

# Unit 5 - Week 4: Graph Theory

## Course outline

### How to access the portal

### Week 1: Mathematical Logic

### Week 2: Mathematical Logic

### Week 3: Mathematical Logic And Set Theory

### Week 4: Graph Theory

- Lec 1: Introduction to graph theory
- Lec 2: Trees, Cycles , Graph coloring
- Lec 3: Bipartite Graphs
- Quiz : Assignment 4
- Feedback form

### Week 5: Graph Theory-II

### Week 6: Set Theory & Number Theory

### Week 7: Set Theory & Number Theory

### Week 8: Combinatorics

### Week 9: Combinatorics

### Live Session-1

### Week 10: Number Theory

### Live Session-2

### Week 11: Algebra

### Week 12: Algebra-II

## Assignment 4

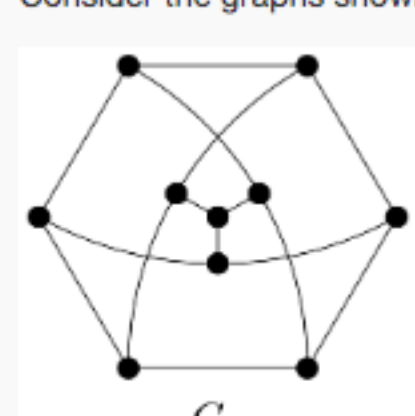
The due date for submitting this assignment has passed.  
As per our records you have not submitted this assignment.

**Due on 2019-08-28, 23:59 IST.**

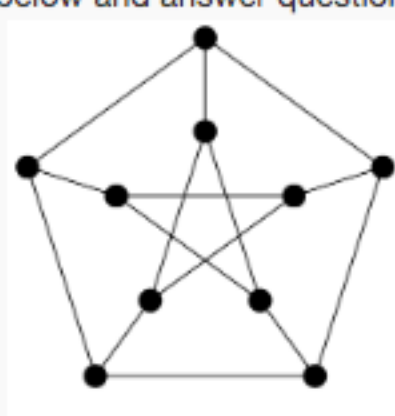
### Instructions:

- This question paper has 10 questions.
- Each question can have multiple correct options. Your answer will be treated as correct only if all the correct options are bubbled. Correct responses will be awarded 4 marks. Incorrect responses and Unattempted questions will be awarded 0 marks

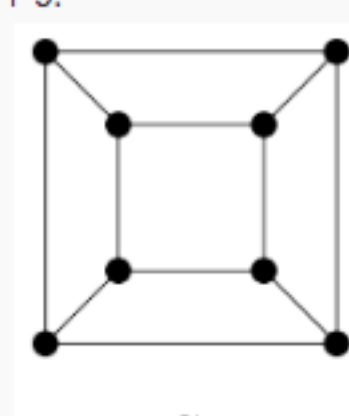
Consider the graphs shown below and answer questions 1-9.



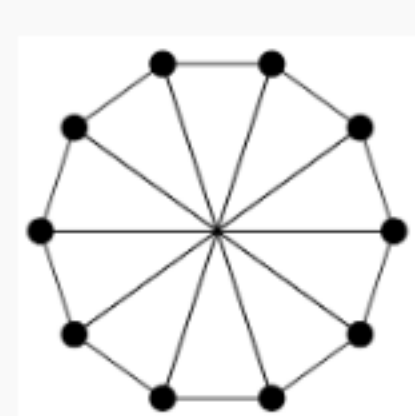
$G_1$



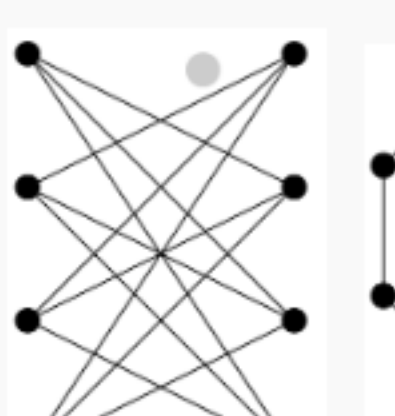
$G_2$



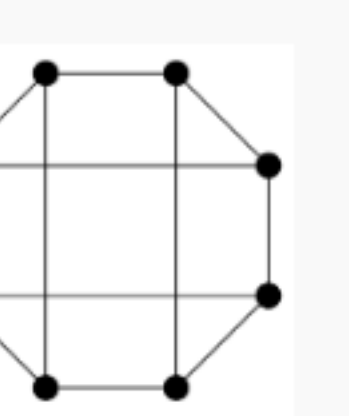
$G_3$



$G_4$



$G_5$



$G_6$

1) Which of the following pairs of graphs are isomorphic? 4 points

- $G_1, G_2$
- $G_1, G_4$
- $G_2, G_3$
- $G_3, G_6$
- $G_3, G_5$

No, the answer is incorrect.  
Score: 0

Accepted Answers:  
 $G_1, G_2$   
 $G_3, G_6$   
 $G_3, G_5$

2) Which of the following graphs are not Eulerian? 4 points

- $G_1$
- $G_3$
- $G_5$
- $G_6$

No, the answer is incorrect.  
Score: 0

Accepted Answers:  
 $G_1$   
 $G_3$   
 $G_5$   
 $G_6$

3) Which of these of graphs contain a Hamiltonian cycle? 4 points

- $G_1$
- $G_2$
- $G_5$
- $G_3$

No, the answer is incorrect.  
Score: 0

Accepted Answers:  
 $G_5$   
 $G_3$

4) What is the minimum number of edges that needed to be removed to make any one of the above graphs disconnected? 4 points

- 1
- 2
- 4
- 3

No, the answer is incorrect.  
Score: 0

Accepted Answers:  
3

5) Which of these of graphs are bipartite? 4 points

- $G_1$
- $G_2$
- $G_3$
- $G_6$
- $G_5$

No, the answer is incorrect.  
Score: 0

Accepted Answers:  
 $G_3$   
 $G_6$   
 $G_5$

6) Which of these of graphs have the least chromatic number? 4 points

- $G_1$
- $G_2$
- $G_3$
- $G_6$
- $G_4$

No, the answer is incorrect.  
Score: 0

Accepted Answers:  
 $G_3$   
 $G_6$   
 $G_4$

7) Consider graphs whose vertices are numbered 1 to  $n$ . A sequence of  $n$  numbers  $\{a_i : 1 \leq i \leq n\}$  is called a degree sequence if  $a_i$  is the degree of vertex  $i$ . Which of the following sequences are degree sequences for some graph? 4 points

- 1, 2, 3, 2, 3, 2
- 3, 3, 3, 3, 3
- 2, 4, 6, 8, 10, 11, 9
- 1, 2, 1, 2, 1, 2, 1, 2
- 3, 3, 3, 3, 3, 3

No, the answer is incorrect.  
Score: 0

Accepted Answers:  
1, 2, 1, 2, 1, 2, 1, 2  
3, 3, 3, 3, 3, 3

8) Which of the following statements are true? 4 points

- $G_2$  is a 3 regular graph.
- For every  $n$ , any connected 2 regular graph on  $n$  vertices are isomorphic
- For every  $n$ , any connected 3 regular graph on  $n$  vertices are isomorphic
- $G_5$  is a 2 regular graph.

No, the answer is incorrect.  
Score: 0

Accepted Answers:  
 $G_2$  is a 3 regular graph.  
For every  $n$ , any connected 2 regular graph on  $n$  vertices are isomorphic

9) Assume the edges of the graph  $G_2$  were given distinct positive integer weights. Let  $m$  be the weight of its minimal spanning tree. Which of the following statements are true? 4 points

- $m \leq 120$
- $m \leq 45$
- $m \geq 120$
- $m \geq 45$

No, the answer is incorrect.  
Score: 0

Accepted Answers:  
 $m \geq 45$

10) Let  $G$  be a weighted connected graph. Assume that the weights are all distinct positive integers. Which of the following statements are true? 4 points

- The least weighted edge is part of every minimal spanning tree
- The maximum weighted edge is not part of any minimal spanning tree
- The second smallest weighted edge is part of every minimal spanning tree
- The  $n-1$  heaviest edges cannot be part of any minimal spanning tree

No, the answer is incorrect.  
Score: 0

Accepted Answers:  
The least weighted edge is part of every minimal spanning tree  
The second smallest weighted edge is part of every minimal spanning tree