Open book test. You can make use of a one page formulae sheet. Make reasonable assumptions where necessary. No clarifications to questions will be provided during the test. Spend some time thinking about the questions before you start answering. Write the answers clearly and legibly so that they can be graded.

1. A buck converter is operated as a solar charger for a battery as shown in Figure 1. The open circuit voltage is 14 V , the MPPT voltage of the solar panel is 8 V , and the battery voltage is 6 V . Power from the PV panel at MPPT condition is 30 W . The MOSFET $\left(S_{M}\right)$ has and resistance of $13 \mathrm{~m} \Omega$ and the diode characteristics is obtained by operation of MOSFET as a synchronous rectifier $\left(S_{D}\right)$ and has equivalent characteristics of $V_{d o n}=\left(0.1+13 m \Omega i_{d}\right) V$. The switching frequency is 280 kHz and the switching loss data for the MOSFET and Diode at $V_{d c}=13 V$ and $I_{o u t}=8.5 \mathrm{~A}$ is as follows: $E_{O N}=1 \mu J, E_{O F F}=0.3 \mu J$, and $E_{r r}=$ $0.17 \mu J$. Switching power loss exponent $k_{v}$ and $k_{i}=1$, and the $T_{a m b}=60^{\circ} \mathrm{C}$. Also, assume all the other passive components are ideal.


Figure 1: Solar battery charger.
(a) What is the duty cycle required for the switch $S_{M}$ when the PV panel is charging the battery under MPPT conditions?
(2 points)
(b) What is the conduction loss and switching loss in $S_{M}$ and $S_{D}$ under MPPT conditions? What is the corresponding charging power?
(3 points)
(c) What is the maximum $R_{\theta(j a)}$ that the semiconductors can have so as to keep $T_{j}<$ $130^{\circ} \mathrm{C}$ ?
(d) What is the reduction in power loss that can be obtained by using two parallel MOSFETs for the switch $S_{M}$ ?
(e) What is the rms current in $C_{d c}$ neglecting ripple current in the inductors?
(f) The solar charger cost is Rs.1000/- and the cost of the MOSFET is Rs.25/- and is operated daily for 8hrs at MPPT conditions. Compare the EIC of using 1 or 2 parallel MOSFETs considering factors for initial cost and power loss. Assume that the interest rate is $10 \%$, cost of electricity is Rs. $7 / \mathrm{kWhr}$, and ten years of equipment operational life.
(2 points)


Figure 2: Thermal equivalent network.
2. The Foster network model of a thermal system is shown in Figure 2. Convert this to an equivalent Cauer network. Write the expressions for $P_{i}(s) / Q_{i}(s)$ for each stage of the transformation.
(6 points)
3. A designer would like to use electronic equipment that was designed for commercial environment in an automotive application. In the commercial environment, the equipment would experience a daily semiconductor junction cycle of $20^{\circ} \mathrm{C}$. In the automotive environment, the equipment would experience daily four semiconductor junction cycles $80^{\circ} \mathrm{C}$. Assume both components are exposed to similar average temperatures. The Coffin-Manson exponent for the semiconductor, $q=4$.
(a) What is the ratio of the cycles to failure $\left(N_{f}\right)$ for the commercial / automotive equipment due to thermal cycling.
(2 points)
(b) What is the ratio of the expected time to failure (MTTF) for the commercial / automotive equipment.

