

# NPTEL Online Certification

## COMPUTATIONAL HYDRAULICS

### Week 4 : Assignment

July 24-October 13, 2017

1. A system ( $m$  equations) is hyperbolic at a point  $(x, t)$  for conservation law, if
    - Jacobian matrix of flux term ( $m$  numbers) with respect to variables has real eigenvalues
    - Jacobian matrix of flux term ( $m$  numbers) with respect to variables has linearly independent eigenvectors
  2. Total Variation Diminishing (TVD) scheme is
    - monotonicity preserving method
  3. Slope at  $P^{th}$  cell in numerical flux calculation with high resolution methods for Fromm method can be calculated as,
    - $\sigma_P^n = \frac{\sigma_E^n - \sigma_W^n}{2\Delta x}$
  4. Numerical flux function for Godunov method in case of one dimensional conservational law with flux term  $\mathcal{F}_\phi = a\phi$  [where  $a = \text{constant}$ ,  $a^+ = \max(a, 0)$ ,  $a^- = \min(a, 0)$ ] is
    - $\bar{\mathcal{F}}_\phi(\phi_e(0)) = a^- \phi_E^n + a^+ \phi_P^n$
    - $\bar{\mathcal{F}}_\phi(\phi_w(0)) = a^- \phi_P^n + a^+ \phi_W^n$
  5. Numerical flux function for upwind method in case of one dimensional conservational law with flux term  $\mathcal{F}_\phi = a\phi$  (where  $a = \text{constant}$ ) is
    - All of the above
  6. Lax-Friedrichs scheme for one dimensional conservational law with flux term  $\mathcal{F}_\phi = a\phi$  (where  $a = \text{constant}$ ) is
    - Conditionally stable
    - Conditionally unstable
  7. In Riemann problem, variable value
    - is different on both sides of a face under consideration.
  8. Partition of unity means
    - Summation of all shape functions within support domain is equal to 1.
  9. Polynomial basis of order 2 in one dimension contains
    - 1  $x$   $x^2$
  10. In mesh-free method, node spacing ( $d_c$ ) in two-dimension depends on
    - Area of estimated support domain
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