

Remote sensing and inverse transport modeling of the Kasatochi eruption sulfur dioxide cloud

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Abstract.

An analytical inversion method is used to estimate the vertical profile of SO₂ emissions from the major eruption of Kasatochi volcano in Alaska in August 2008. The method uses satellite-observed total SO₂ columns from GOME- 2, OMI and AIRS during the first two days after the eruption, and an atmospheric transport model, FLEXPART, to calculate the vertical emission profile. The inversion yields an emission profile with two large emission maxima near 7 km above sea level (a.s.l) and around 12 km a.s.l, with smaller emissions up to 20 km. The total mass of SO₂ injected into the atmosphere by the eruption was estimated to 1.7 Tg, with ~1 Tg reaching the stratosphere (>10 km). The estimated vertical emission profile was robust against changes of the assumed eruption time, meteorological input data and satellite data used. Using the vertical emission profile, a simulation of the transport extending for one month after the eruption is performed. The simulated plume agrees very well with SO₂ columns observed by GOME-2, OMI and AIRS until 6 days after the eruption, and the altitudes agree with both CALIPSO measurements and ground-based lidar observations to within 1 km. The method is computationally very fast. It is therefore suitable for implementation within an operational environment, such as the Volcanic Ash Advisory Centers (VAACs), to predict the threat posed by volcanic emissions for air traffic.

1. Introduction

Volcanic eruptions can inject particles and gases high into the atmosphere. Generally, the major component is tephra, also called volcanic ash, which is solidified material. The most abundant gases emitted are water vapour (H_2O) and carbon dioxide (CO_2). Another important gas emitted by volcanic eruptions is sulfur dioxide (SO_2) which is of special concern for the global climate and the ozone layer if it reaches the stratosphere. Explosive volcanic eruptions can emit SO_2 to very high altitudes (> 10 km) in contrast to anthropogenic and other emissions which occur mostly at low altitudes.

Airborne volcanic ash is a danger to aircraft because it can cause serious damage, and even loss of power on the engines. There are nine Volcanic Ash Advisory Centers (VAACs) around the world that advise international aviation of the location and movement of volcanic ash clouds. The VAACs use satellite information, ground reports from volcanological agencies, pilot reports, meteorological knowledge and numerical models to track and forecast ash movement so that aircraft can fly around or over the airborne ash safely [VAAC, 2008]. A fundamental piece of information required by the VAACs is the height of the ash clouds, as this is the principal determinant of the ash transport and potential hazard to jet aircraft.

For non-explosive volcanic eruptions, the injection height of the emissions is of the order of a few hundred meters and is dominated by thermal plume rise. On the other hand, explosive eruptions have a considerable initial exit velocity, and the high thermal energy in the eruption plumes allows them to quickly reach high altitudes (> 10 km). Generally the injection height depends on the kind of eruption and meteorological conditions (e.g., the horizontal winds,

humidity and thermal stratification) [*Oberhuber et al.*, 1998]. For explosive eruptions characterized by a Volcanic Explosivity Index (VEI) of 2–3 (moderate scale) 20% of volcanic plumes rise higher than 15 km, 60% rise above 10 km, and 80% rise above 6 km [*Halmer and Schmincke*, 2003]. For the eruption of Mount Pinatubo in June 1991 (VEI~6, “colossal”), gas and particles were carried to an altitude of more than 30 km [*McCormick et al.*, 1995]. Once the species are injected into the stratosphere they are rapidly advected around the globe.

Dispersion models can forecast the long-range transport of the emissions. However, one problem is the vertical transport in the eruption column which they cannot explicitly simulate. Thus, the vertical emission profile is needed as an input parameter, which must be determined by other means. Determining the emission height profile of a volcanic eruption is a challenge. In principle, it can be obtained by special models like the Active Tracer High Resolution Model (ATHAM) which can simulate the vertical transport of ash in the eruption column. However, they require accurate estimates of the mass flux of pyroclastic material and other information that is normally not available, especially not on a near-real time basis [*Textor et al.*, 2003; *Oberhuber et al.*, 1998].

Measurements using aircraft [*Mankin et al.*, 1992] and weather radar and lidar observations [*Wang et al.*, 2008] can provide information on the plume height. However, not all locations are covered by such observations. Remote sensing observations from satellites can provide global coverage, but normally they only deliver total columns or very poorly resolved vertical profiles. Also, many instruments operate from low-earth orbits providing only one or two overpasses per day limiting the temporal resolution of the measurements. Other methods can potentially provide

information on the SO₂ vertical distribution in the lower troposphere by calculating a residual based on SO₂ columns from infrared and ultraviolet satellite retrievals [*Carn et al.*, 2008].

A common technique to estimate the vertical emission profile for the purpose of volcanic plume forecasting involves trial-and-error fits between satellite observations of the total column of volcanic debris and model results based on different assumptions of the emission height. The HYbrid Single-Particle Lagrangian Integrated Trajectory (HYSPLIT) model, for example, can be used with satellite measurements of SO₂ from the Ozone Monitoring Instrument (OMI), to fit trajectories at certain altitudes with the observations [e.g., *Carn et al.*, 2008]. The disadvantage with this method is that the model runs and satellite data are matched “by eye”. This is a subjective process that is time-consuming and can lead to errors.

In this paper, we present the vertical emission height profile of SO₂ derived through an analytical inversion method. The SO₂ is often more easily observed by satellite sensors than ash. While in a sheared atmosphere the ash and SO₂ in eruption clouds may travel in different horizontal directions, it is likely that the SO₂ is accompanied by some ash. Thus, often SO₂ can serve as a proxy for volcanic ash. The SO₂ is also important for geochemical and climate modeling in itself.

The inverse method has recently been developed by *Eckhardt et al.* [2008] and tested in a case study of the 30 September 2007 low-latitude eruption of the Jebel at Tair volcano (15.55°N, 41.83°E) located in the Red Sea. The Jebel at Tair eruption was an ideal test case because it provided excellent observation conditions for satellite remote sensing (a dry cloudless atmosphere) and very good coverage by such observations. For this paper, which is based on the

first author's master thesis [Kristiansen, 2009], the inverse method is tested for the high-latitude eruption of Kasatochi Volcano in August 2008. The observation conditions for this eruption were more difficult and, thus, provide a more demanding test case for the inverse method.

2 Kasatochi Volcano, Alaska

Kasatochi Volcano (52.17°N, 175.51°W) is a small (2.7×3.3 km) unpopulated island volcano situated on the Aleutian arc. The active stratovolcano reaches only 314 m above sea level (a.s.l) [Smithsonian Institution, 2008]. From 7-8 August 2008 Kasatochi volcano erupted with little warning after lying dormant for more than 200 years [Alaska Volcano Observatory, 2008]. The eruption emitted 1.2 – 2.5 Tg of SO₂ to the atmosphere [e.g., Prata et al., 2009; NASA, 2008; Karagulian et al., 2009; Richter et al, 2009a; Rix et al., 2008], which is the largest SO₂ mass loadings since Chile's Hudson volcano erupted in 1991. The eruption also injected an amount of ash into the atmosphere [Prata et al., 2009] and Alaska Airlines was forced to cancel 44 flights between 10 and 11 August 2008 [O'Malley and Bragg, 2008]. The ash particles were deposited after a few days, while the SO₂ dispersed throughout the northern hemisphere. Theys et al. [2009] also reported large enhancements of bromine monoxide (BrO) seen in satellite data in the vicinity of Kasatochi in the days following the eruption.

The Alaska Volcano Observatory (AVO) reported that three distinct explosive eruptions occurred at Kasatochi at approximately 22:01 UTC on 7 August, 01:50 UTC and 04:35 UTC on 8 August [Waythomas et al., 2008]. The first two events produced relatively ash-poor, but gas-rich eruption clouds that reached approximately 14.5 - 16.5 km a.s.l. The third event generated an ash- and gas-rich plume that rose to about the same altitude, and was followed by about 17

hours of continuous ash emission as determined from satellite data. *Prata et al.* [2009] show that the ash and SO₂ erupted from Kasatochi was collocated and could be observed to travel together for at least 3 days following the 8 August eruptions, thus SO₂ may serve as an appropriate proxy for ash in this case.

Synoptic maps of geopotential heights of the pressure levels 1000 hPa and 500 hPa shortly after the first eruption, taken from the European Centre for Medium-Range Weather Forecasts (ECMWF) analysis, are shown in Figure 1. A low pressure system was passing over the area in the hours of the eruptions, which generated a distinct circular shaped SO₂ plume, as seen from the AIRS satellite measurements. The thermal tropopause height around the Kasatochi volcano, given by the ECMWF data, was about 10 km. Given the reported injection height from AVO (~14.5 - 16.5 km) the debris from the eruption penetrated into the stratosphere.

3. Atmospheric transport modeling

In this study the Lagrangian particle dispersion model FLEXPART ([*Stohl et al.*, 1998, 2005], see also <http://transport.nilu.no/flexpart>) was used to simulate the transport of SO₂ emitted by the eruption of Kasatochi volcano. The model was first described and validated by *Stohl et al.* [1998] with data from continental-scale tracer experiments and is now used for a large range of applications, including simulating the dispersion of volcanic plumes [*Prata et al.*, 2007; *Eckhardt et al.*, 2008].

FLEXPART calculates trajectories of “tracer particles” (not necessarily representing real particles, but infinitesimally small air parcels) as they are displaced by the winds.

For this study, the model simulations were based on meteorological analysis data provided by ECMWF [ECMWF, 2002]. The global ECMWF data has 91 vertical levels, and $1^\circ \times 1^\circ$ horizontal resolution. A nest with higher resolution of $0.5^\circ \times 0.5^\circ$ was used for the area of interest (the eastern North Pacific region: 180°W - 120°W , 40°N - 60°N). Analyses at 00:00, 06:00, 12:00 and 18:00 UTC as well as 3-h forecasts at intermediate times were used. We also made alternative FLEXPART simulations using input data from the National Centers for Environmental Prediction Global Forecast System (GFS) model with $0.5^\circ \times 0.5^\circ$ resolution at 26 pressure levels.

Trajectories of SO_2 tracer particles are calculated using the mean winds interpolated from the analysis fields as well as random motion representing turbulence [Stohl and Thompson, 1999]. For moist convective transport, FLEXPART uses the scheme of Emanuel and Živković-Rothman [1999], as implemented and tested in FLEXPART by Forster et al. [2007].

In the atmosphere, SO_2 is lost by reaction with OH, dry deposition, and aqueous-phase chemical reactions. Monthly averaged three-dimensional OH concentration fields provided from the GEOS-CHEM model [Bey et al., 2001], were used to determine tracer mass loss by reaction with OH. This process is most important in the troposphere. Aqueous-phase chemical reactions were not considered in the model simulations. Dry deposition of SO_2 was calculated with the resistance method [Wesely and Hicks, 1977] using data from Wesely [1989] with updates.

FLEXPART model runs were used as input to the inversion method to explore the sensitivity of downwind SO_2 total columns to the altitude and mass of the initial emissions. Fifty releases were configured in vertically stacked emission layers of 500 m thickness between the model ground

and 25 km above the volcano. In each of these layers, 300 000 tracer particles were released uniformly along a vertical line source and subsequently tracked in the model atmosphere. Three different simulations were executed with particles released at the times of the eruption onsets as reported by AVO; on 7 August 22:01 UTC, 8 August 01:50 UTC and 04:35 UTC. The simulation extended for 2 d after the eruption onset. Concentrations were calculated as hourly means throughout the simulation. The output grid was $0.5^{\circ} \times 0.5^{\circ}$ horizontally, with 9 vertical layers of 2 km resolution between 4 km and 22 km, a single layer between the surface and 4 km, and another layer from 22-50 km a.g.l. From this model output, total atmospheric columns were computed using averaging kernels as described in Section 4.4. The simulations can be viewed as source-receptor relationships which measure the sensitivity of a column value to the emission strength in each of the emission layers. Using these sensitivities and satellite observations of total SO₂ columns, the inversion finally yields estimates of the actual mass injected in each of the layers above the volcano.

After applying the inversion method and obtaining the estimated emission profile of SO₂, a longer FLEXPART simulation of the transport was performed. This simulation extended over one month following the eruption onset and was used for validation of the estimated profile by comparison with independent observations.

4. Remote Sensing Data

Several satellite instruments made measurements of the SO₂ released by the eruption of Kasatochi Volcano over the days following the eruption. For this study we have utilized both ultraviolet and infrared satellite retrievals of SO₂. The instruments measuring in the ultraviolet

spectral region include the Global Ozone Monitoring Experiment-2 (GOME-2) and the Ozone Monitoring Instrument (OMI), while the Atmospheric Infra-Red Sounder (AIRS) provides infrared measurements.

All of the instruments deliver total or partial column measurements with little vertical resolution. The infrared retrievals provide partial column measurements due to very low sensitivity to SO₂ in the moist lower troposphere, while the ultraviolet retrievals can detect SO₂ down to the ground. Depending on which altitude the SO₂ is located and on other factors such as the temperature and humidity profiles, the different retrievals may yield different column amounts. One big advantage of the AIRS retrievals is the ability to make observations also during nighttime, while the ultraviolet measuring instruments are restricted to daytime observations with high solar elevation. All satellite data were re-sampled to the FLEXPART 0.5°×0.5° output grid.

In addition, the Infrared Atmospheric Sounder Interferometer (IASI) provided measurements of the eruption of Kasatochi which were utilized by *Karagulian et al.* [2009] to retrieve a coarse-resolution vertical profile of SO₂. This profile has been applied to our inversion algorithm as *a priori* information.

4.1. GOME-2

The GOME-2 instrument is a UV/visible spectrometer covering the wavelength region of 240 - 790 nm at a moderate spectral resolution of 0.2 - 0.4 nm with a ground-pixel size of 80 x 40 km² over most of the globe [*Munro et al.*, 2006]. With its large swath, GOME-2 provides global coverage nearly daily. SO₂ retrievals are performed with a variant of the Differential Optical

Absorption Spectroscopy (DOAS) method. Using the spectral window of 312.5 - 327 nm, tabulated slant optical depths of SO₂ and ozone are fitted to the observed optical thickness. For the initial iteration, an *a priori* of 1 Dobson Unit (1DU=2.69×10¹⁶ molecules/cm²) SO₂ vertical column is used. Depending on the retrieved column, a new SO₂ optical depth is selected based on a more appropriate *a priori*. This procedure is repeated until closure is found between the retrieved and the *a priori* column. This iterative retrieval approach is necessary as SO₂ becomes a strong absorber in the UV at the high column amounts experienced during the Kasatochi eruption and ignoring this effect leads to strong underestimation of the total column. Similar approaches have been proposed by *Richter et al.* [2006] and *Yang et al.* [2007] for situations with much less SO₂. After the main retrieval, each orbit is post processed to remove a small latitudinal offset in the SO₂ columns by applying a median filter over ±10°latitude. This correction is similar to the one applied to OMI SO₂ data [*Yang et al.*, 2007] and is negligible compared to the columns discussed here. Details on the retrieval can be found in *Richter* [2009b]. As discussed in *Yang et al.* [2007], both the vertical distribution of SO₂ and the ozone column also impact on the results. Here, the US standard atmosphere has been assumed for O₃ and an SO₂ plume of 1 km thickness centered at an altitude of 10.5 km. These constant assumptions together with the impact of clouds and aerosols which have not been accounted for lead to a relatively large uncertainty of the SO₂ columns retrieved in the Kasatochi plume. We estimate this uncertainty to be of the order of 10% in the plume while the noise level outside the plume is better than 1 DU for individual measurements. Maximum SO₂ mass loadings for the eruption of Kasatochi were found to be up to about 2.5 Tg from GOME-2 [*Richter et al.*, 2009a].

4.2. OMI

The OMI instrument on board the EOS/Aura satellite was designed principally for measuring global ozone, but with secondary goals of measuring other trace gases, including SO₂. It measures solar back-scattered radiation in the UV between 270 and 365 nm. The daytime equator crossing time is 10:45 UTC, the nadir pixel size is 13×24 km² and the swath width is 2600 km which provides once-daily global coverage.

SO₂ column data from OMI are produced using the Band Residual Difference (BRD) algorithm [Krotkov *et al.*, 2006] and the Linear Fit (LF) algorithm [Yang *et al.*, 2007]. For this study we used the product estimate of the column density of SO₂ for the upper tropospheric and stratospheric SO₂ (ColumnAmountSO2_STL). The retrieval used for determining SO₂ from OMI exploits the SO₂ absorption features between 310 and 340 nm. The effect of absorption by ozone in the same spectral region, and also effects of Rayleigh multiple scattering, the “Ring effect” and the geometrical air-mass factor have been accounted for in the algorithm. For large SO₂ columns (>100 DU), such as for Kasatochi, the retrieval error increases and the algorithm underestimates the true SO₂ amount. An overall uncertainty of 14 % for the OMI retrievals is assumed to be appropriate for the large SO₂ columns for Kasatochi [K. Yang (pers.comm) and Yang *et al.*, 2007]. Maximum SO₂ mass loadings for the eruption of Kasatochi were found to be about 1.4 Tg from OMI (NASA [2008] and <http://earthobservatory.nasa.gov/IOTD/view.php?id=8998>).

4.3. AIRS

The AIRS instrument on board the EOS-Aqua polar orbiting satellite was able to clearly detect the SO₂ cloud from Kasatochi for about 1 week and less well in the following weeks as the cloud diluted and moved over Europe and on to Russia. The IR retrievals have less sensitivity than the UV retrievals and thus AIRS cannot detect the SO₂ for as long as OMI or GOME-2. The AIRS instrument has high spectral resolution and is operating at infrared wavelengths between 3.7 and 15.4 μm [Chahine *et al.*, 2006]. The swath width is $\pm 49^\circ$ from nadir producing nadir pixels with dimensions $15 \times 15 \text{ km}^2$, increasing to $18 \times 40 \text{ km}^2$ at the swath edge. The SO₂ partial column abundances were determined by use of the retrieval scheme developed by Prata and Bernardo [2007]. The algorithms for determining SO₂ from AIRS exploit the strong SO₂ anti-symmetric absorption feature near 7.3 μm , but because water vapour also absorbs strongly across this band, the retrievals are restricted to regions of the atmosphere that are relatively dry, i.e. - the upper troposphere (heights > 3 km) and lower stratosphere. AIRS error estimates for an individual pixel are at worst $\pm 6 \text{ DU}$, and typically $\pm 3 \text{ DU}$ [Prata and Bernardo, 2007].

Maximum UTLS mass loadings were found to be $\sim 1.2 \text{ Tg}$ from this instrument, which is lower than that found using ultra-violet measurements. The difference is mostly due to the lower sensitivity to pixels with low SO₂ amounts ($< 3 \text{ DU}$), the narrow AIRS swath width, which sometimes excluded portions of the plume and to a lesser extent the penetration depth of the AIRS measurements. For SO₂ clouds that are high and thick, it is possible for the IR bands to saturate and an upper limit on SO₂ detection is reached. Examination of the AIRS IR spectra suggests that this did not occur in the case of Kasatochi.

Table 1 gives an overview of the estimates of total mass emitted from the eruption of Kasatochi, derived from various satellite retrievals.

4.4. Height sensitivity

The satellite retrievals depend on a number of factors such as the wavelength region of the satellite measurements, the atmospheric temperature profile and the vertical distribution of all absorbing gases. This implies that the magnitude of the observed SO₂ signal does not only depend on the total SO₂ amount in the atmosphere but also on its vertical distribution which cannot be obtained from the measurements themselves. Thus, in the satellite retrievals of SO₂ certain assumptions have to be made about the height of the SO₂ cloud. In regard to this, the weighting function and averaging kernel are used as described by *Rodgers* [2000] (page 15, 56, and 223). The weighting function represents the radiance contribution from a layer at a certain height level to the total radiance sensed by the satellite. The averaging kernel is the sensitivity of the retrieval to the true state and is needed in comparisons between in situ profile measurements and satellite retrievals and in application of data assimilation.

We use the averaging kernels shown in Fig. 2 when comparing satellite data and model data. Because the vertical sensitivities of the various satellite retrievals are variable, it would be inaccurate to directly compare the reported total columns with total columns obtained from FLEXPART. Instead, it is necessary to sample the FLEXPART SO₂ concentration vertical profile with the corresponding averaging kernel of the satellite retrieval.

For the AIRS satellite data, we use an averaging kernel for a band-averaged channel at around $7.3 \mu\text{m}$ for a perturbed atmosphere with a layer of SO_2 present at 15 km. In practice the $7.3 \mu\text{m}$ channel is sensitive to the absorption of both water vapour and SO_2 , which means that whenever SO_2 and water vapour are collocated it is difficult to quantify the SO_2 . However, the two-step retrieval procedure devised by *Prata and Bernardo* [2007] accounts for both SO_2 and water vapour simultaneously.

For UV retrievals, the averaging kernel depends also on surface albedo and O_3 column, but it is in particular the atmospheric SO_2 profile that is problematic in the presence of large SO_2 amounts as the atmosphere below a thick SO_2 layer is basically shielded from the satellite view.

For GOME-2, we approximate the averaging kernel by a single calculation performed at 317 nm for a UV surface albedo of 0.03 and a 1 km thick SO_2 column of 200 DU. For OMI, the height sensitivity is explained by *Yang et al.* [2007]. For this study we have used an averaging kernel for a cloud-free pixel with a surface reflectivity of 0.1 and a prescribed SO_2 profile in Umkehr layer 3 (see Fig. 7 of *Yang et al.* [2007]).

Ideally, one should use a different averaging kernel for each pixel to account for regional variability. However, in this study, only one typical averaging kernel for each of the three satellite data sets was employed.

4.5. Lidar measurements

The Kasatochi plume was observed with both ground-based and satellite-based aerosol lidar instruments. The Cloud-Aerosol Lidar with Orthogonal Polarization (CALIOP) lidar on board the Cloud-Aerosol Lidar and Infrared Pathfinder Satellite Observation (CALIPSO) satellite made measurements of the Kasatochi eruption clouds several times in the weeks after the eruption. CALIPSO was launched in 2006 and flies as a part of the A-train at 705 km altitude in a 98°-inclination sun-synchronous polar orbit. The equator-crossing time is at 10:30 UTC with a 16-day repeat cycle. CALIOP provides profiles of backscatter at 532 nm and 1064 nm, as well as the degree of the linear polarization of the 532 nm signal. It is a nadir-only looking instrument (60 m pixel size spaced 330 m apart) providing a curtain of measurements with a vertical resolution of 30–300 m. We have utilized the primary level 1 data products of total attenuated backscatter at 532 nm and 1064 nm. The attenuated backscatter profile is the calibrated, range-corrected, laser energy normalized, baseline-subtracted lidar return signal (see *Hostetler et al.* [2006] for more details).

The Dalhousie Raman Lidar at Halifax, Nova Scotia (44.6°N, 63.6°W), Canada, observed the debris from Kasatochi for several months after the eruption. The instrument is described by *Bitar* [2009]. It employs a frequency-doubled Nd:YAG laser transmitting pulses of 532 nm light into the atmosphere at a frequency of 20 Hz, and a 25 cm telescope with photomultipliers and fast counting electronics in the receiver. Profiles of the aerosol extinction coefficient are derived from the measured elastic lidar signals using the Klett inversion technique [*Klett*, 1981]. A constant aerosol extinction-to-backscatter (lidar) ratio of 40 sr was assumed, which is consistent

with the lidar ratio observed for stratospheric aerosols after volcanic eruptions [*Jäger and Deshler*, 2002, and references therein].

The AWIPEV station, operated by AWI (Alfred-Wegener-Institute for Polar and Marine Research) and IPEV (Institut polaire français Paul-Emile Victor) in Ny-Ålesund (78.9°N, 11.9°E) on Svalbard observed the Kasatochi plume using the Koldewey-Aerosol-Raman-Lidar (KARL). KARL is a backscatter-Raman lidar determining the concentration of aerosols in the atmosphere using a pulsed Nd:YAG laser which emits beside the 1064 nm fundamental laser line the frequency doubled (532 nm) and tripled (355 nm) laser lines with a pulse repetition frequency of 50 Hz. The receiving telescope has a diameter of 30 cm (for further details, see *Hoffmann et al*, [2009]). The aerosol backscatter coefficient is calculated with the Klett algorithm [*Klett*, 1981] based on 10 minute integrated profiles with a vertical resolution of 60 m.

The lidar measurements were used to validate the height of the simulated SO₂ plume. The aerosol extinction coefficient is roughly proportional to the total aerosol mass and was used as a proxy of the sulphate concentrations in the atmosphere. Aerosols are formed by the conversion of SO₂ to sulphate and the validation was done by comparing the lidar measurements with the SO₂ concentration simulated by FLEXPART. The comparison is qualitative as aerosol extinction coefficient and concentration of SO₂ are two different quantities. However, because one is formed from the other, it is expected that SO₂ and aerosols are at the same altitude.

5. Inversion algorithm

The inversion method used in this study is based on work of *Seibert* [2000] and has been expanded and described recently by *Eckhardt et al.* [2008]. They improved it to allow for an *a priori* for the unknown sources, a Bayesian formulation considering uncertainties for the *a priori* sources and the observations and an iterative algorithm for ensuring a solution with only positive values. A major advantage of this algorithm is that it provides an almost entirely analytical solution of the optimization problem, making it very fast and reliable.

Like in other inverse problems [e.g., *Menke*, 1984], we have observations that depend on a number of control variables through a physical process which can be quantitatively simulated. Here, the observations are sets of (weighted) SO₂ column values, the control variables are the SO₂ emission rates as a function of height (and possibly time) on a discrete raster, and the physical process is the transport, diffusion and transformation of SO₂ in the atmosphere.

The optimum solution (values of the control parameters) is defined as that which leads to the best agreement between observed and simulated values. “Best” agreement is measured as the sum of the squared differences. Different to the ordinary Root Mean Square Errors (RMSE), however, we are taking into account uncertainty variances as weights for forming the sum. This leads to a “most likely” solution in the statistical sense, provided at least that the errors are normally distributed and independent.

If there were sufficient observation data and not too many unknown control variables, this would be enough to obtain a solution to our problem. Minimising the cost function consisting of the

weighted squared errors yields a linear system of equations that can be solved analytically with standard linear algebra methods and software tools. However, if we construct the vector of unknowns as a simple stack of emissions in equidistant vertical layers, we could easily find that some parts, e.g. close to the ground (low sensitivity of the satellite retrievals) or at high levels near or above the top of the eruption column (small wind shear), are not well constrained by observations. This could render the solution unstable, even if the number of known variables exceeds well the number of unknowns, leaving us with a so-called ill-conditioned inverse problem. To prevent this, some form of *a priori* knowledge has to be added.

In the method used here, two forms of *a priori* knowledge are used. One is a prescribed estimate of the emission profile (typically very smooth, possibly vertically constant) together with an uncertainty (usually formulated as a fraction of the first-guess estimate). The other is the assumption that the vertical profile is not zig-zagging wildly, mathematically expressed as a small absolute value of the second derivative. Both assumptions provide additional terms to be added to the cost function and can be formulated as linear operators on the vector of unknowns. Thus, we can still proceed with the same standard solution method.

The mathematical formalism would allow negative values to occur in the solution. To render the solution more physically meaningful, we use an iterative process to reduce the uncertainty of the first-guess where the solution is negative until the resulting solution is not negative.

All the mathematical details can be found in *Eckhardt et al.* [2008]. What remains is the proper specification of the *a priori* profile and the uncertainties (weights). For this study, the *a priori*

emissions were based on the shape of a coarse-resolution IASI SO₂ profile estimated by Karagulian *et al.* [2009], which shows a broad maximum centered around 12 km. The total mass of the *a priori* profile was specified to 1.3 Tg, which is in agreement with the minimum of the satellite emission estimates (see Table 1). The *a priori* uncertainties were chosen to allow substantial corrections to the initial profile (see Figures 4 and 6).

The standard errors of the observations should contain not only the uncertainty of the retrieved SO₂ columns but rather be standard misfit between the observations and the model results. Because detailed error statistics are lacking, we assume that a large part of the error stems from the model simulation. For the UV satellite data, with an overall uncertainty of the retrievals of about 10-14 %, we used a standard error of 20% of the individual pixel value plus 3 DU, giving a minimum of 3 DU uncertainty for all pixels. For AIRS, a 30% + 3 DU uncertainty was chosen based on the instrument's poorer sensitivity.

The algorithm presently does not give an explicit estimate of the uncertainty of the solution. However, we examine its uncertainty by performing multiple inversions with different data sets and model results.

6. Results and discussion

6.1. Comparison of satellite data

SO₂ column amounts retrieved from GOME-2, OMI and AIRS approximately 2 days after the eruption, between 20:53 UTC on 9 August and 00:13 UTC on 10 August are shown in Figure 3. The plume has mainly drifted southeastward from the volcano over the Pacific Ocean. The SO₂ distributions obtained from the three instruments are qualitatively similar, but the absolute values vary. For instance, the maximum GOME-2 and OMI columns are, respectively, about four times larger and two times larger than the maximum AIRS column.

The reasons for the discrepancies between the different satellite data sets are not entirely clear. However, since AIRS retrievals give only partial SO₂ columns, with SO₂ in the lower troposphere not being captured, a negative bias of the AIRS columns was expected. Also since the GOME-2 retrieval accounts for nonlinearities in the absorption and light path, this results in higher SO₂ values than for OMI. The different pixel sizes, sampling times and different sensitivities to low SO₂ amounts also contribute to the differences between instruments.

It is clear that the biases between the different satellite data sets will cause problems when they are used jointly in the inversion procedure. Ideally, one should apply bias corrections before using these data for the inversions. However, it is not clear which data set should best serve as a reference and the factors determining the biases are not completely understood. Furthermore, the biases cannot easily be described with constant scaling factors. Therefore, we have used the satellite data without bias corrections and leave this task for the future.

6.2. SO₂ emission height profiles

Satellite data for up to two days after the eruption were used for the inversions. During that time interval, seven, two and four overpasses over the Kasatochi SO₂ plume were available for AIRS, OMI and GOME-2, respectively. In addition to using three different satellite data sets, inversions were performed for three different assumed eruption times, 22:01 UTC on 7 August, 01:50 UTC and 04:35 UTC on 8 August, corresponding to the eruption times reported by AVO. For each inversion we assume that all SO₂ mass was emitted at one single eruption time. This is because we lack information on how much SO₂ was likely emitted during each eruption, and it is possible that most of the SO₂ was actually emitted during a single eruption. This approximation may yield inaccuracies, however as the time intervals between the eruptions are not very long, and the ECMWF wind profiles at Kasatochi did not change much over the interval that the eruptions occurred, this approach is assumed valid. Furthermore we used two different meteorological input data sets from ECMWF and GFS, for driving the FLEXPART simulations used for the inversion.

Figure 4 shows the results from the inversions for the 22:01 UTC eruption time using satellite data from one instrument at a time, and using ECMWF data for the model simulation. Generally, the emission profiles show that the eruption of Kasatochi resulted in large emissions of SO₂ both in the middle and upper troposphere (5-10 km) as well as in the lower stratosphere (10-15 km), with two strong emission peaks at ~7 km and ~12 km. Smaller emissions are found up to ~20 km. The largest stratospheric peak extends up to about 15-17 km which corresponds to the reports from AVO indicating emissions up to 14.5 - 16.5 km. On average, ~50% of the total mass is injected above the thermal tropopause at 10 km.

474

475 The strength of the two largest emission peaks depends on the satellite data set used. The
476 inversion with GOME-2 data (red line) gives the largest stratospheric peak, and also the largest
477 total SO₂ mass (2.4 Tg). The OMI profile (green line) is similar but with reduced emission peaks
478 and a total SO₂ mass of 1.1 Tg. The AIRS profile (blue line) with a total SO₂ mass of 1.5 Tg,
479 shows a strong ~7 km emission peak, a smaller stratospheric peak around 12 km, and also more
480 emissions above 15 km. The anomalous peaks below 4 km are probably due to the poor
481 sensitivity of AIRS in the lower troposphere.

482

483 The total SO₂ mass derived from the different AIRS overpasses were strongly fluctuating, partly
484 because there were only two AIRS overpasses which covered the whole plume. Only for the
485 overpass on 9 August 23:53 UTC (see figure 3), was the total mass within the same range (~1
486 Tg) as the GOME-2 and OMI total masses. Therefore, inversions were performed also using this
487 overpass only (turquoise line). This also demonstrates that even when only one satellite overpass
488 is used, results can be in good agreement with profiles based on more satellite data.

489

490 Subsequently, inversions were performed for all the three satellite data sets combined, and also
491 for each of the three eruption times and for each of the two meteorological input data types. To
492 compare the performance of the various inversions, we calculated Pearson correlation
493 coefficients between the observations and the *a posteriori* model values, and RMSE as
494 summarized in Table 2. While correlation coefficients and RMSE are only two of many
495 possibilities to quantitatively describe how well the observations can be fitted by the model using
496 the inverted vertical emission profile, they provide a simple means to compare and rank the

various simulations. Notice that the sum of squared errors is also the largest term in the cost function used for the inversion. When using the AIRS data, the correlation is lower for the inversions using the whole AIRS satellite data set (values in brackets in Table 2) compared to inversions using only the 9 August AIRS overpass. Therefore, for AIRS we chose to use only the one overpass for the remainder of this study.

The bold values in Table 2 indicate the three eruption times for which each meteorological data set yielded the highest correlations and lowest RMSE: ECMWF data for 22:01 UTC, GFS data for 01:50 UTC and 04:35 UTC, respectively. It can also be seen that correlation coefficients tend to be lower when using data from all three instruments at the same time. This can be explained by the biases in the satellite data, which deteriorate correlations. Nevertheless, we expect that inverted profiles are most reliable when all data are used. Figure 5 shows the three best estimates of the inversion profiles based on all satellite data for each eruption time, 22:01 UTC (red line) using ECMWF data, and 01:50 UTC and 04:35 UTC using GFS data (green line and blue line, respectively). While the shape and magnitude of the strong stratospheric peak (~ 12 km) is very similar for all inversion experiments, the altitude of the tropospheric peak depends on the assumed eruption time. Overall, however, the emission profile is quite robust and does not depend strongly on the assumed eruption time. It also does not depend strongly on the choice of the meteorological input data used for driving FLEXPART. The total mass of SO_2 is $1.7 \pm 0.08 \text{ Tg}$ for all profiles, with $1 \pm 0.11 \text{ Tg}$ stratospheric injection ($> 10 \text{ km}$) and emission up to a maximum altitude of $\sim 20 \text{ km}$.

In principle, we could set up the inversion such that the emissions are not only determined as a function of altitude but also of time. However, since the three eruptions occurred during such a short time interval and the inversion results are very similar, the emissions of the three eruptions cannot be clearly separated by the inversion. Therefore, we chose the two profiles with highest correlation, the “ALL 22:01 ECMWF” and “ALL 01:50 GFS”, to define the average of these two profiles as the so-called “reference” profile (thick black line in Fig. 5). This profile was subsequently used to perform a long-range transport simulation by assigning the SO₂ emissions to a time window from the first to the second eruption time.

In Fig. 6, results from some sensitivity experiments are shown. All profiles are for an assumed 01:50 UTC eruption time. The 01:50 UTC profile (thick green line) is the same as the result in Fig. 5, repeated for comparison. The 01:50 UTC constant profile (blue line) shows the inversion profile using a constant *a priori* in contrast to an *a priori* based on IASI estimates. The similarity between these two profiles demonstrates that with a sufficiently large satellite data set the inversion results are robust to changes in the *a priori*, as stated also by Eckhardt *et al.* [2008]. The 01:50 UTC ECMWF profile (turquoise line) is the inversion result when using ECMWF instead of GFS meteorological data for driving the FLEXPART simulations used for the inversion, which result in somewhat lower correlation (0.60 vs. 0.62) for this eruption time. The lower altitude emission peak is located higher than for the GFS results, which is generally the case for the ECMWF results for all eruption times.

The figure also shows the ECMWF temperature profile (dark grey line) for the nearest grid point (52°N, 176°W) to the volcano, as well as the ECMWF tropopause height (light grey line) located

at 10 km. There are no emissions at the tropopause height. The high stratospheric emission peak is collocated with a layer of enhanced stability in the atmospheric temperature profile, which is associated with detrainment of air. In the troposphere, except for the lowest 2 km, there is no layer with particularly large stability, so there does not seem to be a height where detrainment is most likely to occur.

6.3. Simulation and validation of the SO₂ transport

The transport of the volcanic SO₂ plume was simulated with FLEXPART using emissions according to the reference inversion profile shown in Fig. 5. Particles were released continuously from 22:01 UTC on 7 August until 01:50 UTC on 8 August because the results presented in section 6.2 did not allow unambiguous determination of a single most appropriate time. This transport simulation was compared with independent satellite data; that is, measurements which were not used for the inversion. Comparisons with lidar measurements were also performed to evaluate the height of the simulated SO₂.

The long-range transport simulations were performed using both ECMWF data and GFS data. Comparisons and validations showed better agreement when using ECMWF data for the simulation, thus only the results using ECMWF data are shown in this section. The results using GFS data are only described where they clearly differ from the ECMWF results.

6.3.1. Comparison with independent satellite data

Figure 7 shows the FLEXPART simulation using the reference emission profile from Fig. 5 compared with independent satellite data from AIRS on 11 August, OMI on 12 August and

GOME-2 on 13 August. The model results are shown as isolines, while the satellite data are in color shadings. To give a best comparison between the model results and satellite data, the FLEXPART results are weighted with the respective averaging kernel from Fig. 2.

On 11 August, four days after the eruption, the SO₂ cloud hit the coast of Alaska and the plume was split into two parts. One part was transported across northern Canada towards Greenland and the other part spread towards the southern Great Lakes. It was the efficient transport near the tropopause (~12km) by the jet stream that caused the fast movement of the plume across North America. An AIRS satellite overpass at 22:05 UTC captured one part of the SO₂ cloud, with the swath width boundaries of the overpass indicated with the grey box (Fig. 7, top panel). For areas covered by the AIRS observations there is very good agreement between the model simulation and the measurements. The shape of the plume is especially simulated very well with a distinct sharp bend at the plumes southern end, and the tails stretching northward and southward.

On the next day, 12 August, the main part of the SO₂ plume has drifted northeastwards and is located over western Canada. The front tail of the plume is transported by the jet stream towards Greenland. The OMI satellite observations are composites of data collected for various moments during the day, while the FLEXPART results show the dispersed SO₂ at 21:01-22:01 UTC. Despite the time differences there is good agreement between measurements and FLEXPART simulation. The shape of the main part of the plume as well as the southern tail over the Pacific Ocean is captured very well, while there are some observations near Hudson Bay in Canada that are not simulated as well by FLEXPART. However, the model simulation using GFS data shows a better comparison for the areas around Hudson Bay (not shown).

588

589 Six days after the eruption on 13 August, the front tail of the SO₂ cloud hit the Atlantic Ocean,
590 while the main part is found over northern Canada. The GOME-2 observations, shown as
591 composites of overpasses during the day and the FLEXPART results for 16:01-17:01 UTC are in
592 good agreement. The main features of the plume are captured very well by the model. Especially
593 the position of the maximum over Canada correlates very well with the measurements. The two
594 tails of the plume stretching over U.S and Canada, and also the tail remaining over the Pacific
595 Ocean have distinct limits that the model recaptures. However, it seems that the model
596 overestimates the leading tail of the plume over Greenland, and also the westernmost part of the
597 plume over Alaska.

598

599 Some of the minor discrepancies between the model and satellite data may be due to that SO₂
600 loss is only estimated by FLEXPART. The e-folding time for the loss of SO₂ in the model
601 simulation is about 1 day in the boundary layer, about 20 days for the upper troposphere and 50
602 days for the stratosphere, which is in agreement with loss rates found in literature [e.g., *Bluth et*
603 *al.*, 1997]. Thus, the loss of tropospheric SO₂ is to some extent important for validation about a
604 week after the eruption, whereas stratospheric loss is very slow and nearly negligible.

605

6.3.2. Comparison with space-based lidar measurements

CALIPSO profiles of total attenuated backscatter at 532 nm and 1064 nm (level 1B data) are compared with SO₂ concentrations simulated by FLEXPART to evaluate the altitude of the simulated plume. The comparison is qualitative as we compare two different quantities: concentration of SO₂ with backscatter from particulate matter (aerosols and clouds).

The comparisons between the model simulation and CALIPSO were done in an area where the volcanic plume was observed by other satellite instruments (see Fig. 1 and Fig. 3) and where we can be confident that the scattering particles are indeed of volcanic origin. In addition, at this latitude some of the altitudes used for comparison (above 10-12 km) are seldom reached by other type of aerosols or liquid water clouds, but there may be ice clouds.

Figure 8 shows the SO₂ plume simulated by FLEXPART on 8 August (~15 h after the eruption) with the CALIPSO nadir track overlaid (upper panel). The simulated transport patterns agree very well with the satellite observations in Fig. 1, which were used for the inversion. Layers of enhanced attenuated backscatter are found between 5 km and 11 km (lower panel), while the plume simulated by FLEXPART shows two SO₂ layers centered at 6-8 and 11-12 km, coinciding with the two emission maxima of the reference profile (Fig. 5). Generally the simulated plume is broader than the CALIPSO features.

The lowest part of the simulated plume (5-9 km) coincides very well with the CALIPSO measurements, and especially the latitudinal tilting agrees very well. However, the CALIPSO Level 2 data product classifies this area as clouds with some minor aerosol near 5 km. The

conversion from SO₂ to sulphate is on the order of a few days in the lower troposphere, which may indicate that, at this early stage after the eruption, CALIPSO sees volcanic ash, or possibly a mixture of ash, sulphate and cloud. Also the attenuated color ratio (1064nm/532nm) is high (1.4-1.6) for this part of the plume, indicating large particles. As the volcanic ash and SO₂ traveled together for at least 3 days (*Prata et al. [2009]*), the comparison with the CALIPSO features seems reasonable.

For the tropopause region (~10 km), layers with enhanced backscatter are found mainly around 10 km, while the simulated plume is located at 11-12 km. CALIPSO's scene classification imply mostly clouds, the minor 11-12 km feature between 49 and 52°N is classified as "stratospheric feature". This feature shows a stronger signal at 532 nm, indicating smaller particles, thus may be small sulphate particles starting to form from the SO₂. The dislocation between the observed 10 km layer and the simulated 12 km layer may be explained by the very slow conversion rate from SO₂ to sulfate in the stratosphere, thus sulfate particles have not yet started to form. Or, if the observed features at 10 km are volcanic ash particles, they may have subsided due to gravitational settling. The depolarization ratio for the observations is 0.2 - 0.4. Interestingly, the cirrus cloud (strong backscatter, higher depolarization of 0.4-0.5) at ~10 km and 54°N, is not part of the simulated volcanic plume.

Figure 9 shows a similar comparison of the plume transport simulated by FLEXPART and the CALIPSO measurements from 9 August (~48 h after the eruption). Visually the transport patterns agree with the satellite observations in Fig. 3, also used for the inversion. The CALIPSO track cuts through the plume's tail at around 162 °W. The enhanced backscatter at 1064 nm is

shown as some of the observed features were more clearly visible at this wavelength rather than at 532 nm. Three thin veils of enhanced backscatter are observed between 43-47°N at ~3 km, ~12 km and ~15 km altitude. The FLEXPART model results show similar layers centered at the same altitudes, but the highest layer is covering a broader vertical range, the middle layer is narrower and the lowest layer is broader and extending further north. For the lowest layer it is the bottom part of the maximum that corresponds to the CALIPSO feature. The two highest CALIPSO layers are characterized as stratospheric features, while the lowest layer is a mixture of aerosol and cloud. The stratospheric layer has depolarization ratio around 0.1-0.2 and color ratio <1 , indicating a potential mixture of sulphate aerosols and other volcanic debris. Both the depolarization ratio and the color ratio are highest for the layer in the lower troposphere, indicating larger particles, thus maybe volcanic ash. The larger extent of the SO₂ layer compared to the area with enhanced backscatter can be due to wash out of the sulfate particles and ash at this low altitude. Overall, the approximate plume position and especially the three-layer structure and the three layers' mean altitudes are well captured.

6.3.3. Comparison with ground-based lidar measurements

To further validate the height of the simulated plume, we used ground-based lidar measurements at two different locations. These lidar observations were taken from 8 to 25 days after the eruption, on a location over 100° east of the volcano. Since the ash from the eruption was likely deposited after a few days, the observations that can be related to the eruption are of sulphate aerosols converted from the SO₂ emissions.

The Kasatochi plume was observed by the Dalhousie Raman lidar at Nova Scotia (44.6°N, 63.6°W) on the eastern coast of Canada. The measurements of the plume were available from 14 August 2008 on certain days until the end of October.

Fig. 10 shows the FLEXPART SO₂ plume on 18 August and lidar measurements from 18-19 August with corresponding FLEXPART isolines overlaid. The lidar position is marked with a green dot. The SO₂ plume is found mostly over Northern U.S., Canada, over western Alaska and over Greenland, and there is also debris over Nova Scotia. The aerosol extinction coefficients indicate an aerosol layer at ~14-15 km altitude, which corresponds very well with the SO₂ layer simulated by FLEXPART, but the measured aerosol plume is narrower in its vertical extent than the simulated SO₂ cloud. Also the maximum SO₂ concentration at around 03:00 UTC on 18 August is located slightly higher than the maximum aerosol concentration.

Fig. 11 shows the simulated SO₂ plume and lidar measurements from 21-22 August. The SO₂ plume is still visible over Nova Scotia, and an observed layer at ~18 km fits very well with the simulated plume to within ±0.5 km. This coincides with the minor emission peak at ~18km of

our reference emission height profile, and thus the lidar measurements provide validation that the emissions from Kasatochi reached at least 18-20 km altitude.

Observations of the Kasatochi plume were also performed using a ground based lidar at AWIPEV station, in Ny Ålesund (78.9°N, 11.9°E) on Svalbard. The lidar measurements of the Kasatochi plume were taken from 15 August 2008 to 24 September 2008. Several layers were observed at about 10-12 km and 15-17 km altitude [*Hoffmann et al.*, 2009].

Fig. 12 shows the simulated SO₂ plume and lidar measurements from 15 August with FLEXPART isolines overlaid. The SO₂ plume has stretched out from Alaska all the way to Europe. From the model simulation a thin tail of the plume has reached the lidar on Svalbard (green dot), and small amounts (0.5-2.0 $\mu\text{g m}^{-3}$) of SO₂ are found at an altitude of 8-10 km above Ny Ålesund. This is indicated in the lower panel and is in agreement with high aerosol backscatter coefficients at this altitude. The lidar observations also show an aerosol layer at ~11 km altitude which is not found in the model simulation. Only for the observations after 25 August, is this layer present in the model simulation, as shown in Fig. 13 for 1 September. For this day, there is also a very weak aerosol layer observed at 17 km which is also visible in the model simulation. The lidar measurements from 1 September have been examined in detail by *Hoffmann et al.* [2009].

Generally, the altitude of the simulated plume agrees very well with the different lidar observations, but the modeled plume is generally broader than the measured aerosol plume in its vertical extent.

7. Summary and conclusions

An inversion method was used in this study to estimate the vertical profile of SO₂ emissions from the eruption of Kasatochi Volcano in August 2008. This was done by using total column measurements of SO₂ from satellite instruments (GOME-2, OMI and AIRS) and a Lagrangian dispersion model, FLEXPART. Conclusions from this study are summarized as follows:

1. Emission height profiles of SO₂ were estimated by using SO₂ column data from GOME-2, OMI and AIRS for two days after the eruption. Two meteorological data sets (ECMWF and GFS) and three different eruption times were tested; 22:01 UTC on 7 August, 01:50 UTC and 04:35 UTC on 8 August. The first two eruption times yielded the highest correlation between measurements and model results. Generally, two large emission maxima were found; one in the stratosphere (~12 km a.g.l), and one in the middle-upper troposphere (~7km). The largest emission peak extended up to ~17 km which agreed with reports from AVO stating emissions up to 14.5-16.5 km a.s.l., but smaller emissions were obtained for up to ~20 km. According to the “reference” inversion (using satellite data from all three platforms), approximately 1.7±0.08 Tg SO₂ were emitted to the atmosphere, of which ~60% were injected above the tropopause located at 10 km. The estimated emission height profiles showed good agreement with height emission profiles from independent studies, such as estimates based on a trajectory ensemble technique [Maerker *et al.*, 2008], and also Theys *et al.* [2009].

2. The long-range dispersion of the SO₂ plume was simulated by FLEXPART using emissions according to our best-guess “reference” inversion profile. The plume spread mainly southeastward from the volcano and took on a circular shape due to a passing cyclone. The

plume was further transported towards the coast of Alaska where it split into two and traversed the North American continent in two "tails" before reaching the Atlantic Ocean and Europe within a week after the eruption. The simulated plume was compared to independent satellite data up to six days after the eruption. There was overall good agreement between the simulated plume and the observations.

3. The height of the simulated plume was evaluated in a qualitative manner using lidar measurements. Compared to CALIPSO measurements on 8 and 9 August, one and two days after the eruption, the height of the simulated plume agrees very well. In particular, three separate layers were identified at altitudes within ~1 km of the altitudes of the observed layers. Compared to observations from Nova Scotia 10-15 days after the eruption the height of the modeled plume agreed with the observations to within ~1 km, and the comparison also demonstrated that SO₂ was injected to an altitude of 18-20 km by the volcanic eruption. The model results also agreed with observations on Svalbard 8-25 days after the eruption.

Challenges and restrictions of this case study include the following:

The eruption of Kasatochi was characterized by three different eruption times and also subsequent continuous release, and there was no information on how much SO₂ was released during each eruption. The eruptions were not clearly separable by our method, thus we made the assumption that all SO₂ mass was emitted at once, using a time window between the best-fitting eruption times. Furthermore, the first satellite detection of the plume by AIRS, GOME-2 and OMI was about 16, 23, 25 hours after the first eruption, which makes it difficult to demonstrate a near-real time application for this case study.

760

761 The inversion method presented here can provide information needed in order to calculate the
762 actual and future position and extent of volcanic plumes. This information can be utilised in near
763 real-time applications by e.g., the VAACs to rapidly issue warnings on volcanic ash hazards. As
764 soon as satellite data are available for the eruption, the inversion method can be applied and the
765 results can be ready within minutes to a few hours. The method presented can also be utilised for
766 less time-critical studies, such as facilitating the understanding of the climatic impacts of
767 stratospheric SO₂.

768

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913

Satellite retrieval	Total mass SO ₂	Reference
GOME-2	~2.5 Tg	<i>Richter et al.</i> [2009a]
OMI	~1.4 Tg	<i>NASA</i> [2008]
AIRS	~1.2 Tg	<i>Prata</i> [2009] (this issue) This paper
IASI	~2.2 Tg	<i>Karagulian et al.</i> [2009]

914

915 **Table 1:** Estimates of total SO₂ mass emitted by the eruption of Kasatochi, for different satellite
916 retrievals.

917

Model Input data	Satellite data	ERUPTION TIMES					
		22:01 UTC		01:50 UTC		04:35 UTC	
		r	RMSE	r	RMSE	r	RMSE
ECMWF	GOME-2	0.65	2.72	0.62	2.94	0.59	3.09
	OMI	0.64	1.02	0.63	1.08	0.60	1.17
	AIRS	0.69 (0.31)	0.72 (0.96)	0.65 (0.28)	0.80 (1.01)	0.62 (0.21)	0.84 (1.08)
	ALL	0.62 (0.41)	1.93 (2.04)	0.60 (0.41)	2.07 (2.13)	0.56 (0.37)	2.22 (2.26)
GFS	GOME-2	0.61	2.82	0.69	2.74	0.67	2.97
	OMI	0.62	1.03	0.69	0.98	0.69	1.01
	AIRS	0.66 (0.42)	0.77 (0.91)	0.56 (0.32)	0.88 (0.99)	0.55 (0.30)	0.90 (1.04)
	ALL	0.57 (0.46)	1.98 (1.98)	0.62 (0.42)	1.99 (2.08)	0.60 (0.45)	2.07 (2.16)

919

920 **Table 2:** Summary of all inversions performed (using different meteorological input data,
921 different satellite data and three eruption times) and corresponding Pearson correlation
922 coefficients (r) between the observations and the *a posteriori* model values, and root mean
923 square errors (RMSE) given as E-03 kgm⁻². Values in brackets are indicating the inversions
924 using the whole AIRS satellite data set in contrast to using only one AIRS overpass on 9 August.
925 The bold values indicate the three eruption times for which each meteorological data set yielded
926 the highest correlations and lowest RMSE.

927

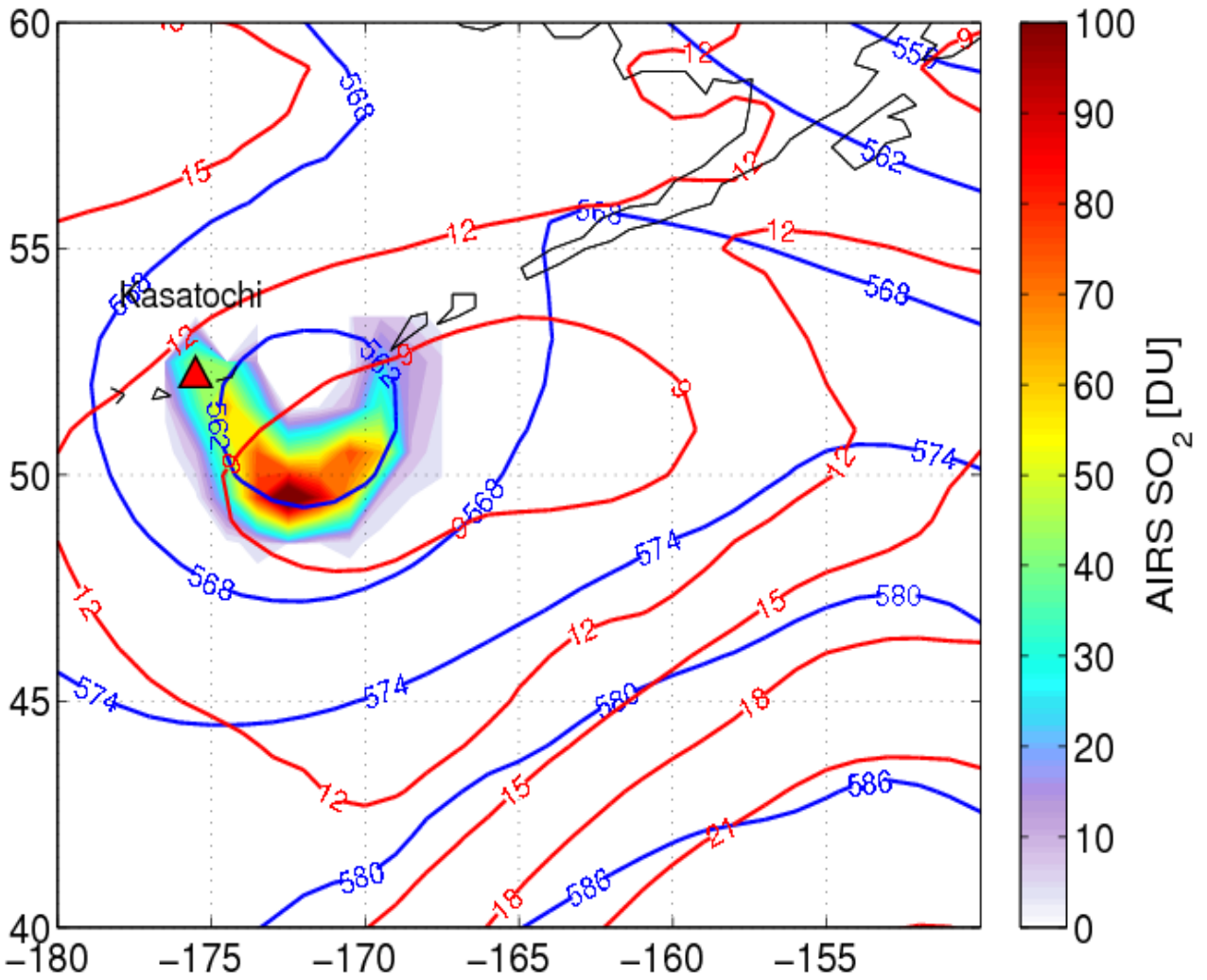
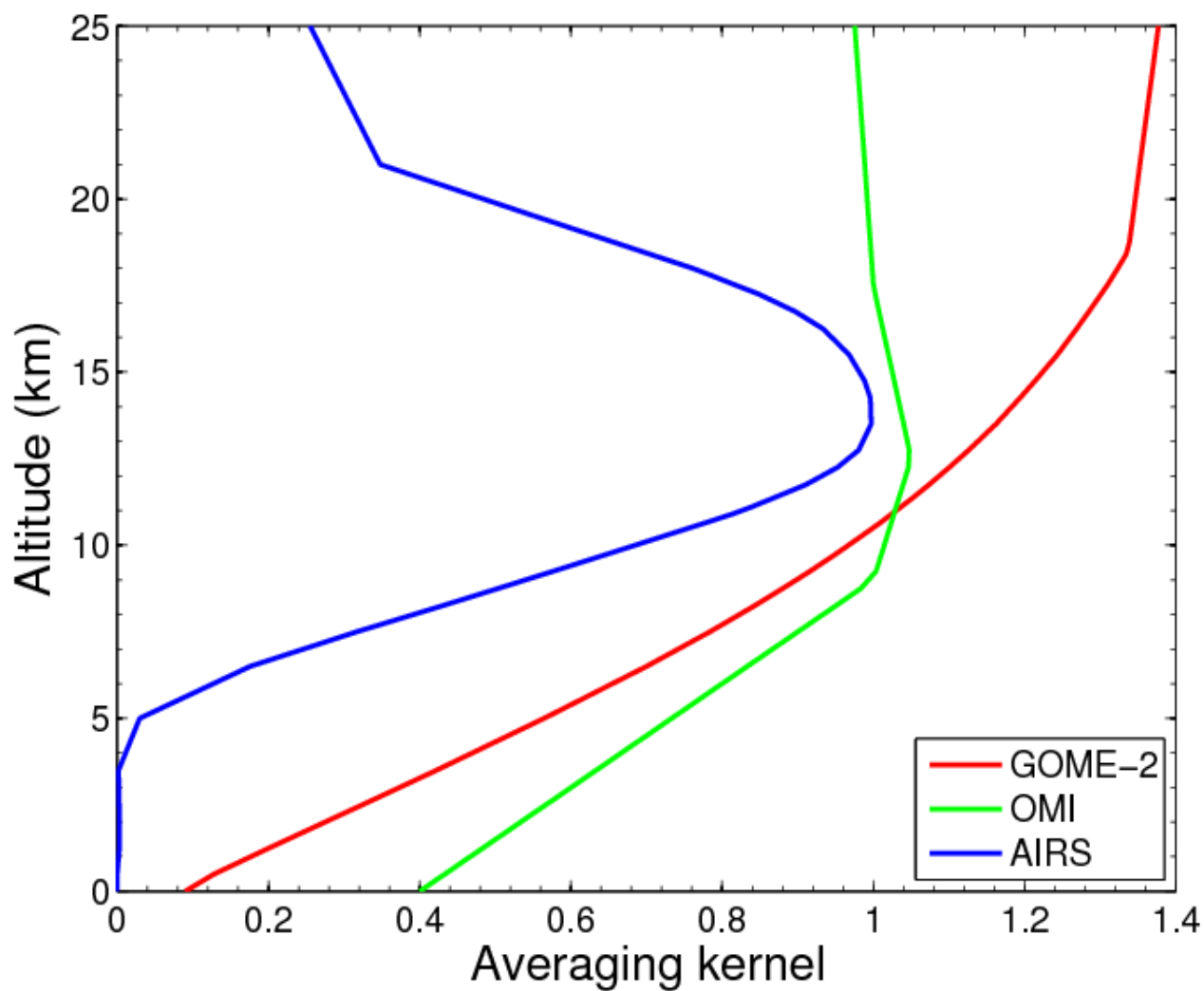


Figure 1: Geopotential height [10^1 m] in the area of the Kasatochi Volcano, on pressure levels 1000 hPa (red lines) and 500 hPa (blue lines) from the ECMWF analysis, on 8 August 2008 at 12:00 UTC. Satellite measurements of SO_2 total columns by AIRS on 8 Aug 13:41 UTC are shown in color shadings. The Kasatochi Volcano is marked by a red triangle.



933

934 **Figure 2:** Averaging kernels for the GOME-2, OMI and AIRS retrievals of SO₂.

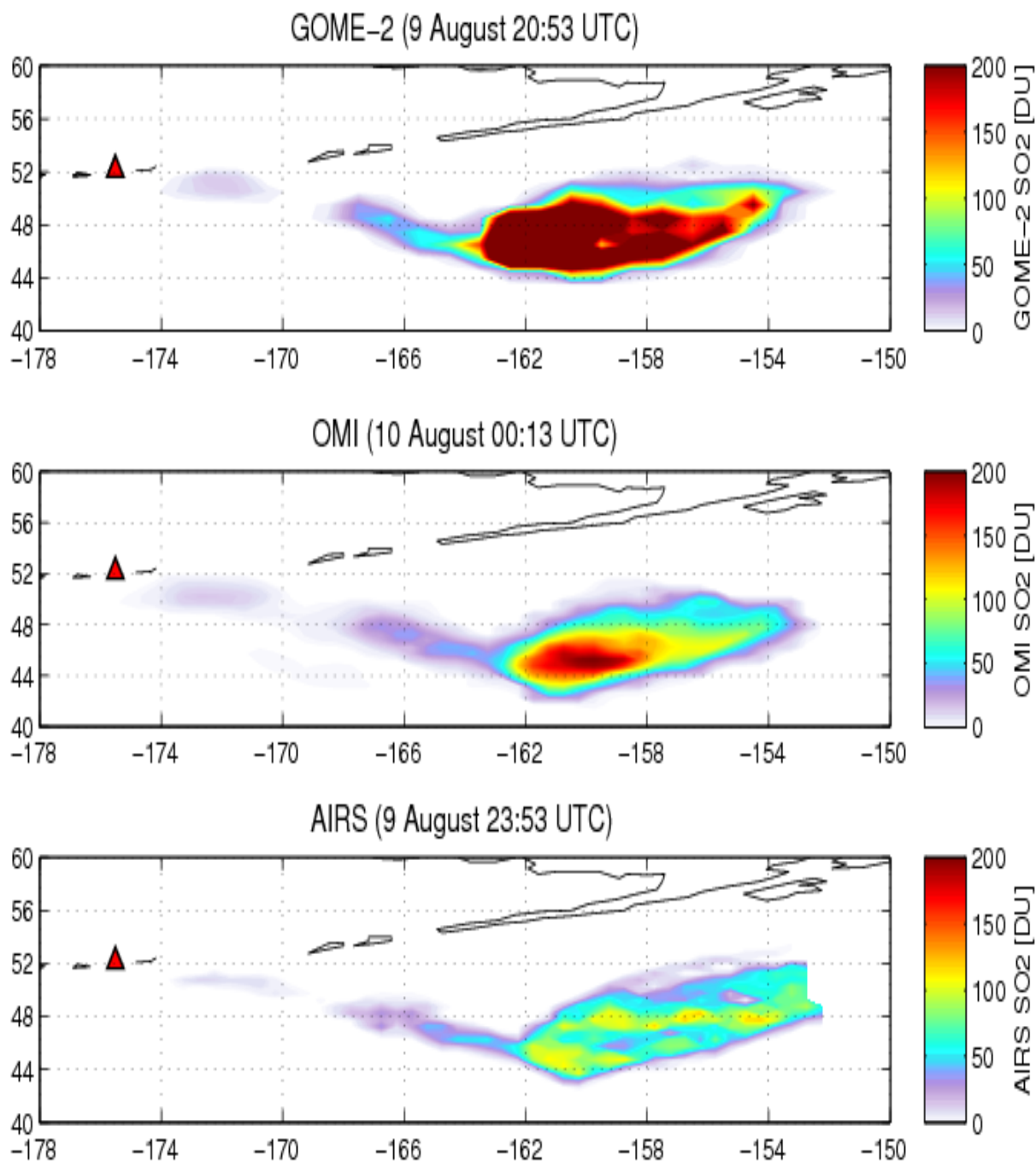
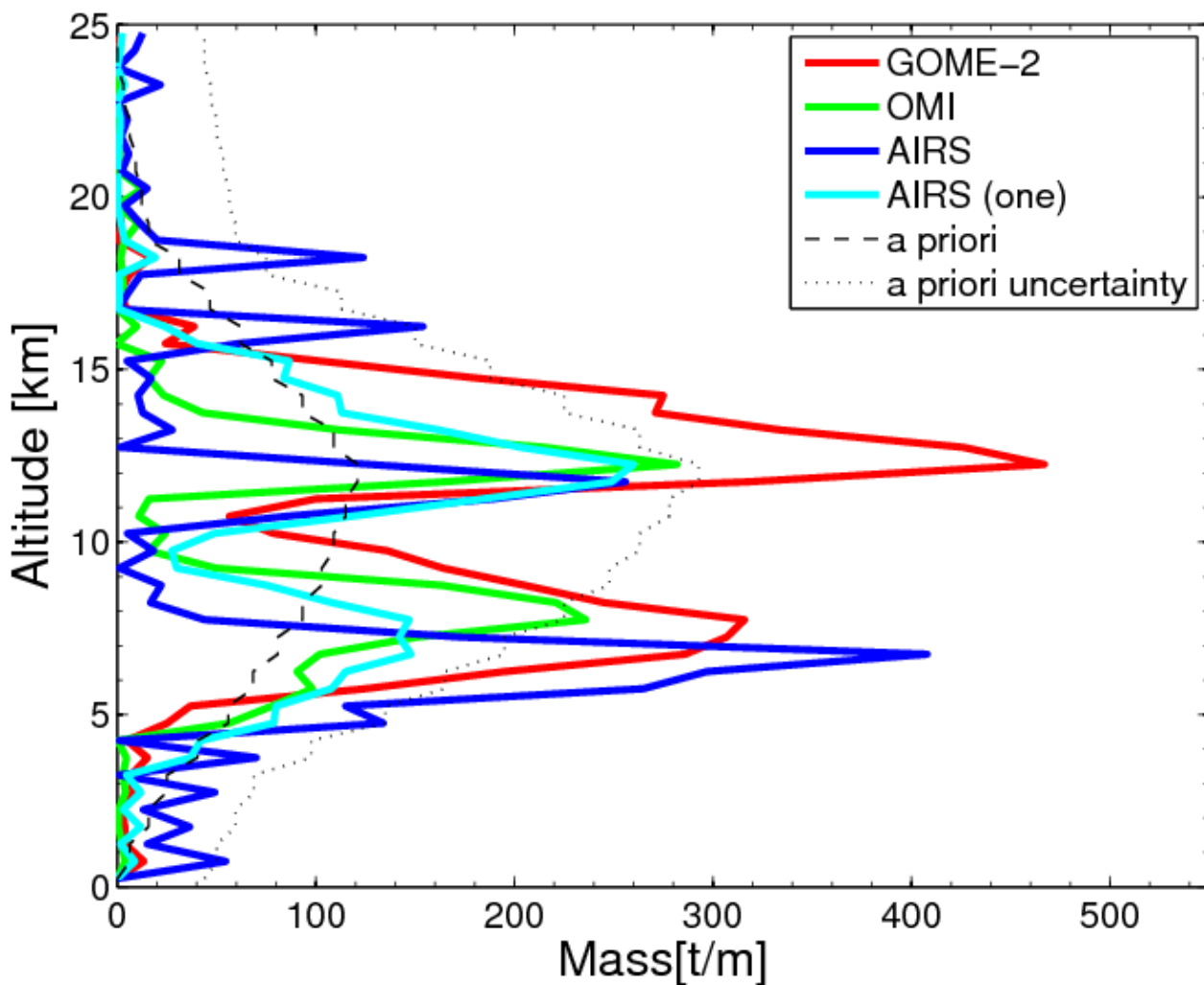


Figure 3: SO₂ columns retrieved from GOME-2, OMI and AIRS measurements on 9-10 August 2008. The Kasatochi Volcano is marked by a red triangle.



939

940 **Figure 4:** Inversion results for the 22:01 UTC assumed eruption time using satellite data from
 941 one instrument at the time; GOME-2 (red line), OMI (green line) and AIRS (blue line). The
 942 AIRS (one) profile is the inversion result when using only one AIRS satellite overpass on 9
 943 August at 23:53 UTC. ECMWF meteorological data were used for driving the FLEXPART
 944 simulations used for these inversions.

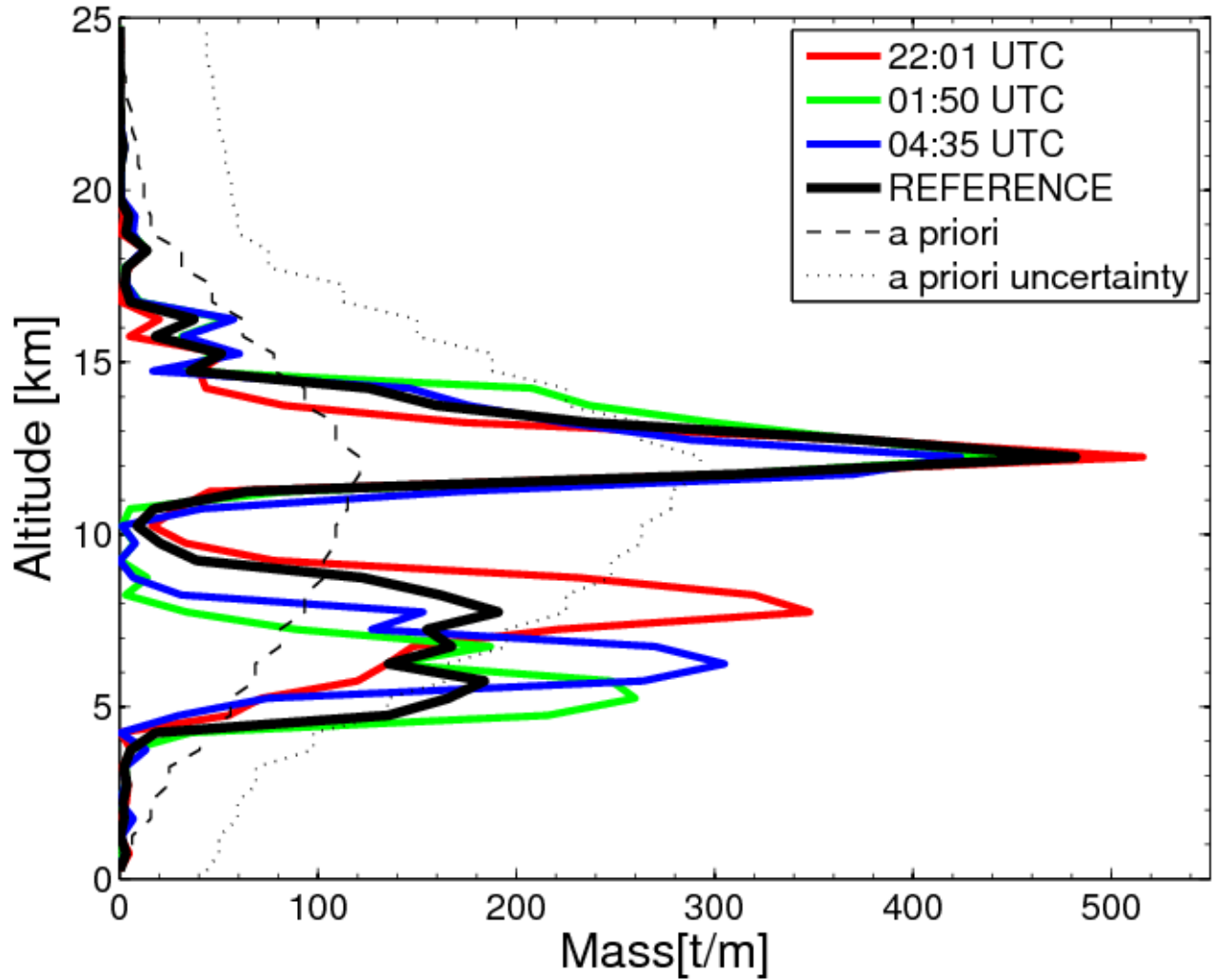


Figure 5: Inversion results when using combined satellite data from all three platforms (GOME-2, OMI and AIRS) for three different assumed eruption times: 22:01 UTC on 7 August (red line), 01:50 UTC (green line) and 04:35 UTC on 8 August (blue line). The reference profile (thick black line) is the average of the 22:01 UTC and the 01:50 UTC profiles. The ECMWF meteorological data set were used for driving the FLEXPART simulations used for the 22:01 UTC inversion, while for 01:50 UTC and 04:35 UTC the GFS data were used.

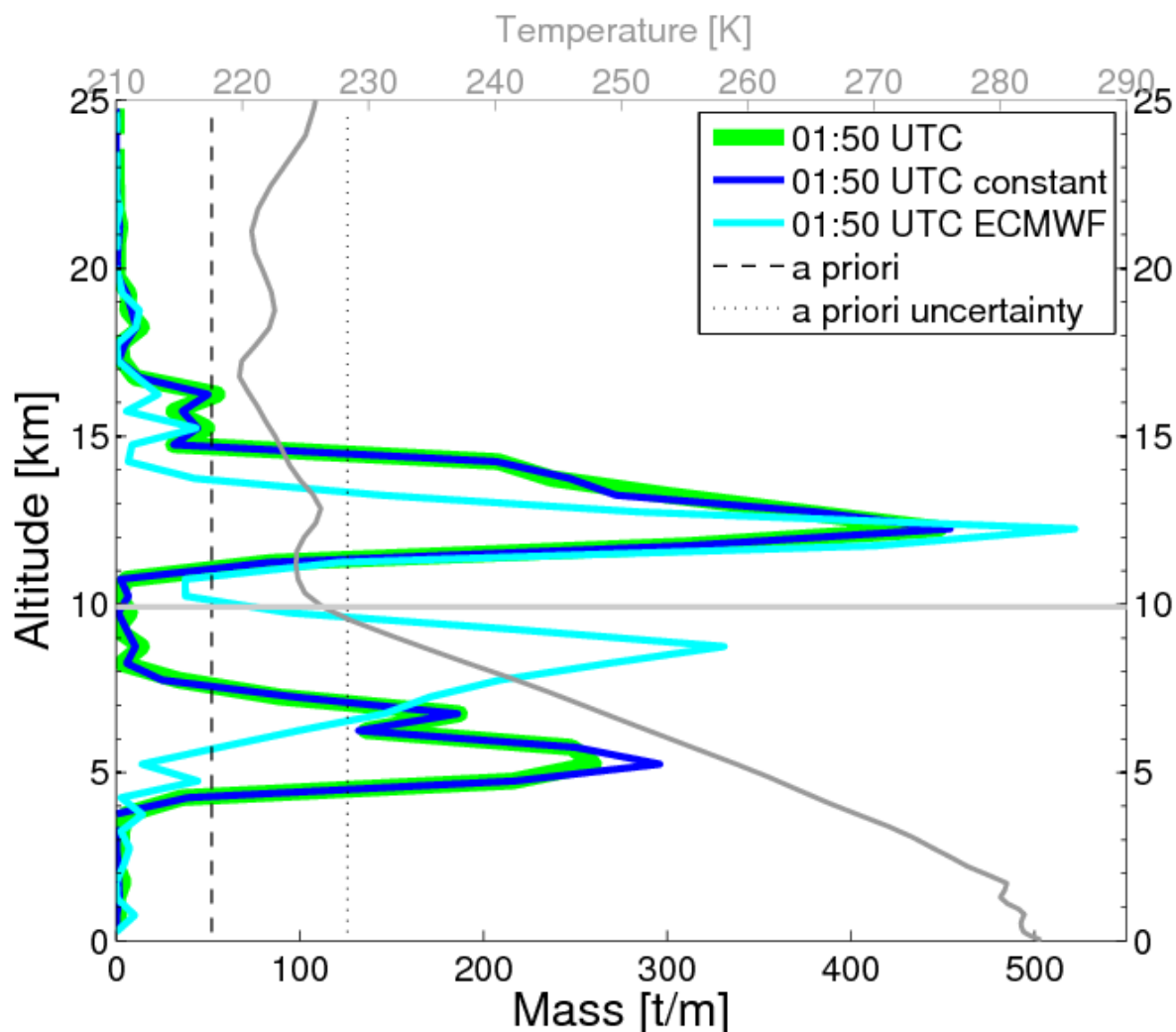


Figure 6: Sensitivity experiments with the inversion algorithm. The profile 01:50 UTC (green line) is the same result as shown in figure 5. The profile 01:50 UTC constant (blue line) is using constant *a priori* emissions (flat *a priori* profile). The profile 01:50 UTC ECMWF (turquoise line) is the inversion result when using ECMWF meteorological data for driving the FLEXPART simulations used for the inversion, instead of using GFS data. The dark grey line is the ECMWF temperature profile for (52°N, 176°W) at 00:00 UTC on 8 August. The tropopause diagnosed from ECMWF data is located at 10 km (light grey line).

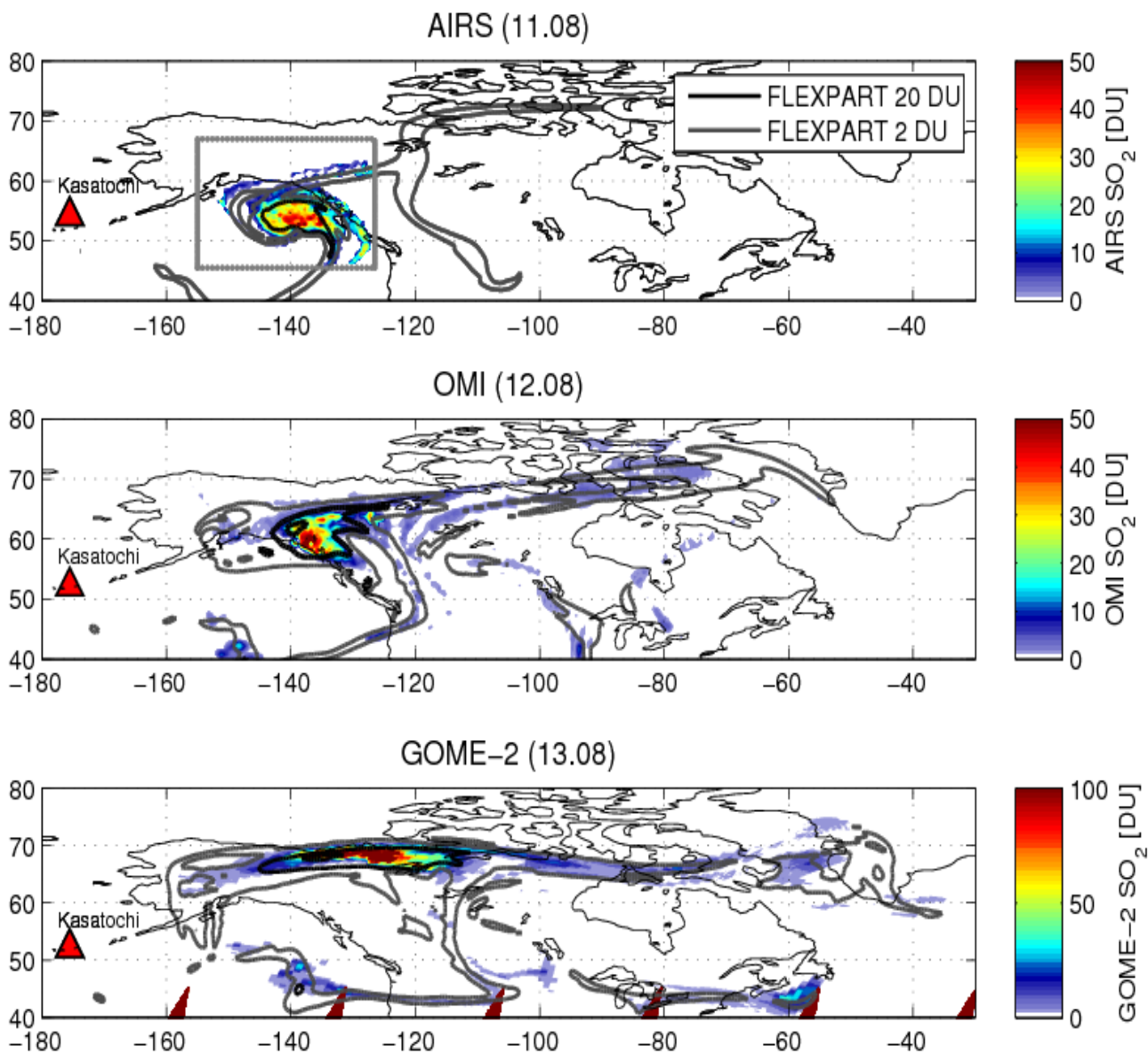


Figure 7: Comparison of SO₂ columns measured by satellite and simulated by FLEXPART using the emission profile from the reference inversion. Satellite data (AIRS for 11 August, OMI for 12 August and GOME-2 for 13 August 2008) are shown by the color shadings, and the FLEXPART results, driven with ECMWF data, are shown as isolines for 2 DU (thick grey line) and 20 DU (thick black line). For AIRS, the satellite's approximate swath width boundaries are shown by grey dotted lines. The Kasatochi Volcano is marked by a red triangle.

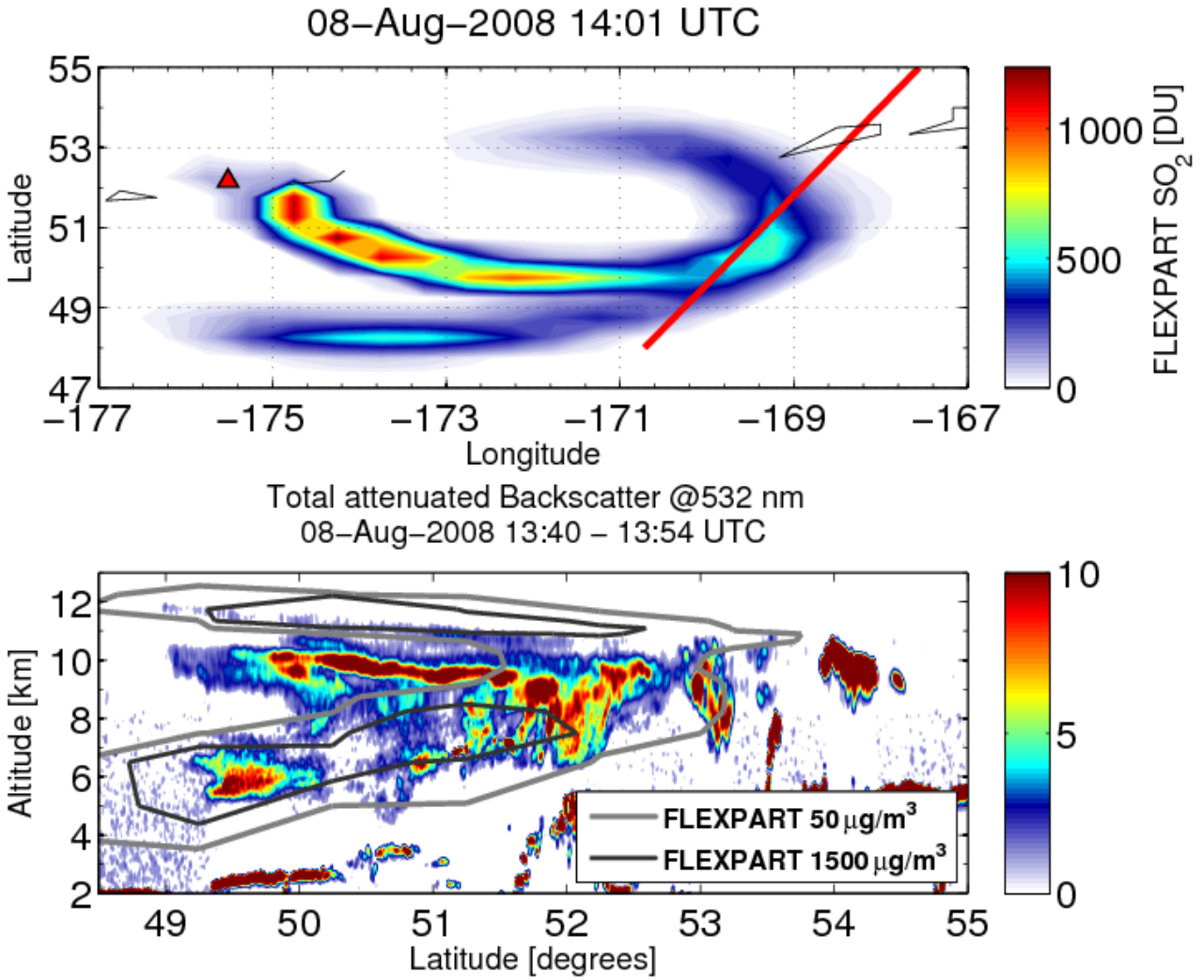
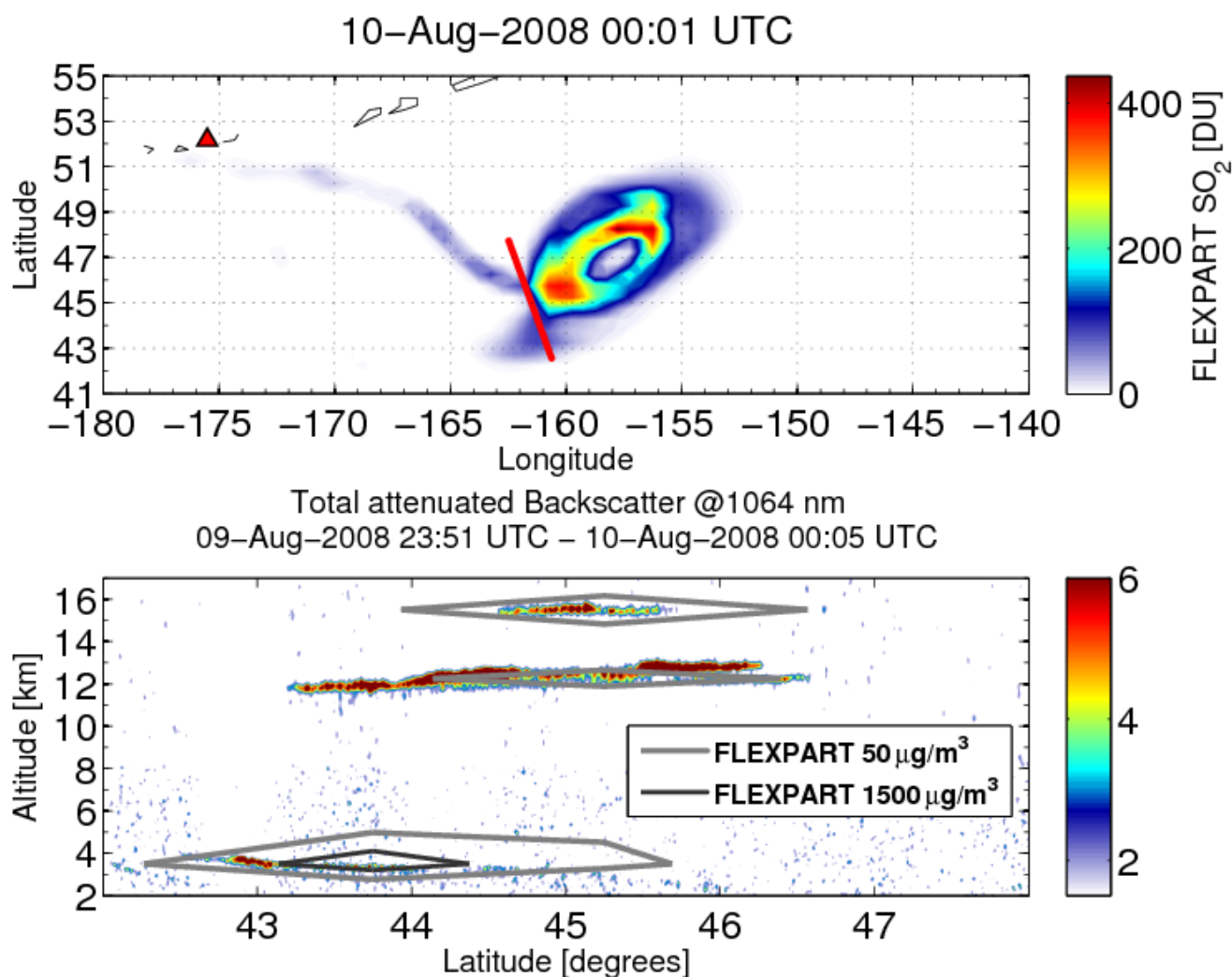


Figure 8: Comparison of CALIPSO attenuated backscatter at 532 nm with SO₂ concentrations simulated by FLEXPART on 8 August. The upper panel shows total columns of SO₂ simulated by FLEXPART. The red line indicates the location of the CALIPSO nadir track. In the lower panel, CALIPSO data are shown by the color shadings (in 10⁻³ /m sr) and the FLEXPART results are plotted as isolines for 50 μg m⁻³ (thick grey line) and 1500 μg m⁻³ (thick black line).



975

976 **Figure 9:** Comparison of CALIPSO attenuated backscatter at 1064 nm with SO₂ concentrations

977 simulated by FLEXPART on 9 August. The upper panel shows total columns of SO₂ simulated

978 by FLEXPART. The red line indicates the location of the CALIPSO nadir track. In the lower

979 panel, CALIPSO data are shown by the color shadings (in 10⁻³ /m sr) and the FLEXPART results

980 are plotted as isolines for 50 µg m⁻³ (thick grey line) and 1500 µg m⁻³ (thick black line).

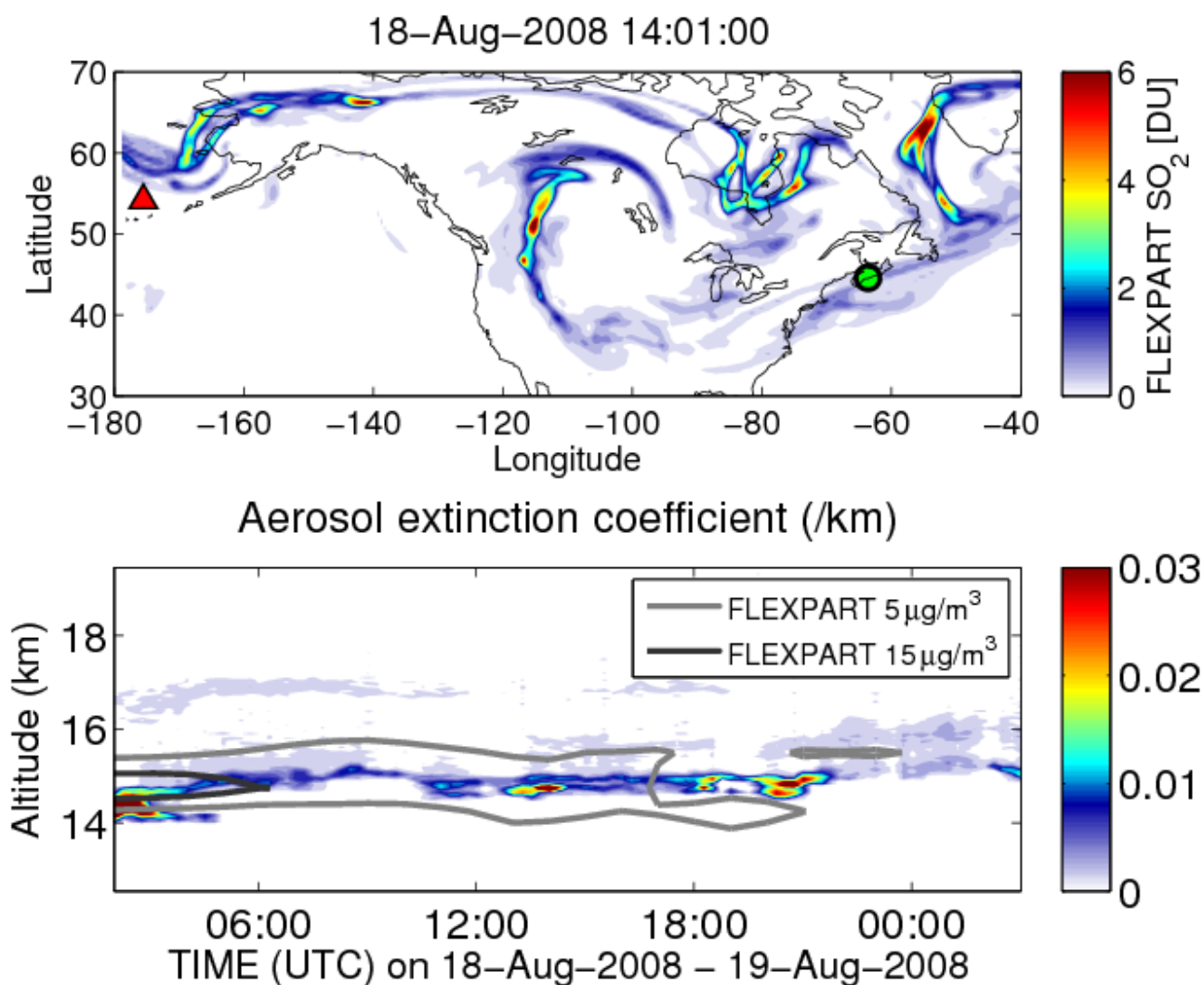
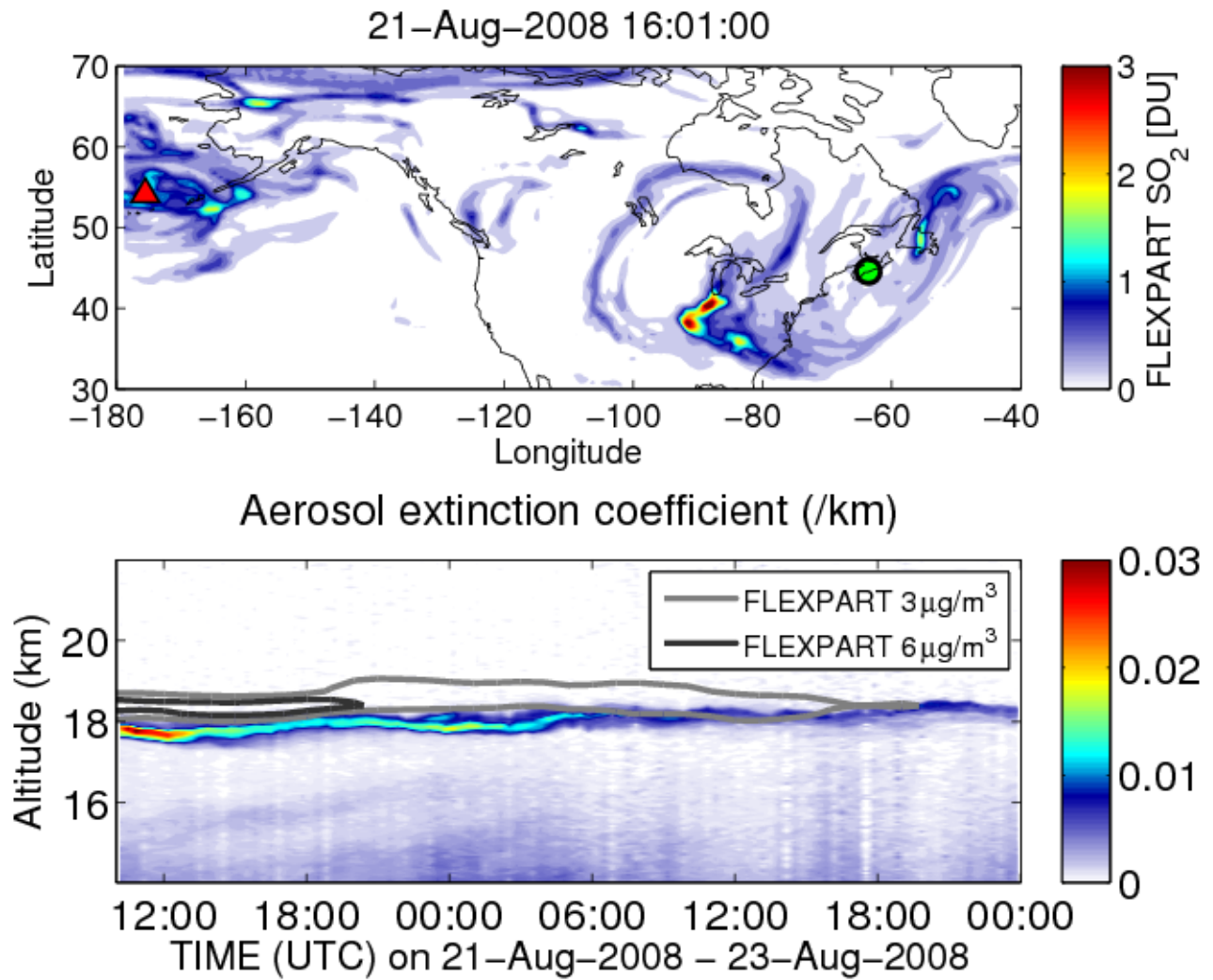


Figure 10: Comparison of aerosol extinction coefficients measured at Nova Scotia on 18-19 August and SO₂ concentrations simulated by FLEXPART. The upper panel shows total columns of SO₂ simulated by FLEXPART from 18 August. The lidar at Nova Scotia is marked with a green dot. In the lower panel, the lidar measurements are shown by the color shadings and the FLEXPART results are plotted as isolines for 5 µg m⁻³ (thick grey line) and 15 µg m⁻³ (thick black line).



988

989 **Figure 11:** Same as Fig. 10 but for 21-22 August. FLEXPART results are plotted as isolines for

990 3 $\mu\text{g m}^{-3}$ (thick grey line) and 6 $\mu\text{g m}^{-3}$ (thick black line).

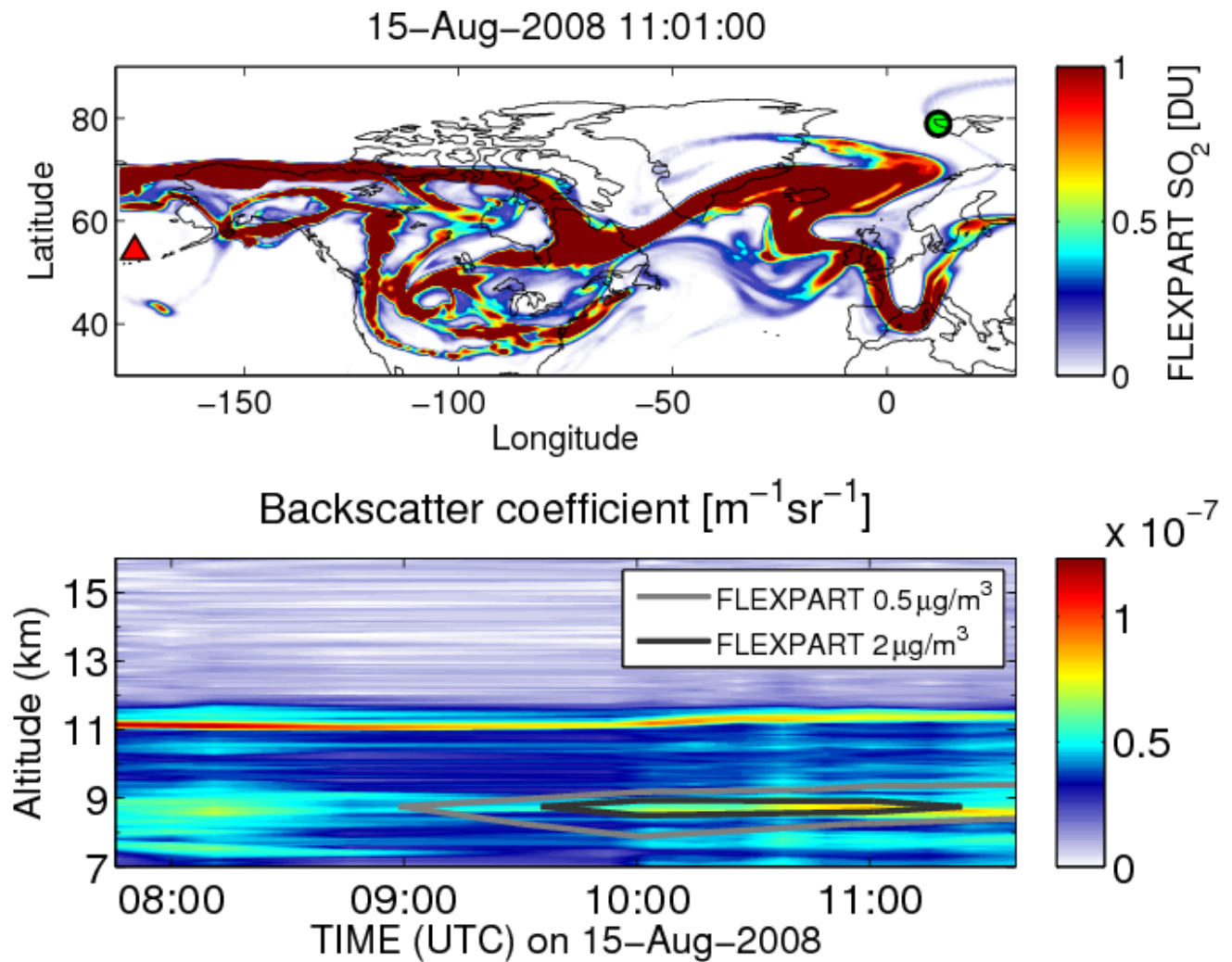


Figure 12: Comparison of aerosol backscatter coefficient measured at Ny Ålesund on 15 August and SO_2 concentrations simulated by FLEXPART. The upper panel shows total columns of SO_2 simulated by FLEXPART from 15 August. The lidar at Ny Ålesund is marked with a green dot. In the lower panel, the lidar measurements are shown by the color shadings and the FLEXPART results are plotted as isolines for $0.5\mu\text{g m}^{-3}$ (thick grey line) and $2\mu\text{g m}^{-3}$ (thick black line).

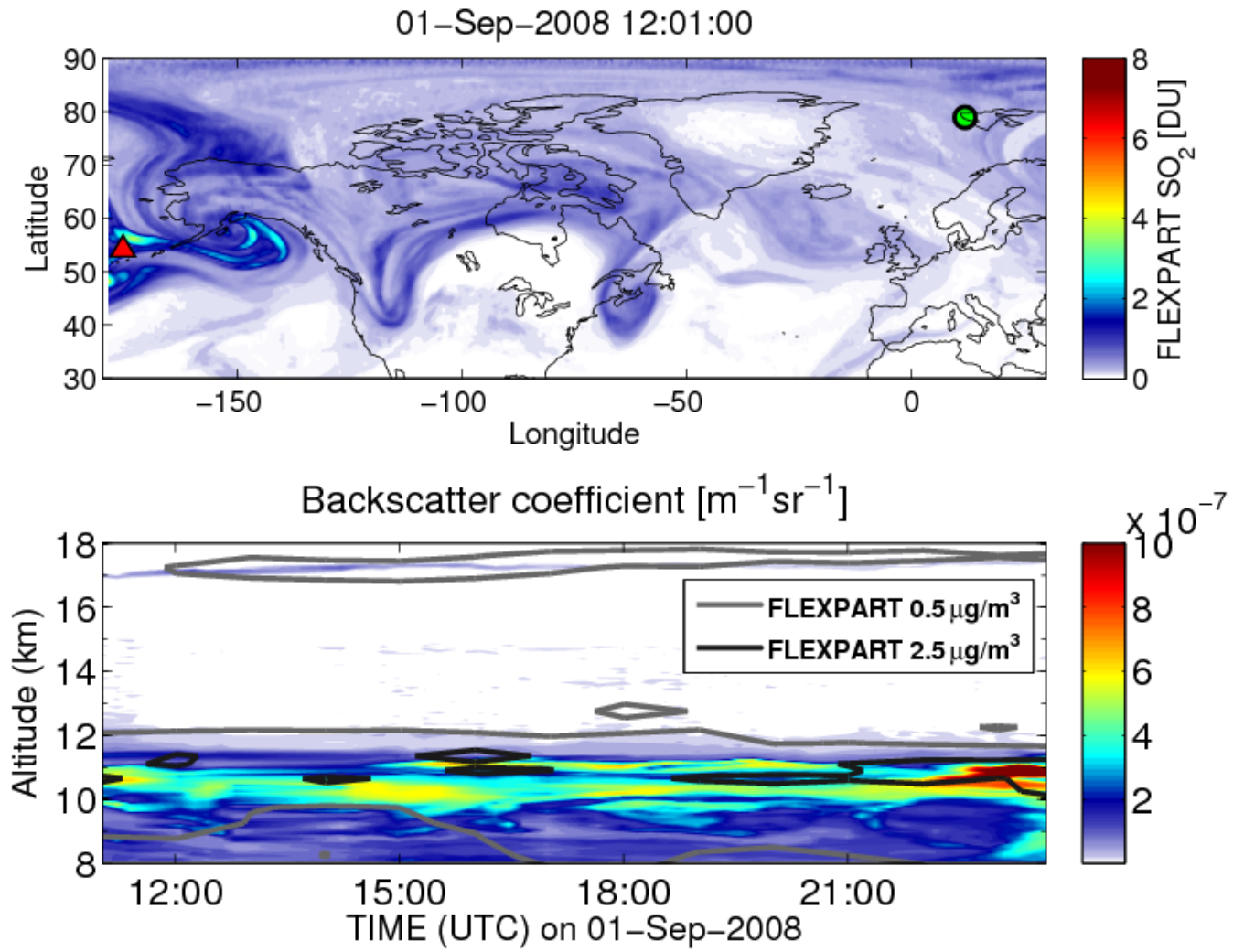


Figure 13: Same as Fig. 11 but for 1 September. The FLEXPART results are plotted as isolines for 0.5 µg m⁻³ (thick grey line) and 2 µg m⁻³ (thick black line).