

Voltage References

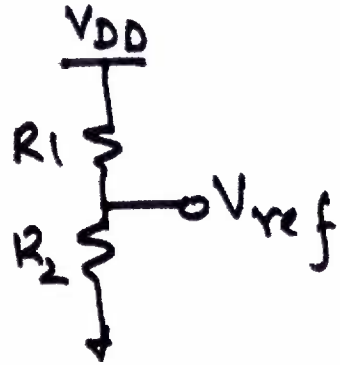
- i. Voltage Divider Reference
- ii MOS VOLTAGE Reference
- iii All MOS Divider Reference
- IV Band Gap Reference



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1. Divider Reference with Resistors



$$V_{ref} = \frac{R_2}{R_1 + R_2} V_{DD} = \frac{1}{1 + \frac{R_1}{R_2}} V_{DD}$$

$$\therefore \frac{dV_{ref}}{dV_{DD}} = \frac{R_2}{R_1 + R_2}$$

$$S_{V_{DD}}^{V_{ref}} = \frac{V_{DD}}{V_{ref}} \cdot \frac{\partial V_{ref}}{\partial V_{DD}} = \frac{R_1 + R_2}{R_2} \cdot \frac{R_2}{R_1 + R_2} = 1$$

We see $\frac{\partial V_{ref}}{V_{ref}} = \frac{\partial V_{DD}}{V_{DD}}$

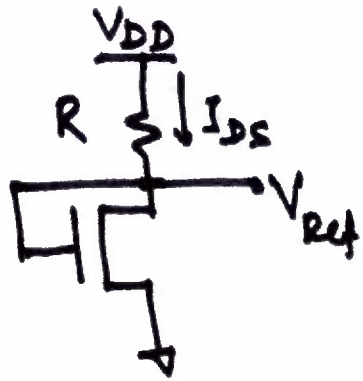
[% change in V_{DD} directly reflect in % variation of V_{ref}]

$$\begin{aligned} \therefore TC_f(V_{ref}) &= \frac{1}{V_{ref}} \cdot \frac{\partial V_{ref}}{\partial T} = \frac{R_1}{R_2} \frac{V_{ref}}{V_{DD}} \left(\frac{1}{R_2} \frac{\partial R_2}{\partial T} - \frac{1}{R_1} \frac{\partial R_1}{\partial T} \right) \\ &= \frac{R_1}{R_2} \frac{V_{ref}}{V_{DD}} [TC_f(R_2) - TC_f(R_1)] \end{aligned}$$



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Voltage Reference with MOSFET & Resistor



Clearly $V_{GS} = V_{ref}$

$$I_{DS} = \frac{V_{DD} - V_{ref}}{R}$$

But $I_{DS} = \frac{\beta}{2} (V_{ov})^2$ for Transistor

$$\therefore V_{DD} - V_{ref} = \frac{\beta}{2} R [V_{ref} - V_T]^2$$

Solving

$$V_{ref} = V_T + \sqrt{\frac{2}{\beta R} (V_{DD} - V_{ref})}$$

If $V_{DD} \gg V_{ref}$

$$\text{Then } V_{ref} = V_T + \sqrt{\frac{2}{\beta R} V_{DD}^{1/2}}$$



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Then $S_{V_{DD}}^{V_{ref}} = \frac{V_{DD}}{V_{ref}} \cdot \frac{\partial V_{ref}}{\partial V_{DD}}$

$$\equiv \frac{1}{V_T \cdot \sqrt{\frac{2\beta R}{V_{DD}} + 2}}$$



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Further

$$TC_f(V_{ref}) = \frac{1}{V_{ref}} \cdot \frac{\partial V_{ref}}{\partial T}$$

$$= \frac{1}{V_{ref}} \left[V_T \cdot TC_f(V_T) - \frac{1}{2} \sqrt{\frac{2}{w/L} \frac{V_{DD}}{R \beta'(T)}} \cdot \left[\frac{1}{R} \frac{\partial R}{\partial T} - \frac{1.5}{T} \right] \right]$$



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$$\text{Then } I_Q R = V_{Tn} + \sqrt{\frac{2 I_Q}{\beta'_n (W/L)_1}}$$

$$\therefore (I_Q R - V_{Tn})^2 = \frac{2 I_Q}{\beta'_n (W/L)_1}$$

$$\therefore I_Q^2 R^2 + V_{Tn}^2 - 2 I_Q R V_{Tn} - \frac{2 I_Q}{\beta'_n (W/L)_1} = 0$$

One solution is

$$\therefore I_Q = \frac{V_{Tn}}{R} + \frac{1}{\beta_1 R^2} + \frac{1}{R} \sqrt{\frac{2 V_{Tn}}{\beta_1 R} + \frac{1}{\beta_1^2 R^2}} = I_1 = I_2$$

and other solution is

$$I_Q = 0 \text{ giving } I_1 = I_2$$

This is trivial solution, but can occur in reality.



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Since M3 & M4 are chosen to be identical (Same β and V_T), with the mirror connected combination, $\therefore I_1 = I_2$, where I_1 flows from V_{DD} to V_{SS} (0V) through M5 and M1 and I_2 flows similarly from M4 - M2 and through R.

Clearly $V_{GS1} = I_2 \cdot R$ or $= I_1 R$

But $V_{GS1} = V_{Tn} + \sqrt{\frac{2I_1}{\beta'_n (W/L)_1}}$

$\therefore I_2 R = I_1 R = V_{Tn} + \sqrt{\frac{2I_1}{\beta'_n (W/L)_1}}$

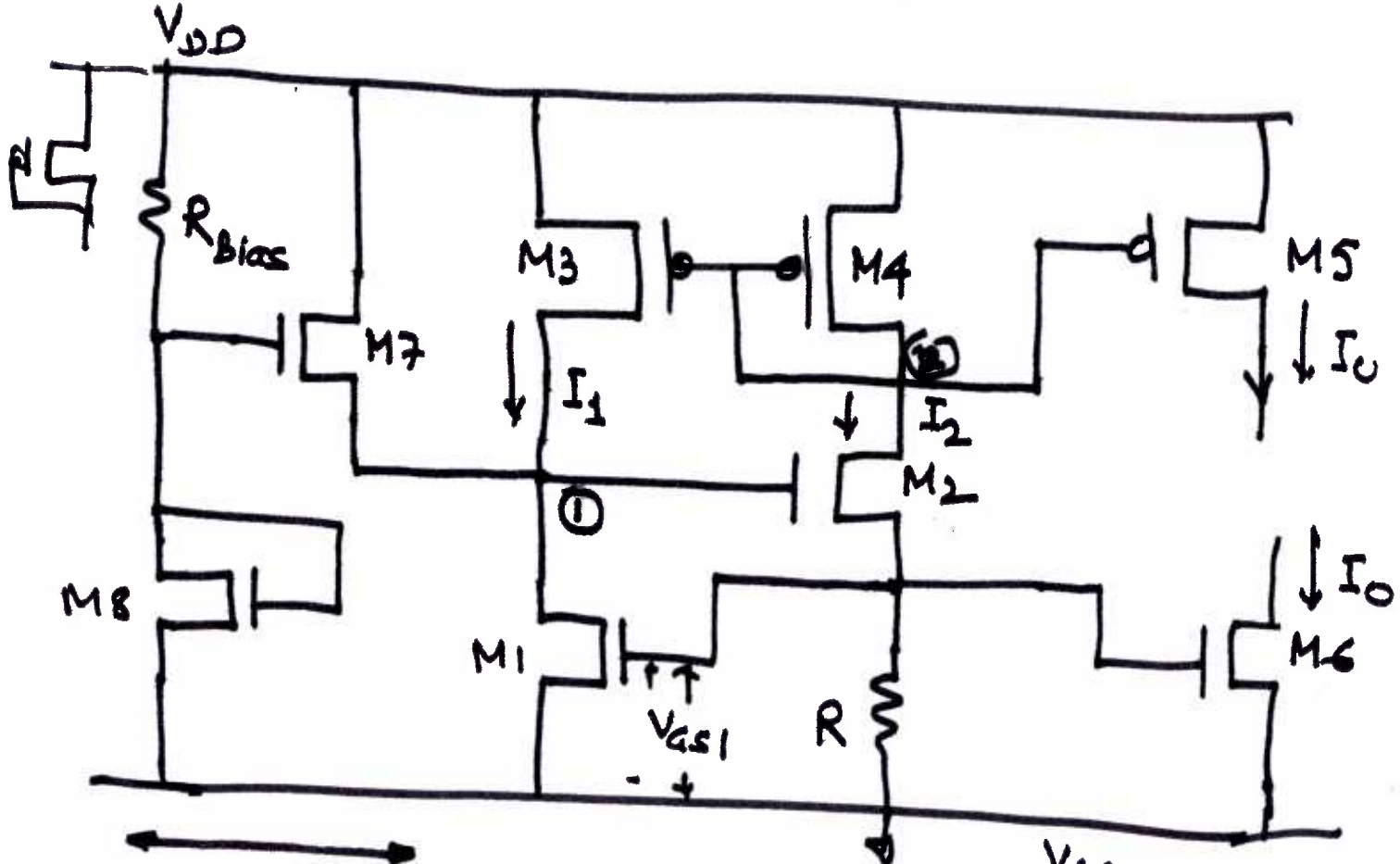
We define $I_1 = I_2 = I_Q$

A Better V_T reference is possible using Bootstrap Technique.



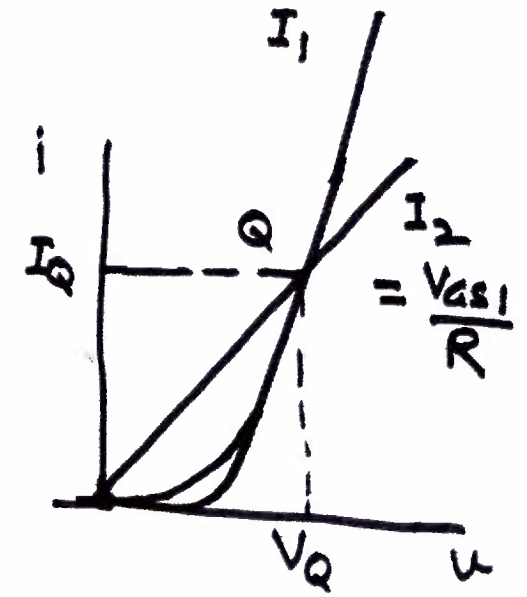
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Start-up
Circuit

Bootstrap Circuit for V_T reference.



In case of $I_1 = I_2 = I_Q = 0$, we see that we need a start-up circuit.

Transistor M7 is 'ON' when initially Node ① is at '0' V. Thus M7 provides

current to M1. This increases V_{GS1} of M1, which in turn increases I_2 ($\frac{V_{GS1}}{R}$). By feedback (& Mirror) action Node ① voltage starts increasing ($V_{GS1} + V_{GS2}$) and at one time V_{GS} for M7 goes below V_{T7} , thereby shutting off M7. Here the Q point of Reference reaches second stable point. Further Starting Circuit then stops participating.



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If R is created from Polysilicon Layer (nt),

$$\text{then } TC_f(R) = \frac{1}{R} \frac{dR}{dT} \cong -2000 \text{ ppm}/^\circ\text{C}$$

The β -Multiplier circuit thus show

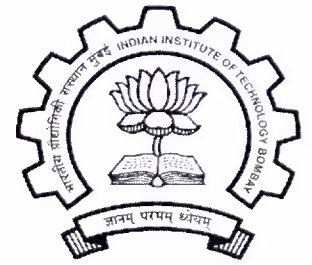
$$TC_f(I_0) = -2 \times 2000 + \frac{1.5}{T} (\text{ok})$$

$$= +1000 \text{ ppm}/^\circ\text{C} \quad \text{at } T = 300^\circ\text{K}$$

We can use this circuit as Voltage Reference V_{REF} equal to V_{AS1}

$$V_{REF} = V_{AS1} = \frac{2}{\beta_1 R} \left(1 - \sqrt{\frac{1}{K}} \right) + V_{TN}$$

$$\frac{\partial V_{REF}}{\partial T} = \frac{\partial V_{TN}}{\partial T} + \frac{2}{\beta_1 R} \left(1 - \sqrt{\frac{1}{K}} \right) \left[\frac{1}{R} \frac{dR}{dT} + \frac{1}{\beta_1} \frac{\partial \beta_1}{\partial T} \right]$$



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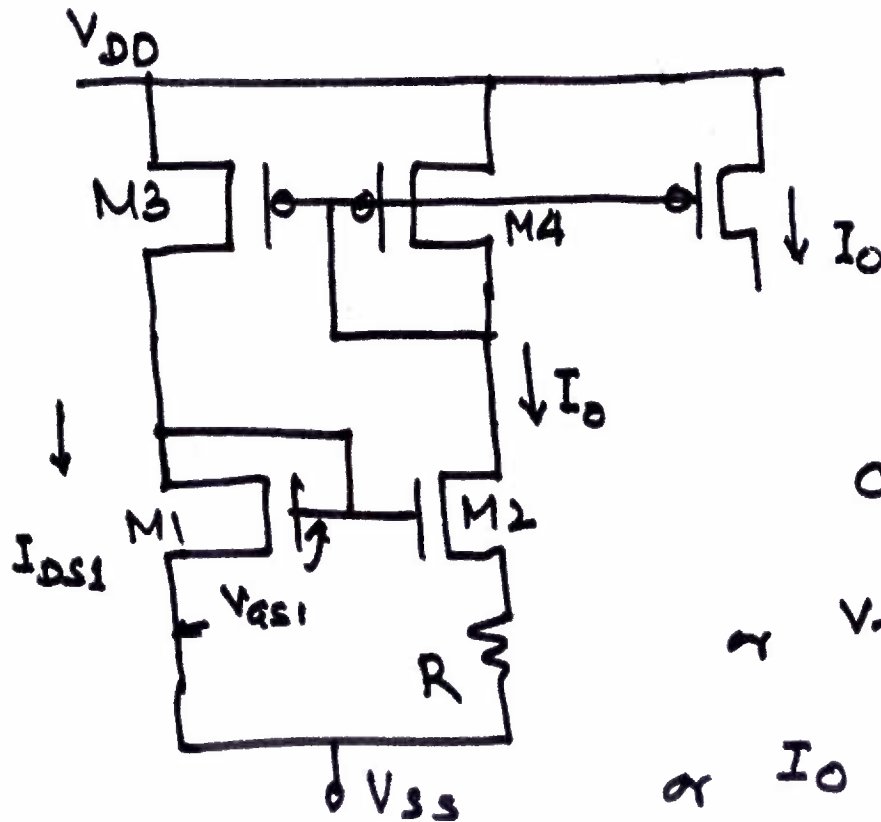
β - Multiplier V_{REF} .



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This scheme is also called Self-Biasing Scheme
This also uses 'Starting Circuit' for Operation to begin.



$$I_{DS1} = I_O$$

Here width of M_2 , W_2 is chosen K times of width W_1 of M_1

$$\alpha \beta_2 = K \beta_1$$

clearly $V_{GS1} = V_{GS2} + I_O R$

$$\alpha V_{TN} + \sqrt{\frac{2I_O}{\beta_1}} = V_{TN} + \sqrt{\frac{2I_O}{K\beta_1}} + I_O R$$

$$\alpha I_O \cong \frac{2}{R^2 \beta_1} \left(1 - \frac{1}{\sqrt{K}}\right)^2$$

We can find value of k , for $\frac{dV_{REF}}{dT} = 0$

Thus choice of k can give $TC_f(V_{REF}) = 0$

Corresponding

$$V_{REF} = V_{TN} + \frac{2}{R\beta_1} \left[1 - \frac{1}{\sqrt{k}} \right]$$



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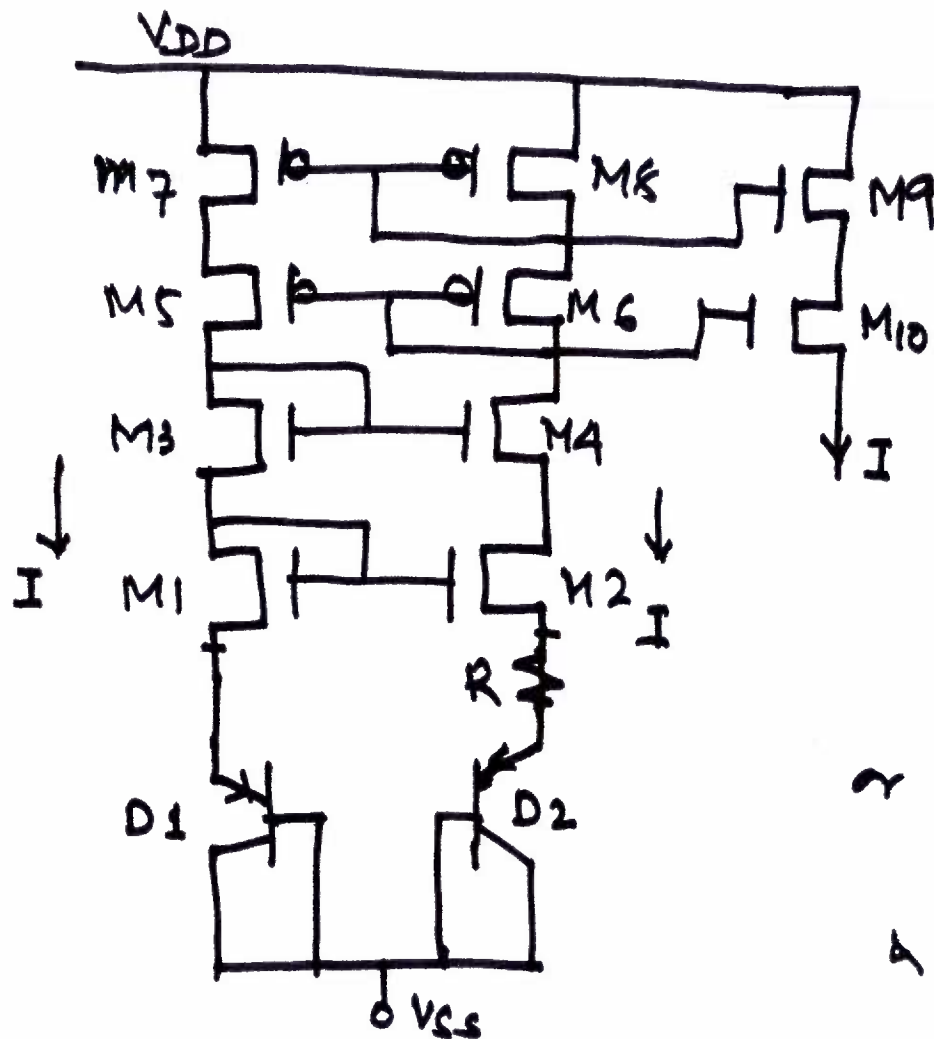
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PTAT Current Biasing Scheme



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As $V_{GS1} = V_{GS2}$
for same current
in M1 & M2

Also $\beta_2 = k \beta_1$ ($W_2 = kW_1$)

$\therefore V_{GS1} = V_{DS1} = IR + V_{DS2}$ — (1)

Diode currents are

$$I_{D1} = I = I_{sat} e^{\frac{qV_{BE}}{kT}}; \quad V_{BE} = V_{DS1}$$

$$\begin{aligned} \approx V_{DS1} &= \frac{nkT}{q} \ln \frac{I}{I_{sat}} \\ \text{A } V_{DS2} &= \frac{nkT}{q} \ln \frac{I}{k \cdot I_{sat}} \end{aligned} \quad \text{(2)}$$

Substituting (2) in (1)

$$\frac{nkT}{q} \ln \frac{I}{I_{sat}} = \frac{nkT}{q} \ln \frac{I}{K \cdot I_{sat}} + IR$$

$$\frac{nkT}{q} \ln \left(\frac{I/I_{sat}}{I/K I_{sat}} \right) = IR$$

$$\text{or } IR = \frac{nkT}{q} \ln K$$

$$\text{or } I = \frac{nkT}{qR} \cdot \ln K$$

$$= \frac{V_{Thermal}}{R} \cdot \ln K$$

$\therefore I \propto T$ (Proportional to Absolute Temperature)

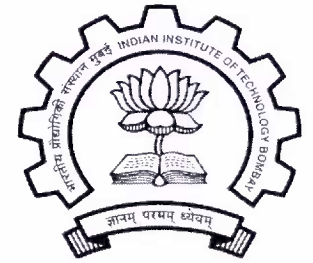
$$TC_f(I) \sim 1000 \text{ ppm}/^\circ\text{C}$$



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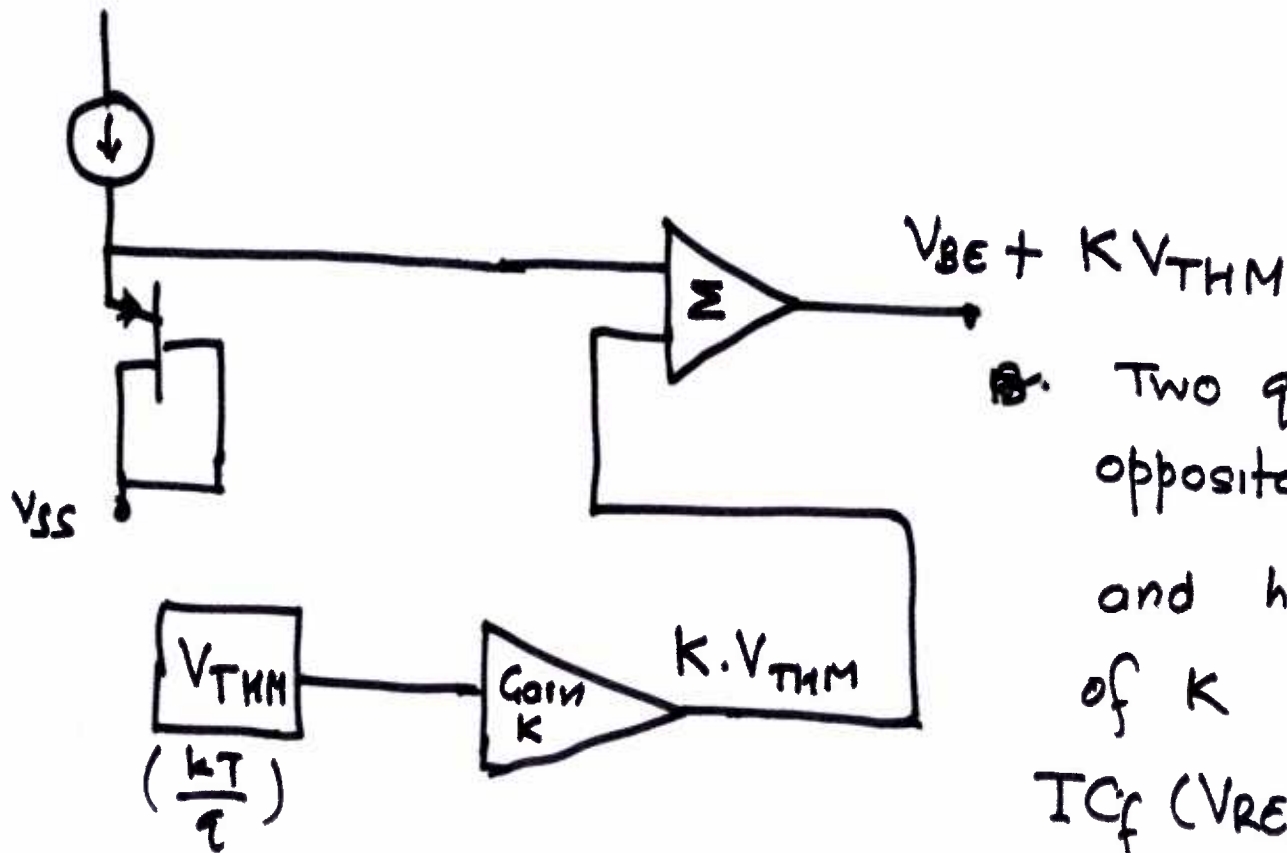
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Principle of BANDGAP REFERENCE



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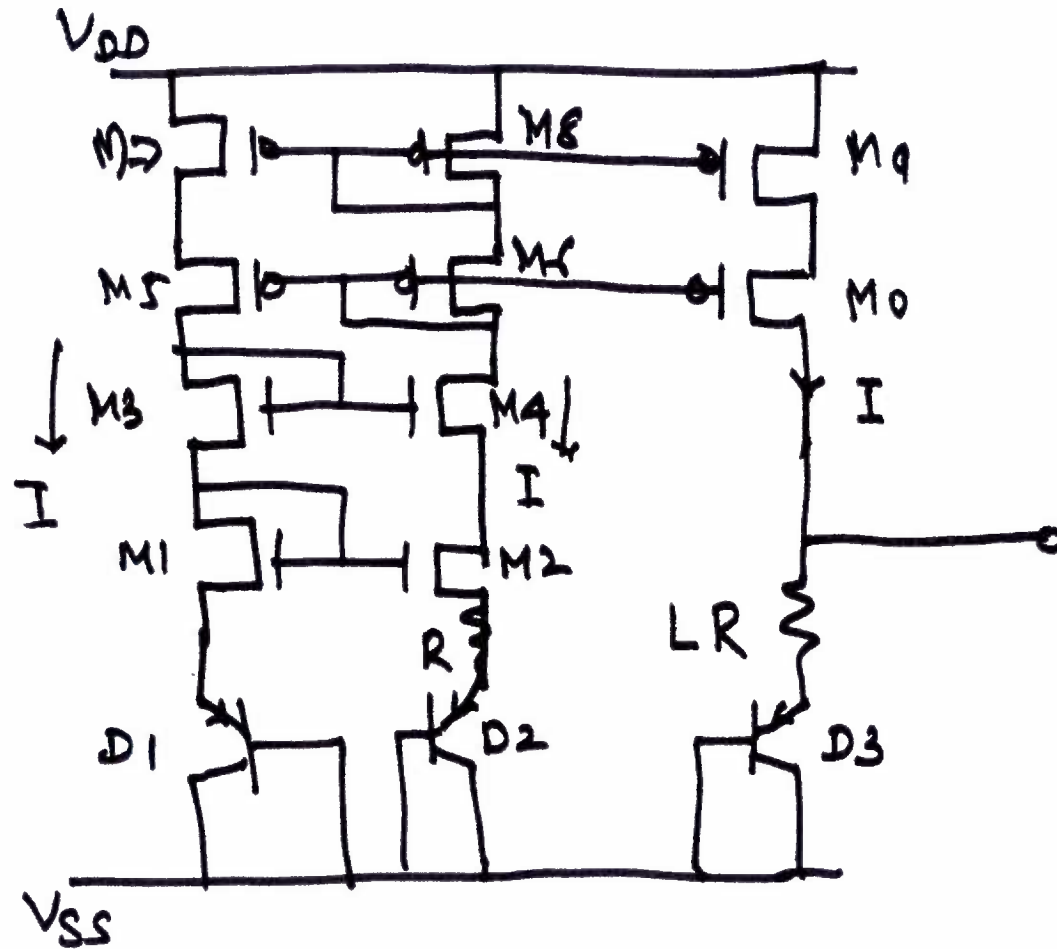
Two quantities have opposite Polarity TC_f and hence by adjustment of K
 $TC_f (V_{REF}) \rightarrow 0$

Bandgap Reference Circuit



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$$V_{Thermal} = \frac{kT}{q}$$

To the PTAT circuit, we have

additional resistance LR

and Diode D3 in output arm.

Then we get V_{ref} with near

$$TC_f(V_{ref}) \rightarrow 0$$

V_{ref}

From PTAT ckt

$$I = \frac{V_{Thermal} \ln(K)}{R}$$

$$\text{Then } V_{\text{Ref}} = V_{D3} + I \cdot L \cdot R$$

$$= V_{D3} + \frac{L V_{\text{Thermal}}}{1} \ln K$$

$$V_{D3} = \frac{n k T}{q} \ln \frac{I}{K I_{\text{sat}}}$$

$$\therefore V_{\text{REF}} = L \cdot V_{\text{THM}} \cdot \ln K + V_{\text{TMM}} \ln \frac{I}{K I_{\text{sat}}}$$

$$= V_{\text{THM}} \left[L \ln(K) + \ln \frac{I}{K I_{\text{sat}}} \right]$$

For normal diode in CMOS Technology, with $L=12$ & $K=8$

we get $V_{\text{REF}} = 1.25\text{V}$ (Bandgap of Silicon)

Further $\frac{dV_{\text{REF}}}{dT} \rightarrow \equiv 0$ + value - value. If Adjust K, L is done



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