 \\ 0 & 0 & 4 \end{bmatrix}$ and $B = \begin{bmatrix} 5 & 6 & 0 \\ 0 & 7 & 0 \\ 0 & 0 & 8 \end{bmatrix}$, if $C_{ij} = A_{ik}B_{kj}$, find C_{21}

No, the answer is incorrect. Score: 0

Accepted Answers: (Type: Numeric) 58

6) Consider $A = \begin{bmatrix} 1 & 2 & 0 \\ 0 & 3 & 0 \\ 0 & 0 & 4 \end{bmatrix}$ and $B = \begin{bmatrix} 5 & 6 & 0 \\ 0 & 7 & 0 \\ 0 & 0 & 8 \end{bmatrix}$, if $C_{ij} = A_{ik}B_{kj}$, find C_{21} **1 point**

No, the answer is incorrect. Score: 0

Accepted Answers: (Type: Numeric) 0

7) if $\vec{a} = \hat{i} + 2\hat{j} + 3\hat{k}$ and $\vec{b} = 4\hat{i} + 5\hat{j} + 6\hat{k}$ are 2 vectors, then the dyadic product $\vec{a} \otimes \vec{b}$ is given by **1 point**

- $\begin{bmatrix} 4 & 5 & 6 \\ 8 & 10 & 12 \\ 12 & 15 & 18 \end{bmatrix}$
 $\begin{bmatrix} 4 & 8 & 12 \\ 5 & 10 & 15 \\ 6 & 12 & 18 \end{bmatrix}$
 32
 $[-3 \ 6 \ -3]$

No, the answer is incorrect. Score: 0

Accepted Answers: $\begin{bmatrix} 4 & 5 & 6 \\ 8 & 10 & 12 \\ 12 & 15 & 18 \end{bmatrix}$

8) if $a_i = [1 \ 2 \ 3]$ and $b_j = [4 \ 5 \ 6]$, then the inner product given by $a_i b_i = \dots$ **1 point**

No, the answer is incorrect. Score: 0

Accepted Answers: (Type: Numeric) 32

Lecture -2 (Subscript notation II):

9) Levi-Civita symbol is written as ϵ_{ijk} . Which of the following expressions are true. **1 point**

- i. $\epsilon_{123} + \epsilon_{231} + \epsilon_{312} = 3$
 ii. $\epsilon_{321} + \epsilon_{312} + \epsilon_{322} = 0$
 iii. $\epsilon_{111} + \epsilon_{222} + \epsilon_{333} = 3$

- i,ii
 ii,iii
 i,iii
 i

No, the answer is incorrect. Score: 0

Accepted Answers: i,ii

10) Using subscript notations, find $(\vec{j} \times \vec{g}) \cdot (\vec{j} \times \vec{g}) =$ **1 point**

- $(\vec{j} \cdot \vec{g})\vec{g} - (\vec{g} \cdot \vec{j})\vec{j}$
 $(\vec{j} \times \vec{j})\vec{g} - (\vec{g} \times \vec{g})\vec{j}$
 $(\vec{j} \cdot \vec{g})^2 - |\vec{j}|^2|\vec{g}|^2$
 $|\vec{j}|^2|\vec{g}|^2 - (\vec{j} \cdot \vec{g})^2$

No, the answer is incorrect. Score: 0

Accepted Answers: $|\vec{j}|^2|\vec{g}|^2 - (\vec{j} \cdot \vec{g})^2$

11) if $\vec{B} = \mu \vec{H}$ and $\vec{B} = \vec{\nabla} \times \vec{A}$, then find $\vec{\nabla} \times \vec{H}$ in terms of \vec{A} . **1 point**

- $\frac{1}{\mu} (\nabla \cdot \vec{A}) - \nabla^2 \vec{A}$
 $\frac{1}{\mu} (\nabla^2 \vec{A} - \nabla(\nabla \cdot \vec{A}))$
 0
 $\frac{1}{\mu} ((\nabla \cdot \vec{A})\vec{A} - \nabla(\nabla \cdot \vec{A}))$

No, the answer is incorrect. Score: 0

Accepted Answers: $\frac{1}{\mu} (\nabla(\nabla \cdot \vec{A}) - \nabla^2 \vec{A})$

12) if ψ and φ are scalar fields, then $\nabla^2(\varphi\psi)$ is given by **1 point**

- $\varphi(\nabla^2\psi) + \psi(\nabla^2\varphi)$
 $\varphi(\nabla^2\psi) + \psi(\nabla^2\varphi) + 2\nabla\psi \cdot \nabla\varphi$
 $\varphi(\nabla^2\psi) + \psi(\nabla^2\varphi)$
 $\varphi(\nabla^2\psi) + \psi(\nabla^2\varphi) + 2\vec{\nabla}$

No, the answer is incorrect. Score: 0

Accepted Answers: $\varphi(\nabla^2\psi) + \psi(\nabla^2\varphi) + 2\nabla\psi \cdot \nabla\varphi$

13) The relationship between Levi-civita symbol and Kronecker delta is given by $\epsilon_{ijk}\epsilon_{lmn} = \begin{vmatrix} \delta_{il} & \delta_{im} & \delta_{in} \\ \delta_{jl} & \delta_{jm} & \delta_{jn} \\ \delta_{kl} & \delta_{km} & \delta_{kn} \end{vmatrix}$ The expression for $\epsilon_{ijk}\epsilon_{imn}$ is given as **1 point**

(Hint : Substitute l=i)

- $\delta_{jm}\delta_{kn} - \delta_{km}\delta_{jn}$
 $\delta_{kn}\delta_{jn} - \delta_{jm}\delta_{kn}$
 $2\delta_{kn}$
 $\delta_{jm}\delta_{in} - \delta_{im}\delta_{jn}$

No, the answer is incorrect. Score: 0

Accepted Answers: $\delta_{jm}\delta_{kn} - \delta_{km}\delta_{jn}$

14) The relationship between Levi-civita symbol and Kronecker delta is given by $\epsilon_{ijk}\epsilon_{lmn} = \begin{vmatrix} \delta_{il} & \delta_{im} & \delta_{in} \\ \delta_{jl} & \delta_{jm} & \delta_{jn} \\ \delta_{kl} & \delta_{km} & \delta_{kn} \end{vmatrix}$ Find the value of $\epsilon_{ijk}\epsilon_{ijn}$ **1 point**

- $\delta_{jk}\delta_{in} - 9$
 $2\delta_{kn}$
 $-2\delta_{kn}$
 $2\delta_{kn} - \delta_{jk}\delta_{in}$

No, the answer is incorrect. Score: 0

Accepted Answers: $2\delta_{kn}$

Lecture -3 (Co-ordinate transformations)

15) A tensor $[D] = \begin{bmatrix} 6 & 6 & 4 \\ 7 & 2 & 8 \\ 1 & 3 & 3 \end{bmatrix}$ where it is arbitrarily rotated about an axis to get $[D'] = \begin{bmatrix} 3 & 1 & 9 \\ q & p & 6 \\ 8 & 7 & 2 \end{bmatrix}$. Find the value of p. **1 point**

- 3
 5
 6
 7

No, the answer is incorrect. Score: 0

Accepted Answers: 6

16) If a vector is rotated 'θ' degrees counter-clockwise direction around z-axis, then the relation between 'θ' and transformation matrix 'T' is given by **1 point**

- $\theta = \cos^{-1} \left(\frac{1}{2} \text{Trace}(T) \right)$
 $\theta = \cos^{-1} \left(\frac{\text{Trace}(T)-1}{2} \right)$
 $\theta = \frac{1}{2} \cos^{-1} (\text{Trace}(T))$
 $\theta = \frac{1}{2} \cos^{-1} (\text{Trace}(T) - 1)$

No, the answer is incorrect. Score: 0

Accepted Answers: $\theta = \cos^{-1} \left(\frac{\text{Trace}(T)-1}{2} \right)$

17) If a vector is rotated '90' degrees counter-clockwise direction around z-axis, the T_{11} of transformation matrix will be **1 point**

- 0
 1
 90
 0.707

No, the answer is incorrect. Score: 0

Accepted Answers: 0

18) If a vector $\vec{a} = \hat{i} + \hat{j} + \hat{k}$ is rotated 45° counter-clockwise direction around z-axis, the resultant vector obtained is **1 point**

- $\sqrt{2}\hat{j} + \hat{k}$
 $\sqrt{2}\hat{i} + \hat{k}$
 $\hat{j} + \sqrt{2}\hat{k}$
 $\sqrt{2}\hat{i} + \hat{j}$

No, the answer is incorrect. Score: 0

Accepted Answers: $\sqrt{2}\hat{j} + \hat{k}$

19) If 'T' is the transformation matrix under rotation, which of the following statements are true. **1 point**

- i. $\text{Det}(T)=1$
 ii. $\text{Inverse}(T)=\text{Transpose}(T)$
 iii. $\text{Trace}(T)$ is an invariant

- i,ii
 i,iii
 iii
 i,ii,iii

No, the answer is incorrect. Score: 0

Accepted Answers: i,ii,iii

20) Match the following. **1 point**

- | | |
|---------------------------------------------|-------------------------------------------------------|
| A. Right handed-co-ordinate system | 1. δ_{mn} |
| B. Invariant under rotation | 2. Vector |
| C. Changes according to $a_i = T_{ij}a_j$ | 3. Scalar |
| D. Product of transformation $T_{im}T_{ji}$ | 4. $\hat{x}_1 \cdot (\hat{x}_2 \times \hat{x}_3) = 1$ |

- A-1, B-3, C-2, D-4
 A-4, B-3, C-2, D-1
 A-1, B-2, C-3, D-4
 A-4, B-3, C-4, D-2

No, the answer is incorrect. Score: 0

Accepted Answers: A-4, B-3, C-2, D-1