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Courses » Integral Equations,calculus of variations and its applications

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Unit 7 - Week 6

Course outline

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Week 6

- Neumann series and resolvent kernels-II
- Equations with convolution type kernels-I
- Equations with convolution type kernels-II
- Singular integral equations-I
- Singular integral equations-II
- Quiz : Assignment 6
- Solutions of

Assignment 6

The due date for submitting this assignment has passed.

As per our records you have not submitted this assignment. **Due on 2018-09-12, 23:59 IST.**

1) With the aid of resolvent kernel, the solution of the integral equation **1 point**

$$\phi(x) = 1 - 2x - \int_0^x e^{x^2-t^2} \phi(t) dt, \text{ is}$$



$$e^{x^2-x} (1 + 2x)$$



$$e^{x^2-x} - 2x$$



$$e^{x^2-x}$$



$$e^{x^2-x} + 2x$$

No, the answer is incorrect.

Score: 0

Accepted Answers:

$$e^{x^2-x} - 2x$$

2) With the aid of resolvent kernel, the solution of the integral equation **1 point**

$$\phi(x) = xe^{\frac{x^2}{2}} + \int_0^x e^{-(x-t)} \phi(t) dt \text{ is}$$



$$e^{\frac{x^2}{2}} (x + 1) - 1$$



$$e^{\frac{x^2}{2}} (x + 1)$$



$$x^2$$

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Accepted Answers:

$$e^{\frac{x^2}{2}}(x+1) - 1$$

3) The solution of the convolution type integral equation

1 point

$$\phi(x) = e^x + 2 \int_0^x \cos(x-t)\phi(t)dt, \text{ is}$$

$$e^x$$

$$e^x(1+x)$$

$$e^x(1+x)^2$$

$$e^x(1+x^2)$$

No, the answer is incorrect.

Score: 0

Accepted Answers:

$$e^x(1+x)^2$$

4) The solution of the convolution type integral equation

1 point

$$\phi(x) = e^{2x} + \int_0^x e^{t-x}\phi(t)dt \text{ is}$$

$$e^{2x}$$

$$\frac{e^{2x}}{2}$$

$$(3e^{2x} - 1)$$

$$\frac{(3e^{2x}-1)}{2}$$

No, the answer is incorrect.

Score: 0

Accepted Answers:

$$\frac{(3e^{2x}-1)}{2}$$

5) The solution of the system of integral equations

1 point

$$\phi_1(x) = e^{2x} + \int_0^x \phi_2(t)dt,$$

$$\phi_2(x) = 1 - \int_0^x e^{2(x-t)}\phi_1(t)dt,$$

is

$$\phi_1(x) = e^x - 2, \quad \phi_2(x) = 2e^x - 3e^{2x}$$

$$\phi_1(x) = 3e^x - 2, \quad \phi_2(x) = 2e^x - 3e^{2x}$$

$$\phi_1(x) = 3e^x - 2, \quad \phi_2(x) = 3e^x - 2e^{2x}$$

$$\phi_1(x) = e^x - 2, \quad \phi_2(x) = 3e^x - 2e^{2x}$$

No, the answer is incorrect.

Score: 0

Accepted Answers:

$$\phi_1(x) = 3e^x - 2, \phi_2(x) = 3e^x - 2e^{2x}$$

6) The solution of the system of integral equations

1 point

$$\phi_1(x) = x + \int_0^x \phi_2(t) dt$$

$$\phi_2(x) = 1 - \int_0^x \phi_1(t) dt$$

$$\phi_3(x) = \sin x + \frac{1}{2} \int_0^x (x-t)\phi_1(t) dt, \text{ is}$$



$$\phi_1(x) = 2 \sin x, \phi_2(x) = 2 \cos x, \phi_3(x) = x$$



$$\phi_1(x) = 2 \sin x, \phi_2(x) = 2 \cos x + 1, \phi_3(x) = x^2$$



$$\phi_1(x) = 2 \sin x, \phi_2(x) = 2 \cos x - 1, \phi_3(x) = x^2$$



$$\phi_1(x) = 2 \sin x, \phi_2(x) = 2 \cos x - 1, \phi_3(x) = x$$

No, the answer is incorrect.**Score: 0****Accepted Answers:**

$$\phi_1(x) = 2 \sin x, \phi_2(x) = 2 \cos x - 1, \phi_3(x) = x$$

7) The solution of the Cauchy type integral equation

1 point

$$x^2 = \int_2^x \frac{y(t) dt}{(x^2 - t^2)^{\frac{1}{2}}} \quad 2 < x < 4 \text{ is}$$



$$y(x) = \frac{4x(x^2-2)(x^2+4)^{-\frac{1}{2}}}{\pi}$$



$$y(x) = \frac{4x(x^2+2)(x^2-4)^{-\frac{1}{2}}}{\pi}$$



$$y(x) = \frac{4x(x^2-2)(x^2-4)^{-\frac{1}{2}}}{\pi}$$



$$y(x) = \frac{4(x^2-2)(x^2-4)^{-\frac{1}{2}}}{\pi}$$

No, the answer is incorrect.**Score: 0****Accepted Answers:**

$$y(x) = \frac{4x(x^2-2)(x^2-4)^{-\frac{1}{2}}}{\pi}$$

8) The solution of the Cauchy integral equation $x = \int_x^4 \frac{g(t) dt}{(t-x)^{\frac{1}{3}}}$, is

1 point



$$g(x) = \frac{-3}{2\pi} (4-x)^{\frac{2}{3}} (8-3x)$$



$$g(x) = \frac{-3\sqrt{3}}{2\pi} (4-x)^{\frac{-2}{3}} (8-3x)$$



$$g(x) = \frac{-3}{2\pi} (4-x)^{\frac{2}{3}} (3x-8)$$



$$g(x) = \frac{\sqrt{3}}{2\pi} (4-x)^{\frac{-2}{3}} (3x-8)$$

No, the answer is incorrect.

Score: 0

Accepted Answers:

$$g(x) = \frac{\sqrt{3}}{2\pi} (4-x)^{\frac{-2}{3}} (3x-8)$$

9) The solution of Cauchy type integral equation

1 point

$$1 = \int_{\frac{\pi}{2}}^x \frac{g(t)dt}{(\cos t - \cos x)^{\frac{1}{2}}}, \quad \frac{\pi}{2} < x < \pi \text{ is}$$



$$g(t) = \frac{1}{\pi} (\sin t)(-\cos t)^{\frac{1}{2}}$$



$$g(t) = \frac{1}{\pi} (\sin t)(-\cos t)^{\frac{-1}{2}}$$



$$g(t) = \frac{1}{\pi} (-\cos t)^{\frac{1}{2}}$$



$$g(t) = \frac{-1}{\pi} (\sin t)(-\cos t)^{\frac{-1}{2}}$$

No, the answer is incorrect.

Score: 0

Accepted Answers:

$$g(t) = \frac{1}{\pi} (\sin t)(-\cos t)^{\frac{-1}{2}}$$

10) The solution of the Cauchy type integral equation

1 point

$$x = \int_x^4 \frac{u(t)dt}{(t-x)^{\frac{1}{4}}}, \quad 2 < x < 4 \text{ is}$$



$$u(t) = \frac{-16}{5\sqrt{2}\pi} (4-t)^{\frac{1}{4}} (t+1)$$



$$u(t) = \frac{-2\sqrt{2}}{\pi} (4-t)^{\frac{-3}{4}} (3-t)$$



$$u(t) = \frac{-2\sqrt{2}}{\pi} (4-t)^{\frac{-3}{4}} (5-t)$$



$$u(t) = \frac{-2\sqrt{2}}{\pi} (4-t)^{\frac{3}{4}} (3-t)$$

No, the answer is incorrect.

Score: 0

Accepted Answers:

$$u(t) = \frac{-2\sqrt{2}}{\pi} (4-t)^{\frac{-3}{4}} (3-t)$$

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