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Courses » Advanced Topics in Probability and Random Processes

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## Unit 7 - Week 6: Discrete Time Markov Chain

### Course outline

How to access the portal

Week 1: Introduction to probability and Random Variable

Week 2: Random process basics and infinite sequence of events

Week 3: Convergence of Sequence of Random Variables

Week 4: Applications of Convergence Theory

Week 5: Markov Chain

Week 6: Discrete Time Markov Chain

Discrete Time Markov Chain-2

Discrete Time Markov Chain-3

### Assignment 6

The due date for submitting this assignment has passed.

As per our records you have not submitted this assignment. **Due on 2018-09-19, 23:59 IST.**

1) Let  $\{X_n\}$  be a homogeneous Markov chain with the state space  $V = \{0, 1\}$ . **1 point** If  $P(X_{n+1} = 0/X_n = 0) = 0.4$  and  $P(X_{n+1} = 1/X_n = 1) = 0.3$ , then the transition probability matrix of the chain is



$$P = \begin{bmatrix} 0.4 & 0.6 \\ 0.7 & 0.3 \end{bmatrix}$$



$$P = \begin{bmatrix} 0.6 & 0.4 \\ 0.7 & 0.3 \end{bmatrix}$$



$$P = \begin{bmatrix} 0.4 & 0.6 \\ 0.3 & 0.7 \end{bmatrix}$$



$$P = \begin{bmatrix} 0.4 & 0.6 \\ 0.3 & 0.4 \end{bmatrix}$$

**No, the answer is incorrect.**

**Score: 0**

**Accepted Answers:**

$$P = \begin{bmatrix} 0.4 & 0.6 \\ 0.7 & 0.3 \end{bmatrix}$$

2) Let  $\{X_n\}$  be a homogeneous Markov chain with the state space  $V = \{0, 1, 2\}$  and state **1 point** transition probability  $p_{i,j}$ ,  $i = 0, 1, 2$ ,  $j = 0, 1, 2$ . Using the Chapman-Komogorov equation, the 2-step transition probability  $p_{1,2}^{(2)}$  can be expressed as



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Week 7:  
Continuous  
Time Markov  
Chain

Week 8:  
Martingale  
Process

New Unit

Assignment  
Solutions

$$p_{1,2}^{(2)} = p_{1,0}p_{0,2} + p_{1,1}p_{1,2} + p_{1,2}p_{0,2}$$

No, the answer is incorrect.

Score: 0

Accepted Answers:

$$p_{1,2}^{(2)} = p_{1,0}p_{0,2} + p_{1,1}p_{1,2} + p_{1,2}p_{2,2}$$

3) Which of the following matrices are not stochastic? 1 point

$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 1 & 0 & 0 \end{bmatrix}$$

$$\begin{bmatrix} \frac{1}{2} & \frac{1}{3} & 0 \\ \frac{1}{2} & \frac{1}{4} & \frac{1}{4} \\ 1 & 0 & 0 \end{bmatrix}$$

$$\begin{bmatrix} \frac{1}{2} & \frac{1}{3} & \frac{1}{6} \\ \frac{1}{2} & \frac{1}{4} & \frac{1}{4} \\ 1 & 0 & 0 \end{bmatrix}$$

$$\begin{bmatrix} \frac{1}{2} & \frac{1}{3} & 0 \\ \frac{1}{2} & \frac{1}{3} & \frac{1}{4} \\ 1 & 0 & 0 \end{bmatrix}$$

No, the answer is incorrect.

Score: 0

Accepted Answers:

$$\begin{bmatrix} \frac{1}{2} & \frac{1}{3} & 0 \\ \frac{1}{2} & \frac{1}{4} & \frac{1}{4} \\ 1 & 0 & 0 \end{bmatrix}$$

$$\begin{bmatrix} \frac{1}{2} & \frac{1}{3} & 0 \\ \frac{1}{2} & \frac{1}{3} & \frac{1}{4} \\ 1 & 0 & 0 \end{bmatrix}$$

4) Consider a 4-state Markov chain with the transition probability 1 point

matrix  $P = \begin{bmatrix} 0 & 1 & 0 & 0 \\ \frac{1}{2} & 0 & \frac{1}{2} & 0 \\ \frac{1}{3} & \frac{1}{3} & 0 & \frac{1}{3} \\ \frac{1}{4} & \frac{1}{4} & \frac{1}{4} & \frac{1}{4} \end{bmatrix}$ . The largest eigen value of  $P$  is

- 1
- 2
- 3
- 4

No, the answer is incorrect.

Score: 0

Accepted Answers:

1

5) Suppose  $\lambda = 1$  is a distinct eigen value of a  $3 \times 3$  transition matrix  $P$ . The **1 point** corresponding eigen vector is

$$\begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}$$

$$\begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix}$$

$$\begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix}$$

$$\begin{bmatrix} 1 \\ 0 \\ 1 \end{bmatrix}$$

**No, the answer is incorrect.**

**Score: 0**

**Accepted Answers:**

$$\begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix}$$

6) Consider an independent increment process  $\{W(t), t \geq 0\}$  where the **1 point** increment  $W(t+s) - W(t)$  is normally distributed.  $\{W(t), t \geq 0\}$  is an example of a

Discrete-time discrete state Markov process

Discrete-time continuous state Markov process

Continuous-time continuous state Markov process

Continuous-time discrete state Markov process

**No, the answer is incorrect.**

**Score: 0**

**Accepted Answers:**

*Continuous-time discrete state Markov process*

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