

# Negative feedback amplifier transfer function :

Note Title

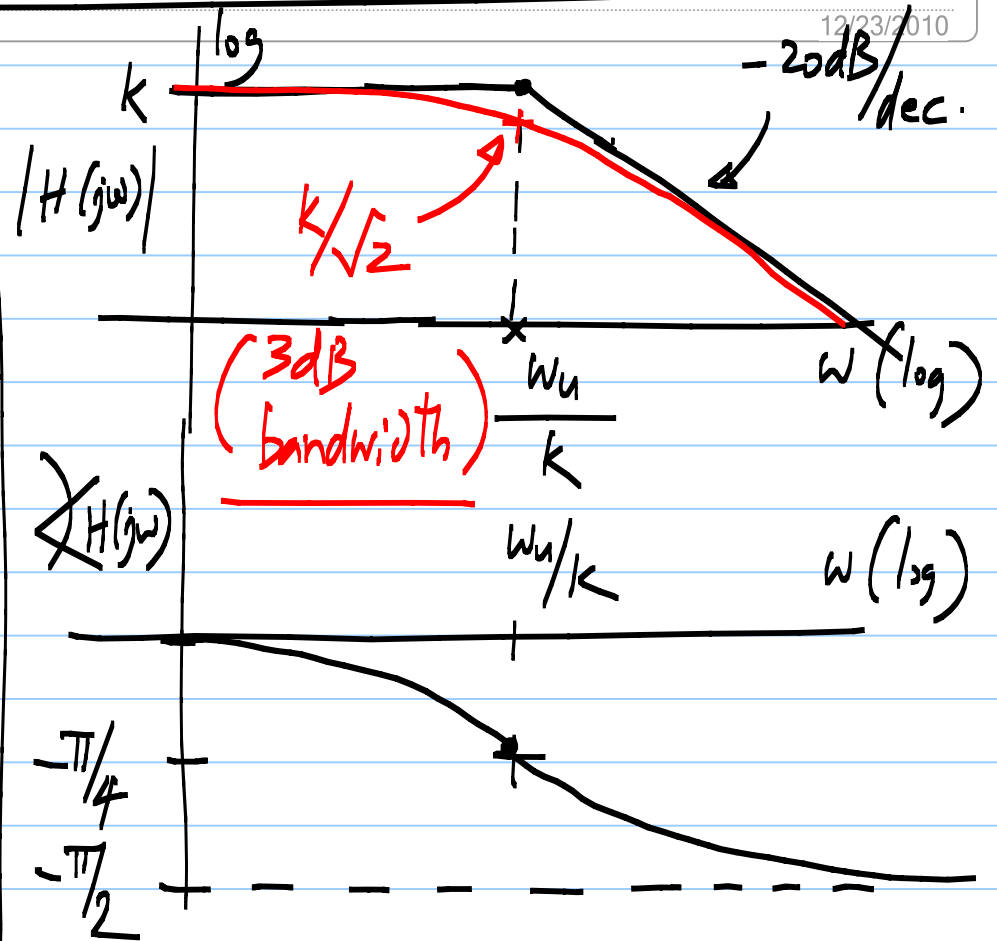
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$$H(s) = \frac{k}{1 + s \cdot \frac{k}{\omega_n}}$$

$$H(j\omega) = \frac{k}{1 + j\omega \cdot \frac{k}{\omega_n}}$$

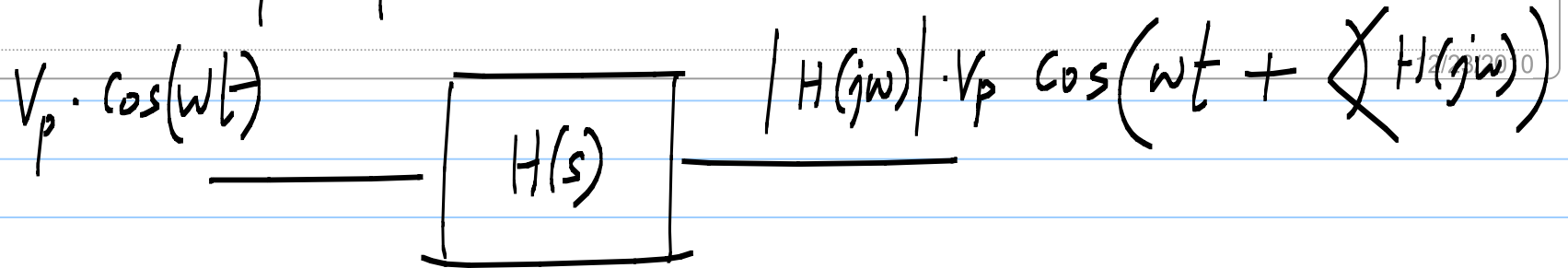
$$|H(j\omega)| = \frac{k}{\sqrt{1 + \frac{k^2 \omega^2}{\omega_n^2}}}$$

$$\angle H(j\omega) = -\tan^{-1}\left(\frac{\omega \cdot k}{\omega_n}\right)$$



Transfer function :  $H(s)$

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Input :  $V_p \cos \omega t$

Output :  $\frac{kV_p}{\sqrt{1 + \frac{\omega^2 k^2}{\omega_n^2}}} \cdot \cos \left( \omega t - \tan^{-1} \left( \frac{\omega \cdot k}{\omega_n} \right) \right)$

$$\text{Input: } V_p \cos \omega t$$

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$$\text{Output: } \frac{kV_p}{\sqrt{1 + \frac{\omega^2 k^2}{\omega_n^2}}} \cdot \cos \left( \omega t - \tan^{-1} \left( \frac{\omega \cdot k}{\omega_n} \right) \right)$$

$$\omega \ll \frac{\omega_n}{k}$$

$$\tan^{-1} x \approx x$$

$$\text{output} \approx kV_p \cdot \cos \left( \omega t - \frac{\omega \cdot k}{\omega_n} \right)$$

$$= \underline{kV_p} \cos \left( \omega \left( t - \frac{k}{\omega_n} \right) \right)$$

Amplitude =  $kV_p$   
(Gain =  $k$ )

delay  $\left( \frac{k}{\omega_n} \right)$

Output:

$$\frac{kV_p}{\sqrt{1 + \frac{\omega^2 k^2}{\omega_n^2}}} \cos\left(\omega t - \tan^{-1}\left(\frac{\omega - k}{\omega_n}\right)\right)$$

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$$\omega \Rightarrow \frac{\omega_n}{k}$$

$$\frac{kV_p}{\sqrt{\frac{k^2 \omega^2}{\omega_n^2}}} = \frac{\omega_n}{\omega} \cdot V_p$$

$$\text{output} \approx \frac{\omega_n}{\omega} \cdot V_p \cdot \cos\left(\omega t - \frac{\pi}{2}\right)$$

Low frequencies  $\left(\omega \ll \frac{\omega_n}{k}\right)$

Note Title

Amplifier  
working  
properly

$$\text{Output} \approx kV_p \cos\left(\omega\left(t - \frac{k}{\omega_n}\right)\right)$$

- Ideal gain - independent of  $\omega_n$ , the parameter of the integrator
- Delay  $k/\omega_n$

High frequencies  $\left(\omega \gg \frac{\omega_n}{k}\right)$

$$\text{Output} \approx \frac{\omega}{\omega_n} \cdot \cos\left(\omega t - \frac{\pi}{2}\right)$$

Amplifier  
is "not  
working  
properly"

Bandwidth = usable range of  $\omega$

# Frequency domain analysis:

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- The amplifier is usable for frequencies below  $\frac{\omega_n}{K}$  (← Bandwidth of the system)
- For higher bandwidth, use an integrator with a higher  $\omega_n$

Time domain:

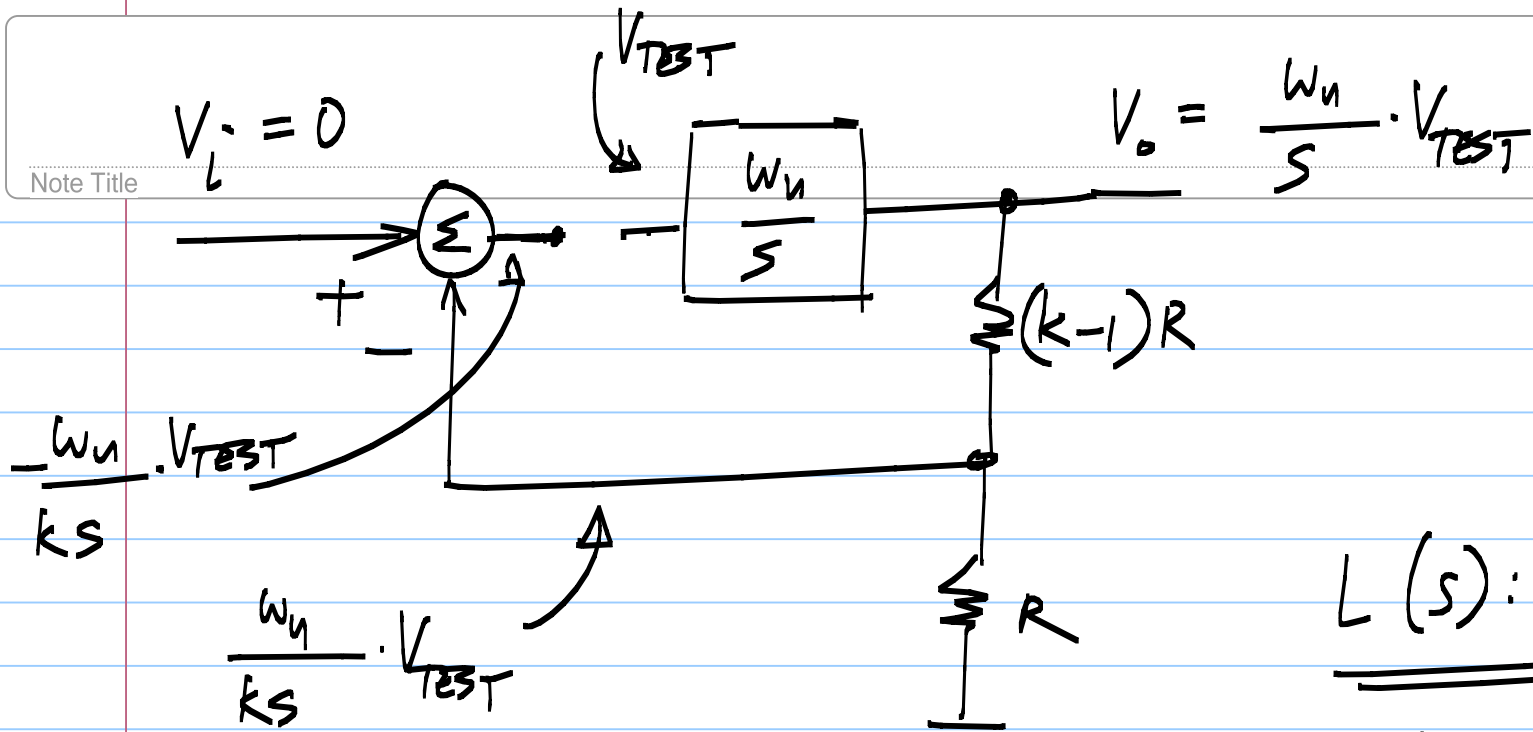
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Step response:  $V_o(t) = kV_x \left( 1 - \exp\left(-\frac{\omega_n t}{k}\right) \right)$

time constant =  $\frac{k}{\omega_n}$

Frequency domain:

pole:  $-\frac{\omega_n}{k} \rightarrow \text{Bandwidth} = \frac{\omega_n}{k}$

what is the significance of  $\frac{\omega_n}{k}$ ?



$L(s)$ : loop gain

$$L(s) = \frac{W_n}{k \cdot s}$$

$$V_{RETURN} = -\frac{W_n}{k s} \cdot V_{TEST}$$

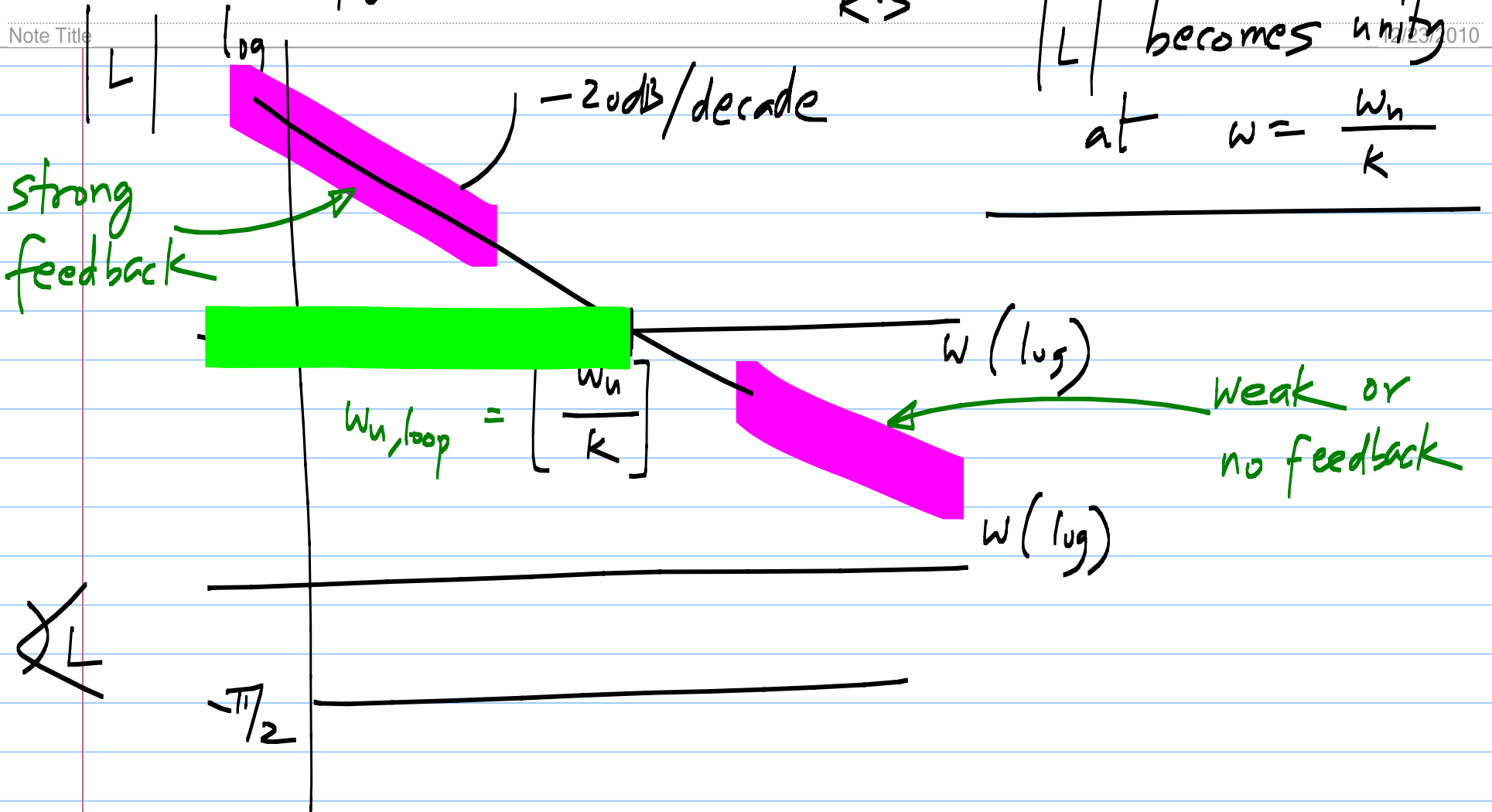
$$\frac{V_{RETURN}}{V_{TEST}} = -\frac{W_n}{k s} = -L(s)$$



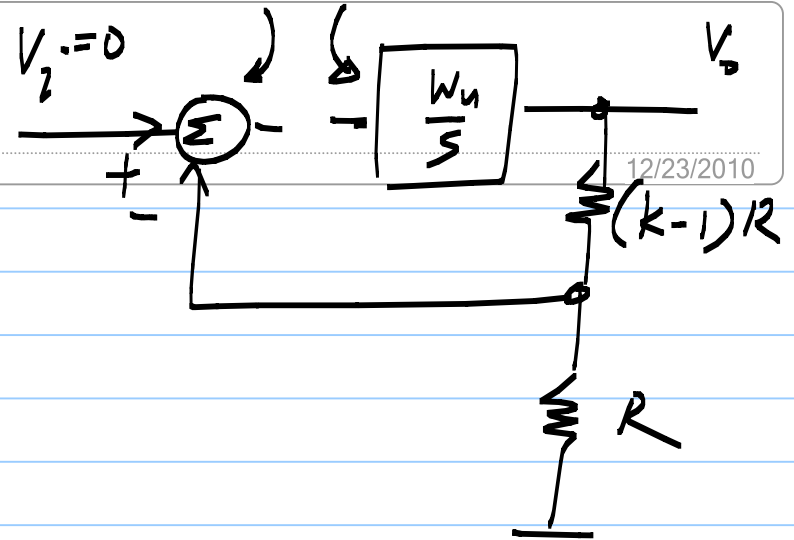
Loop gain

$$L(s) = \frac{\omega_n}{k \cdot s}$$

$|L|$  becomes unity  
at  $\omega = \frac{\omega_n}{k}$



$$\frac{V_{\text{RETURN}}}{V_{\text{TEST}}} = -L(s)$$



$L(s)$  : loop gain

Frequencies where  $|L(j\omega)| \gg 1$

- strong feedback
- ideal behavior

Unity loop gain frequency :  $\omega_{u, \text{loop}}$

Frequencies where  $|L(j\omega)| \ll 1$

- weak feedback, non-ideal behavior

The unity loop gain frequency  $\omega_{u,loop}$

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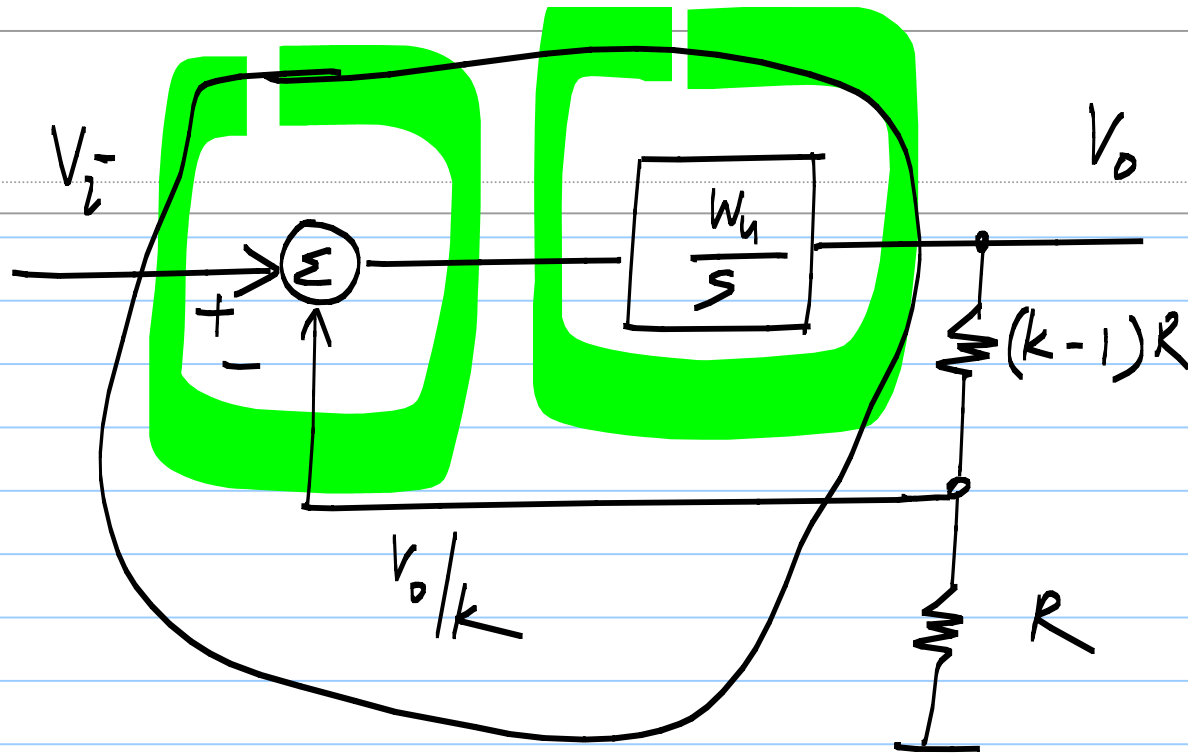
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is the frequency at which  $|L(j\omega)| = 1$

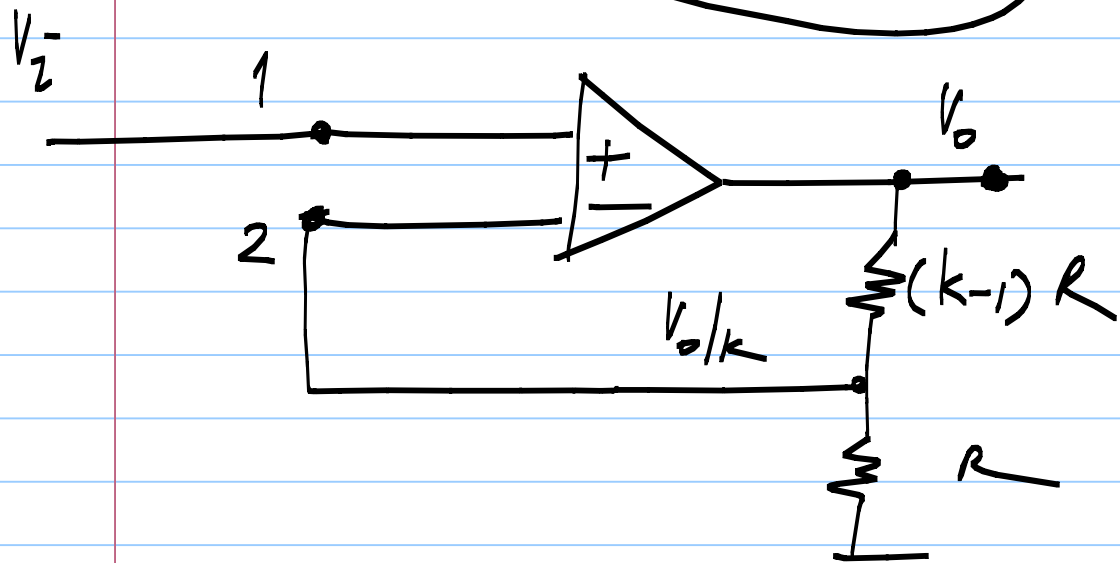
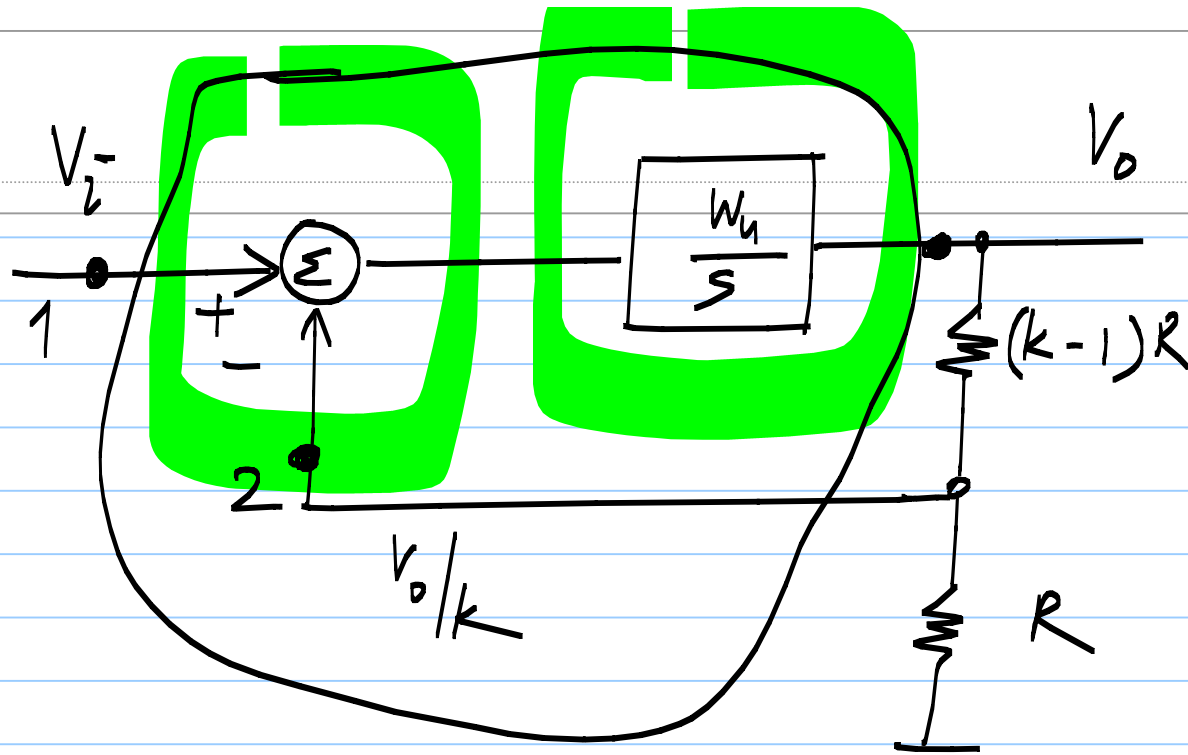
- divides regions of ideal & non ideal behavior

-  $\omega_{u,loop} \approx$  bandwidth of the negative feedback system.

$$\omega_{u,loop} = \frac{\omega_u}{K}$$



- Difference between input & feedback
  - Integrates
- Operational amplifier  
(opamp)

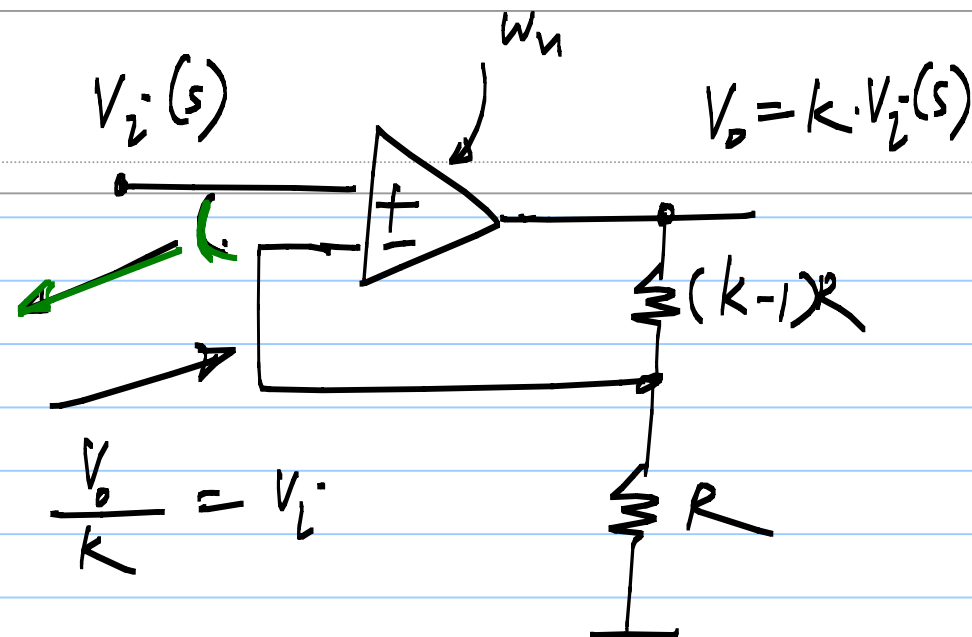


(dc gain > 0)

"Non inverting"  
amplifier

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$$\frac{V_o}{k} = V_i$$

$$\frac{V_o(s)}{V_i(s)} = \frac{k}{1 + s \cdot \frac{k}{w_u}} = k$$

$w_u$ : unity gain frequency of the opamp

$$\text{Bandwidth} = \frac{w_u}{k}$$

$$w_u = \infty \Rightarrow \text{Bandwidth} = \infty$$

Ideal opamp:

$$w_u \rightarrow \infty$$