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## Unit 4 - Outer measure

### Course outline

[How does an NPTEL online course work?](#)

[Sigma algebras, Measures and Integration](#)

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### Outer measure

- [Consequences of MCT, Fatou's lemma and DCT \(unit? unit=30&lesson=31\)](#)
- [Rectangles in  \$\mathbb{R}^n\$  and some properties \(unit? unit=30&lesson=32\)](#)
- [Outer measure on  \$\mathbb{R}^n\$  \(unit? unit=30&lesson=33\)](#)
- [Properties of outer measure](#)

## Week 3 Assessment

The due date for submitting this assignment has passed. **Due on 2020-02-19, 23:59 IST.**  
As per our records you have not submitted this assignment.

1) Let  $F$  be a countable subset of  $\mathbb{R}^n$  then  $m_*(F)$  equals

1 point

- 0  
  $\infty$   
 Any positive number

No, the answer is incorrect.  
Score: 0

Accepted Answers:  
0

2) Which of the following are correct?

1 point

- Any countable set is measurable  
 Any open set is measurable  
 The set  $\{x \in \mathbb{R} : |e^x \sin x| > 1\}$  is measurable

No, the answer is incorrect.  
Score: 0

Accepted Answers:  
*Any countable set is measurable*  
*Any open set is measurable*  
*The set  $\{x \in \mathbb{R} : |e^x \sin x| > 1\}$  is measurable*

3) Which of the following sets are Borel sets?

1 point

on  $\mathbb{R}^n$  (unit?  
unit=30&lesson=34)

- Lebesgue measurable sets and Lebesgue measure on  $\mathbb{R}^n$  (unit?  
unit=30&lesson=35)

- Quiz : Week 3 Assessment (assessment? name=95)

Lebesgue measure and its properties

Lebesgue measure and positive Borel measures on locally compact spaces

Lebesgue measure and invariance properties

$L^p$  spaces and completeness

Product spaces and Fubini's theorem

Applications of Fubini's theorem and complex measures

Complex measures and Radon-Nikodym theorem

Radon-Nikodym theorem and applications

Riesz representation theorem and Lebesgue differentiation theorem

The subset of  $[0, 1]$  whose decimal expansions starts with 2

Subsets of  $\mathbb{R}$  whose complements are countable

No, the answer is incorrect.

Score: 0

Accepted Answers:

*The subset of  $[0, 1]$  whose decimal expansions starts with 2*

*Subsets of  $\mathbb{R}$  whose complements are countable*

4) The outer measure of the set  $\{0\} \times [-1, 1] \subset \mathbb{R}^2$  is

1 point

 0

 1

 2

No, the answer is incorrect.

Score: 0

Accepted Answers:

0

5) Let  $E \subset \mathbb{R}^n$  be an unbounded set.

1 point

Outer measure of  $E$  is infinity

Outer measure of  $E$  is positive, but need not be infinity always

There are unbounded sets whose outer measure is zero

No, the answer is incorrect.

Score: 0

Accepted Answers:

*There are unbounded sets whose outer measure is zero*

6) Let  $E \subset \mathbb{R}^n$  be such that  $m_*(E) = 0$ . Let  $O_k$  be the open set  $O_k = \{y \in \mathbb{R}^n : d(y, E) < \frac{1}{k}\}$  where  $d(y, E) = \inf_{x \in E} |x - y|$ .

1 point

$m_*(O_k) = \infty$  always

$m_*(O_k)$  is finite always

$m_*(O_k)$  is positive always

No, the answer is incorrect.

Score: 0

Accepted Answers:

*$m_*(O_k)$  is positive always*

7) Let  $E \subset \mathbb{R}^n$  be such that  $m_*(E) = 0$  and Let  $O_k$  be the open set  $O_k = \{y \in \mathbb{R}^n : d(y, E) < \frac{1}{k}\}$  where  $d(y, E) = \inf_{x \in E} |x - y|$ . Then the statement  $m_*(O_k) \rightarrow 0$  is

1 point

 True always

True if  $E$  is closed

True if  $E$  is bounded

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True if  $E$  is compact

No, the answer is incorrect.

Score: 0

Accepted Answers:

*True if  $E$  is compact*

8) Let  $E \subset \mathbb{R}^n$  and  $x \in \mathbb{R}^n$ . Define  $E + x = \{y + x : y \in E\}$ . Suppose  $m_*(E) = 0$ . **1 point**  
Which of the following are correct?

$$m_*(E + x) = 0.$$

$E + x$  is measurable

$E + x$  need not be measurable

No, the answer is incorrect.

Score: 0

Accepted Answers:

$$m_*(E + x) = 0.$$

*$E + x$  is measurable*

9) Let  $A_n = \{n\} \times [-n, n] \subset \mathbb{R}^2$ . If  $A = \bigcup_{n=1}^{\infty} A_n$ , then **1 point**

$$m_*(A) = 0$$

$$m_*(A) = \infty$$

$$0 < m_*(A) < \infty$$

No, the answer is incorrect.

Score: 0

Accepted Answers:

$$m_*(A) = 0$$

10) Let  $A = [0, 1]$ . Which of the following are correct? **1 point**

$$m_*(A) = \inf\{m_*(O) : A \subset O, O \text{ open}\}$$

$$m_*(A) = \sup\{m_*(K) : K \subset A, K \text{ compact}\}$$

No, the answer is incorrect.

Score: 0

Accepted Answers:

$$m_*(A) = \inf\{m_*(O) : A \subset O, O \text{ open}\}$$

$$m_*(A) = \sup\{m_*(K) : K \subset A, K \text{ compact}\}$$

