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Courses » Computational Fluid Dynamics

Announcements

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Unit 10 - Week 9

Course outline

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- Lecture 41 : "Conjugate gradient method "
- Lecture 42 : "Convection diffusion equation "
- Lecture 43 : "Central difference scheme applied to convection-diffusion equation "
- Lecture 44 : "Upwind scheme "
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Assignment Solution

Live Session - Sep 13,2018

Week 9 Assignment 9

The due date for submitting this assignment has passed.
As per our records you have not submitted this assignment.

Due on 2018-10-03, 23:59 IST

1) Consider the following statement regarding the gradient search based method. 1 point

- (i) r_0 and r_1 are orthogonal to each other.
- (ii) r_0 is "A" orthogonal to r_1
- (iii) p_0 and p_1 are orthogonal to each other.
- (iv) p_0 is "A" orthogonal to p_1

Choose the correct statement(s)

- (a) only (i) is correct
- (b) only (iii) is correct
- (c) (i) and (iv) are correct
- (d) (ii) and (iii) are correct.

- a
- b
- c
- d

No, the answer is incorrect.

Score: 0

Accepted Answers:

c

2) One has applied conjugate gradient method for solving $Ax=b$. The iteration equation is written as 1 point

$$x^n = x^{n-1} + \alpha_{n-1} p_{n-1}$$

where r_{n-1} is the residual at (n-1) th iteration and is given by $r_{n-1} = b - Ax^{n-1}$. Choose the correct expression for α_{n-1} and p_{n-1}

- (a) $\alpha_{n-1} = \frac{r_{n-1}^T r_{n-1}}{r_{n-1}^T A r_{n-1}}$, $p_{n-1} = r_{n-1} - \frac{p_{n-2}^T A r_{n-1}}{p_{n-2}^T A p_{n-2}} p_{n-2}$
- (b) $\alpha_{n-1} = \frac{p_{n-1}^T r_{n-1}}{p_{n-1}^T A p_{n-1}}$, $p_{n-1} = r_{n-1} - \frac{p_{n-2}^T A r_{n-1}}{p_{n-2}^T A p_{n-2}} p_{n-2}$
- (c) $\alpha_{n-1} = \frac{p_{n-1}^T r_{n-1}}{p_{n-1}^T A p_{n-1}}$, $p_{n-1} = r_{n-1} - \frac{p_{n-2}^T r_{n-1}}{r_{n-2}^T A r_{n-2}} p_{n-2}$
- (d) $\alpha_{n-1} = \frac{p_{n-1}^T p_{n-1}}{r_{n-1}^T A r_{n-1}}$, $p_{n-1} = r_{n-1} - \frac{r_{n-2}^T r_{n-1}}{p_{n-2}^T A p_{n-2}} p_{n-2}$

- a
- b
- c
- d

No, the answer is incorrect.

Score: 0

Accepted Answers:

b

3)

1 point

Consider the solution of $\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} = \begin{bmatrix} 2 \\ 2 \end{bmatrix}$ by using gradient search method.

Which of the following is correct?

- (a) Steepest descent method can be applied for the problem, while conjugate gradient method can not be applied.
- (b) Conjugate gradient method can be applied for the problem, while steepest descent method can not be applied.
- (c) Both the methods can be applied although steepest descent method requires more number of steps than conjugate gradient method.
- (d) Both the methods can be applied and the solution can be obtained by identical steps in both steepest descent and conjugate gradient method.

- a
- b
- c
- d

No, the answer is incorrect.

Score: 0

Accepted Answers:

d

4)

1 point

In general, the Peclet number corresponding to energy transfer, momentum transfer and mass transfer are respectively given by

- (a) Pr, Re and Sc
- (b) Pr, Re and Re \times Sc
- (c) Re/Pr, Re and Re/Sc
- (d) Re \times Pr, Re and Re \times Sc

where Pr is Prandtl number, Re is Reynolds number and Sc is Schmidt number.

- a
- b
- c
- d

No, the answer is incorrect.

Score: 0

Accepted Answers:

d

5)

1 point

The central difference scheme will not work accurately

- (a) if the cell based Peclet number is less than or equal to 2
- (b) if the coefficients of the discretized equation satisfy the Scarborough criterion
- (c) in the limit of very weak diffusion
- (d) in the limit of very weak advection

- a

- b
- c
- d

No, the answer is incorrect.

Score: 0

Accepted Answers:

c

6)

A property ϕ is transported by means of convection and diffusion through the one dimensional domain sketched in Figure 1a which is divided into 5 equal control volumes

as shown in Figure 1b. The governing differential equation is $\frac{d}{dx}(\rho u \phi) = \frac{d}{dx} \left(\Gamma \frac{d\phi}{dx} \right)$

The boundary conditions are $\phi_A=1$ at $x=0$ and $\phi_B=0$ at $x=L$. Other parameter include $u=1$ m/s, $L=2$ m, $\rho=1$ kg/m³ and $\Gamma=0.5$ kg/ms. If the finite volume based discretized equation with the central difference scheme for convective and diffusive terms is of the form $a_P \phi_P = a_W \phi_W + a_E \phi_E + S_u$ and the domain is discretized into five equal control volumes then the solution obtained will

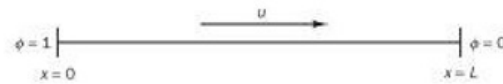


Figure 1a

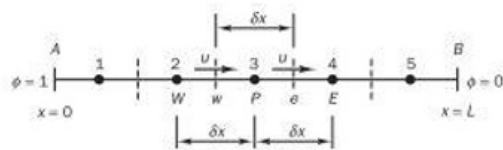


Figure 1b

- (a) Satisfy conservativeness and boundedness
- (b) Satisfy conservativeness, boundedness and Transportiveness
- (c) Satisfy conservativeness, but will be unbounded and non-transportive
- (d) Satisfy boundedness but will not be conservative

- a
- b
- c
- d

No, the answer is incorrect.

Score: 0

Accepted Answers:

c

7)

1 point

Consider the governing differential equation $\frac{d}{dx}(\rho u \phi) = \frac{d}{dx} \left(\Gamma \frac{d\phi}{dx} \right)$ which is discretized using the central difference scheme into the form $a_P \phi_P = a_W \phi_W + a_E \phi_E$ with $a_E = D_e - \frac{F_e}{2}$, $a_W = D_w - \frac{F_w}{2}$ and $a_P = a_E + a_W$. Given that $F_e = F_w = 100$, $\phi_E = 100$ and $\phi_W = 0$. If $\Gamma = 10 \text{ kg/ms}$ then the minimum number of control volumes into which the domain of length 1m should be divided in order to achieve a bounded solution is

- (a) 4
- (b) 5
- (c) 10
- (d) 20

- a
- b
- c
- d

No, the answer is incorrect.

Score: 0

Accepted Answers:

b

8)

1 point



A property ϕ is transported by means of convection and diffusion through the one-dimensional domain sketched in the figure 2a which is divided into 5 equal control volumes as shown in Figure 2b. The governing differential equation is $\frac{d}{dx}(\rho u \phi) = \frac{d}{dx}\left(\Gamma \frac{d\phi}{dx}\right)$. The boundary conditions are $\phi_A=1$ at $x=0$ and $\phi_B=0$ at $x=L$. Other

parameter include $u=5$ m/s, $L=2$ m, $\rho=1$ kg/m³ and $\Gamma=0.5$ kg/ms. If the finite volume based discretized equation with the upwind difference scheme for convective and diffusive terms is of the form $a_P \phi_P = a_W \phi_W + a_E \phi_E + S_u$ then the relation between ϕ_4 and ϕ_5 is

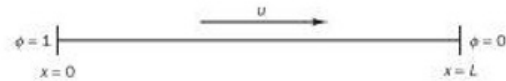


Figure 2a

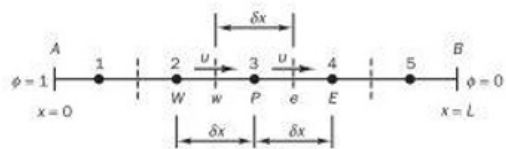


Figure 2b

- (a) $\phi_5 = 6.25\phi_4$
 (b) $\phi_5 = 8.75\phi_4$
 (c) $\phi_5 = 0.7143\phi_4$
 (d) $\phi_5 = \phi_4/0.7143$

- a
 b
 c
 d

No, the answer is incorrect.

Score: 0

Accepted Answers:

c

9)

1 point

The temperature variation in condenser tube is given by $\dot{m}C \frac{dT}{dx} = \frac{UA}{L}(T_0 - T)$, where \dot{m} is mass flow rate, C is the specific heat, T is the temperature of cooling water, T_0 is the constant temperature of the condensing steam, U is the overall heat transfer coefficient, A is the total heat transfer area. It is given that $\frac{AU}{\dot{m}C} = 2$. Define a non-dimensional

temperature $\theta = \frac{T - T_{in}}{T_0 - T_{in}}$, $y = \frac{x}{L}$ with $y = 0$ at $\theta = 0$. The exact profile of temperature expressed as

(a) $\theta = 1 - e^{-2y}$

(b) $\theta = 1 - e^{-y}$

(c) $\theta = 1 + e^{-2y}$

(d) $\theta = 1 + e^{-y}$

- a
 b
 c
 d

No, the answer is incorrect.

Score: 0

Accepted Answers:

a

10)

1 point

The temperature variation in condenser tube is given by $\dot{m}C \frac{dT}{dx} = \frac{UA}{L}(T_0 - T)$, where \dot{m} is the mass flow rate, C is the specific heat, T is the temperature of cooling water, T_0 is the constant temperature of the condensing steam, U is the overall heat transfer coefficient, L is the length of the condenser tube and A is the total heat transfer area. It is given that $\frac{AU}{\dot{m}C} = 2$. Define a non-dimensional temperature $\theta = \frac{T - T_{in}}{T_0 - T_{in}}$, $y = \frac{x}{L}$. The

boundary conditions are at $x=0$, $T=T_{in}$. If the domain is divided into 5 grid points with $\Delta x = 0.25 L$, then what is the value of θ at the 5th grid point using upwind scheme?

(a) 0.8025

(b) 0.9265

(c) 0.9864

(d) 0.62

- a
 b
 c
 d

No, the answer is incorrect.

Score: 0

Accepted Answers:

a

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End

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