

# Unit 5 - Week 4

## Course outline

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## Assignment 4

The due date for submitting this assignment has passed.  
As per our records you have not submitted this assignment.

**Due on 2019-08-28, 23:59 IST.**

1) Consider the lattice  $D_{12} = \{1, 2, 3, 4, 6, 12\}$  ordered by divisibility. Then which of the following subsets of  $D_{12}$  is/are sublattice(s) of  $D_{12}$ ? 1 point

(i)  $S = \{1, 2, 3, 4\}$ , (ii)  $T = \{1, 3, 4, 12\}$

- only  $S$   
 only  $T$   
 both  $S$  and  $T$   
 neither  $S$  nor  $T$

No, the answer is incorrect.

Score: 0

Accepted Answers:  
only  $T$

2) Consider the subset  $S = \{2, 3, 6\}$  of the poset  $(\{1, 2, 3, 4, 5, 6\}, |)$ , (where  $x|y$  means  $x$  divides  $y$ ). Then the upper bound and lower bounds of  $S$  are, respectively, 1 point

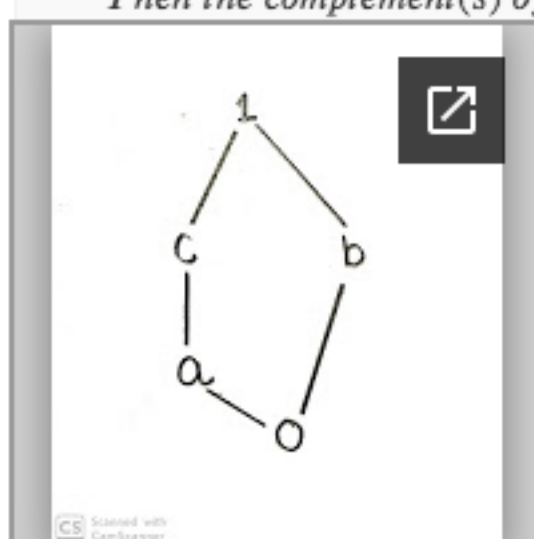
- 6, 2  
 6, 1  
 6, 3  
 6 and 1, 2

No, the answer is incorrect.

Score: 0

Accepted Answers:  
6, 1

3) Consider the lattice as shown below. Then the complement(s) of the element  $b$  is/are : 1 point



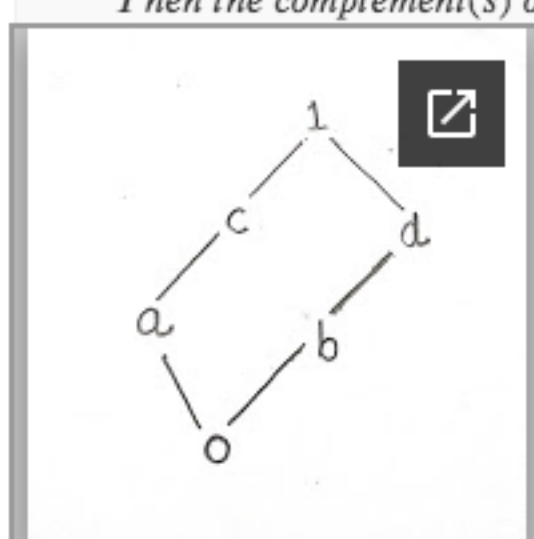
- a  
 c  
 a and c  
 b

No, the answer is incorrect.

Score: 0

Accepted Answers:  
a and c

4) Consider the lattice as shown below. Then the complement(s) of the element  $a$  is/are : 1 point



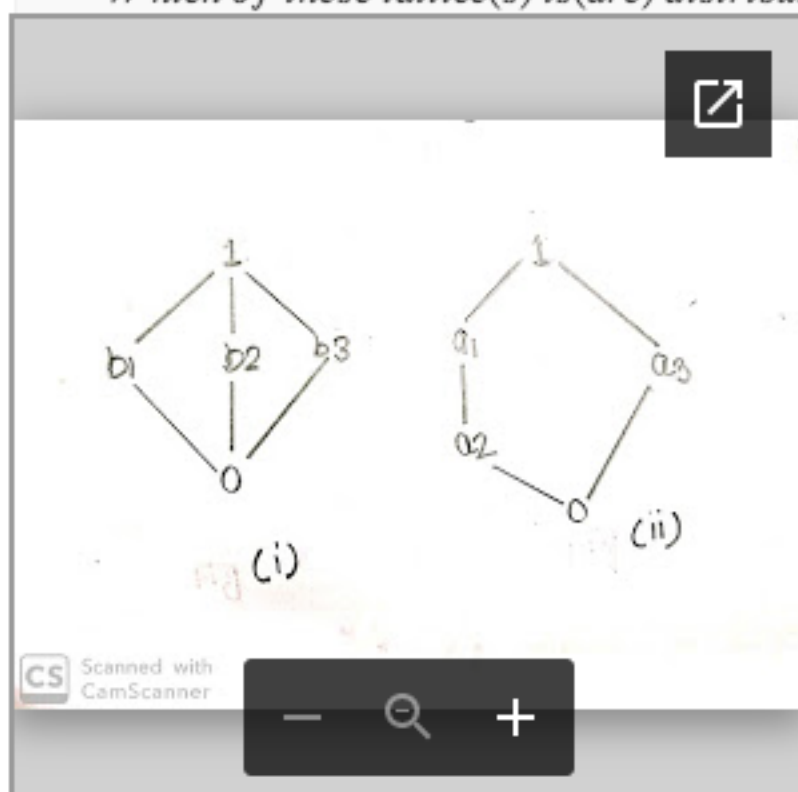
- b  
 b and d  
 d  
 b, c and d

No, the answer is incorrect.

Score: 0

Accepted Answers:  
b and d

5) Consider the lattices as shown below. Which of these lattice(s) is/are distributive? 1 point



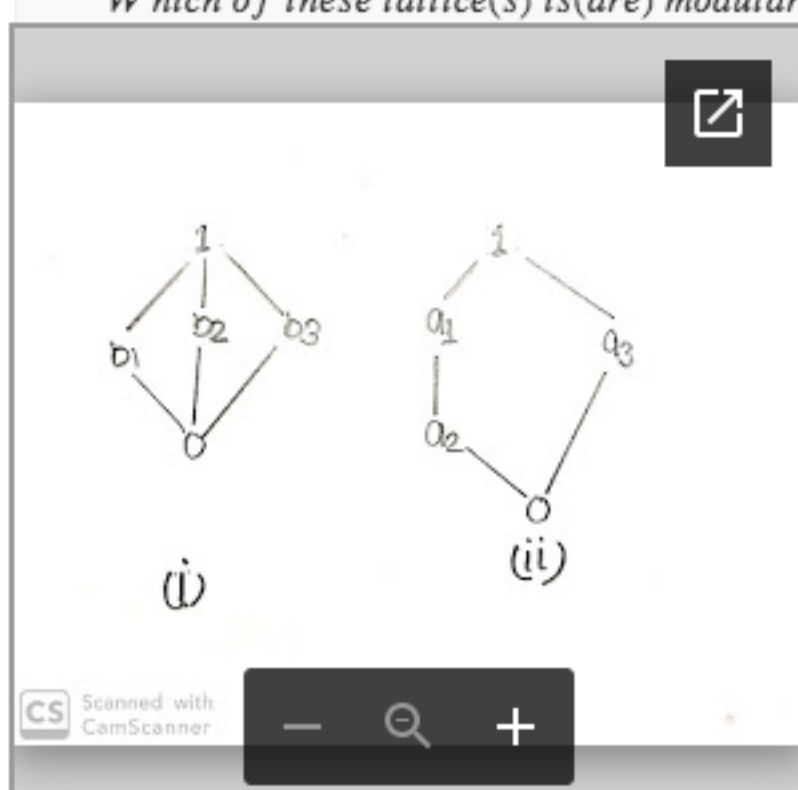
- (i)  
 (ii)  
 both (i) and (ii)  
 neither (i) nor (ii)

No, the answer is incorrect.

Score: 0

Accepted Answers:  
neither (i) nor (ii)

6) Consider the lattices as shown in the figures below. Which of these lattice(s) is/are modular? 1 point



- (i)  
 (ii)  
 both (i) and (ii)  
 neither (i) nor (ii)

No, the answer is incorrect.

Score: 0

Accepted Answers:  
(i)

7)  $A = \{1, 5, 7, 35\}$  be the set of positive integers and the operations  $+$ ,  $*$  and  $'$  be defined on  $A$  as follows : 1 point

$$a + b = \text{lcm}(a, b)$$

$$a * b = \text{gcd}(a, b)$$

$$a' = \frac{35}{a}$$

Then the zero element and the unit elements of the Boolean algebra  $(A, +, *, ')$  are, respectively, given by

- 0, 1  
 1, 35  
 0, 35  
 1, 0

No, the answer is incorrect.

Score: 0

Accepted Answers:  
1, 35

8) Let  $a = 1101110111$  and  $b = 1100110110$  in  $B_{10}$ . Then  $a + b$ ,  $a * b$  and  $a'$  are, respectively, given by 1 point

- 1100110110, 1101110111, 0010001000  
 0010001000, 1101110111, 1100110110  
 1101110111, 1100110110, 0010001000  
 1101110111, 0010001000, 1100110110

No, the answer is incorrect.

Score: 0

Accepted Answers:  
1101110111, 1100110110, 0010001000

9) Consider the Boolean algebra  $D_{30} = \{1, 2, 3, 5, 6, 10, 15, 30\}$ , the divisors of 30, with the operations  $+$ ,  $*$  and  $'$  defined as  $a + b = \text{l.c.m.}(a, b)$ ,  $a * b = \text{g.c.d.}(a, b)$  and  $a' = \frac{30}{a}$ . Then the values of  $x = (30 * 15) + 6'$ ,  $y = (3 + 6) * (10 * 15)'$  and  $z = 30 * (5 + 10)'$  are, respectively, given by 1 point

- 15, 6, 30  
 5, 6, 15  
 5, 6, 30  
 15, 6, 15

No, the answer is incorrect.

Score: 0

Accepted Answers:  
15, 6, 15

10) The dual of the Boolean equation  $ab(b + b'c) + a'c$  is 1 point

- $[(a + b) + b(b' + c)](a' + c)$   
  $[(a + b) + b(b' + c)] + (a' + c)$   
  $[(a + b)b + (b' + c)](a' + c)$   
  $[(a + b)b + (b' + c)] + (a' + c)$

No, the answer is incorrect.

Score: 0

Accepted Answers:  
 $[(a + b) + b(b' + c)](a' + c)$