

## Course outline

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#### Week 1

- Lecture 1 : Introduction to CFD
- Lecture 2 : Classification of partial differential equations
- Lecture 3 : Examples of partial differential equations
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Assignment Solution

Live Session - Sep 13,2018

# Week 1 Assignment 1

The due date for submitting this assignment has passed. As per our records you have not submitted this assignment.



1) In the context of a second order PDE for a 2D problem, a characteristic is defined as (i) a line across which the first order derivatives **1** point are discontinuous (ii) a surface across which the first order derivatives are discontinuous (iii) a line across which the second order derivatives are continuous (iv) a line across which the second order derivatives are discontinuous (iv) a line across which the second order derivatives are discontinuous (iv) a line across which the second order derivatives are discontinuous (iv) a line across which the second order derivatives are discontinuous (iv) a line across which the second order derivatives are discontinuous (iv) a line across which the second order derivatives are discontinuous (iv) a line across which the second order derivatives are discontinuous (iv) a line across which the second order derivatives are discontinuous (iv) a line across which the second order derivatives are discontinuous (iv) a line across which the second order derivatives are discontinuous (iv) a line across which the second order derivatives are discontinuous (iv) a line across which the second order derivatives are discontinuous (iv) a line across which the second order derivatives are discontinuous (iv) a line across which the second order derivatives are discontinuous (iv) a line across which the second order derivatives are discontinuous (iv) a line across which the second order derivatives are discontinuous (iv) a line across which the second order derivatives are discontinuous (iv) a line across which the second order derivatives are discontinuous (iv) a line across which the second order derivatives are discontinuous (iv) a line across which the second order derivatives are discontinuous (iv) a line across (iv) a l

- (a) (i), (ii) and (iii)
- (b) (ii) only
- (c) (ii) and (iv)
- (d) (i) and (iv)

No, the answer is incorrect.

Score: 0

Accepted Answers:

(a) (i), (ii) and (iii)

2) The general form of the conservation equation is

1 point

where r is the density, f is the transport variable, G is the diffusion coefficient and S is the source term per unit volume.

(a) 
$$\frac{\partial}{\partial t}(\phi) + \nabla . (\vec{V}\phi) = \nabla . (\Gamma \nabla \phi) + S$$
  
(b)  $\frac{\partial}{\partial t}(\rho \phi) + \nabla . (\rho \vec{V}\phi) = \nabla . (\Gamma \nabla \phi) + S$   
(c)  $\frac{\partial}{\partial t}(\rho) + \nabla . (\rho \vec{V}) = \nabla . (\Gamma \nabla \phi) + S$ 

No, the answer is incorrect.

Score: 0

Accepted Answers:

(b) 
$$\frac{\partial}{\partial t} (\rho \phi) + \nabla (\rho \vec{V} \phi) = \nabla (\Gamma \nabla \phi) + S$$

3) Consider the following statements (i) CFD modelling is cheaper than experiments (ii) CFD modelling can handle any degree of complexity (iii) Multiple solutions can never exist in numerical modelling (iv) CFD deals with a mathematical description and not with the reality Out of these the following are the answers which of them are correct

- (a) (i) only
- (b) (i) and (iv)
- (c) (i), (ii) and (iv)
- (d) (ii) and (iii)

### No, the answer is incorrect.

### Score: 0

Accepted Answers:

(c) (i), (ii) and (iv)

4) Choose the correct statement regarding the nature of the partial differential equations

- (a) If the equation has no real characteristics, the equation is elliptic
- (b) If the equation has no real characteristics, the equation is hyperbolic
- $\hfill \bigcirc$  (c) If the equation has no real characteristics, the equation is parabolic
- (d) If the equation has one real characteristics, the equation is elliptic

No, the answer is incorrect.

Score: 0

(a) If the equation has no real characteristics, the equation is elliptic

5)

Accepted Answers:

1 point

1 point

A two-dimensional small-disturbance velocity potential equation for compr

as  $(1-M_{\infty}^2)\frac{\partial^2 \phi}{\partial x^2} + \frac{\partial^2 \phi}{\partial y^2} = 0$ , where  $M_{\infty}$  is the Mach number of flow.

 $(M_{\infty} < 1)$ , the equation is

No Sc Ac (c) 6)

	T I
(a) linear	
(b) parabolic	
(c) elliptic	
<ul> <li>(d) hyperbolic</li> </ul>	
o, the answer is incorrect. core: 0	in
ccepted Answers: ) elliptic	<b>8</b> <sup>+</sup>
	1 point

Consider one dimensional unsteady state wave propagation giv

$$c^{2} \frac{\partial^{2} T}{\partial x^{2}} = \frac{\partial^{2} T}{\partial t^{2}}, \text{ where } c > 0. \text{ The type of the equation is}$$

$$(a) \text{ linear}$$

$$(b) \text{ parabolic}$$

$$(c) \text{ elliptic}$$

$$(d) \text{ hyperbolic}$$
No, the answer is incorrect.
Score: 0
Accepted Answers:
$$(d) \text{ hyperbolic}$$
7)
1 point

Consider the following systems of partial differential equ  $\frac{\partial \phi}{\partial v} = \theta$ , where  $\phi$  and  $\theta$  are the two dependent variables. The equation

OV (a) elliptic (b) hyperbolic (c) linear (d) parabolic No, the answer is incorrect. Score: 0 Accepted Answers: (d) parabolic

Consider a general form of the energy conservation equation as:

$$\frac{\partial}{\partial t} \left( \rho C_p T \right) + \nabla \left( \rho \vec{V} C_p T \right) = \nabla \left( k \nabla T \right) + S.$$

In a physical problem, one is interested to obtain the transient tempe (T as a function of x and t) in a uniform flow field  $(u = U_{\infty} = c_0)$  diffusivity  $(k/\rho C_p)$  of the medium is negligibly small (can be tak analysis). There is a uniform rate of volumetric heat generation (S) and in the physical space the temperature varies only along the x direct properties of the medium can be taken as invariants. Then the nature c differential equation is

1 point

6

<ul> <li>(a) parabolic</li> <li>(b) hyperbolic</li> <li>(c) elliptic</li> </ul>	
<ul> <li>(d) linear</li> <li>No, the answer is incorrect.</li> <li>Score: 0</li> <li>Accepted Answers:</li> <li>(b) hyperbolic</li> </ul>	f
<sup>9)</sup> Consider the following equation $\alpha \frac{\partial^2 \phi}{\partial x^2} = \frac{\partial \phi}{\partial t}$ . The equation is	1 point
<ul> <li>(a) linear</li> <li>(b) parabolic</li> <li>(c) elliptic</li> <li>(d) hyperbolic</li> </ul>	<mark>in</mark> 8⁺
No, the answer is incorrect. Score: 0 Accepted Answers: (b) parabolic	
10) Consider the governing differential equation in	1 point the
$\sum_{i} \sum_{j} A_{ij} \frac{\partial^2 \phi}{\partial x_i \partial y_j} + B = 0.$ The equation is hyperbolic if	
<ul> <li>(a) any one of the eigen values of A is zero</li> <li>(b) none of the eigen values of A is zero and all the eigen values are of same sign</li> <li>(c) none of the eigen values of A is zero and all but one eigen value is of opposite sign</li> <li>(d) none of the eigen values of A is zero and may be of any sign</li> </ul>	
No, the answer is incorrect. Score: 0 Accepted Answers: (c) none of the eigen values of A is zero and all but one eigen value is of opposite sign	
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