

Crystal Growth



CDEEP
IIT Bombay

EE 669 L / Slide 1

1. Czochralski Technique (CZ)

2. Float-Zone Technique. (FZ)

i. CZ :— Most IC industries use CZ grown Crystal

Advantages: Large Diameter wafers

Simpler Process and easy to control

Impurity Conc.

Disadvantage: Contains many small amount of
Impurities like Carbon, Oxygen, Iron
etc

ii Float-Zone Technique



CDEEP
IIT Bombay

a) Costlier

(b) Large size wafers cannot be grown. EE 669 L 4 / Slide 2

(c) However it will ^{have} very high degree of uniformity of impurities of choice (Dopants).

(d) Highly pure silicon wafers with impurities like O, C & Fe etc absent

(e) Resistivities of the order of $10000 \text{ ohm}\cdot\text{cm}$ and even $20000 \text{ ohm}\cdot\text{cm}$ are possible. Compared to CZ crystals which can have high $100 \text{ }\Omega\cdot\text{cm}$ resistivity.



CDEEP
IIT Bombay

EE 669 L 4 / Slide 3

- 1 Doping — P as n type
- 2 Crystal Orientation $\langle 100 \rangle$
3. Resistivity $0.1 \text{ ohmcm} \rightarrow 0.1 \text{ to } 0.2 \text{ ohmcm}$
- 4 Dislocation Count : no of dislocations/cm²
EDP
- 5 radial resistivity variation.
- 6 & Thickness
- 7 Diameter $\pm \Delta D$



CDEEP
IIT Bombay

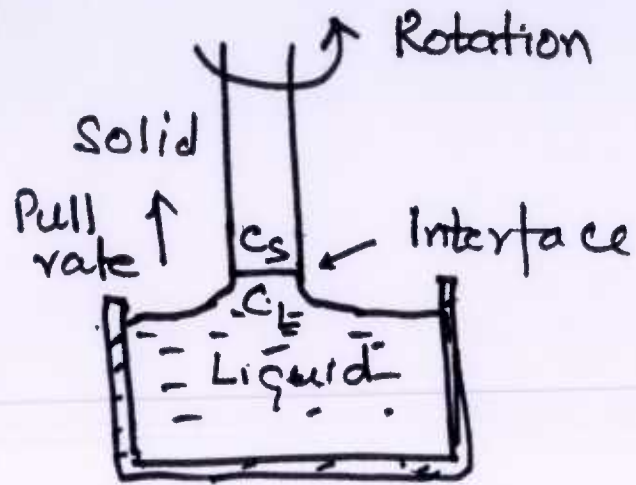
EE 669 L 4 / Slide 4

Modeling Dopant Behaviour During Crystal Growth - Mathematical Representation

1. Dopants are added to the Melt to provide controlled n or p doping conc. in the wafers.
- 2 As said earlier, the problem of modeling becomes difficult because of impurity segregation in melt and solid

Segregation Coeff. $k_0 = \frac{C_s}{C_L} = \frac{\text{Conc. of Solute (By wt) in Solid}}{\text{Conc. of Solute (By wt.) in Liquid}}$

CZ Process (cont.)



Crystals are pulled from the melt with certain Pull-rate and with spin rate of rotating Crystal.

The Impurities are added to the Melt by weight and during solidification gets into Lattice to form n or p Silicon.

Typical Dopants are

P-type :— Boron , Aluminum , Gallium , Indium

N-type :— Phosphorous , Arsenic (As), Antimony

Other Impurities :— Oxygen, Carbon, Bi, Li, and Au



CDEEP
IIT Bombay

EE 669 L 4 / Slide 5

Dopant/Impurity

B

Al

Ga

In

P

As

Sb

O

C

Li

Bi

Au

Segregation Coeff. K

0.8

2.8×10^{-3}

8×10^{-3}

3.6×10^{-4}

0.35

0.30

0.023

0.5

0.07

10^{-2}

7×10^{-4}

2.5×10^{-5}



CDEEP
IIT Bombay

EE 669 L 4 / Slide 6

If C_s = Conc. of Impurities in Solid surface (By wt)

& C_L = Conc. of Impurities in Liquid (Melt) (By wt.)

One defines segregation Coefficient k_0 as

$$k_0 = \frac{C_s}{C_L}$$

Rapid Stirring Case:

Let W_M = Initial Weight of Melt

C_M = Conc. of Solute in Melt (By Wt.)

During Crystal Growth, at any instant

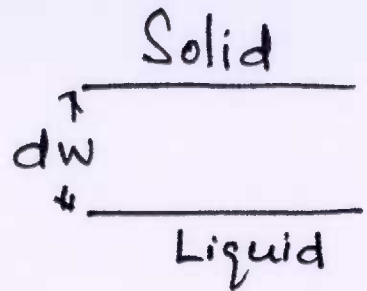
C_L = conc. of Solute in Liquid

C_s = conc. of Solute in Solid



CDEEP
IIT Bombay

One defines S as weight of Solute in Melt



Consider dw is wt. of an element of a Crystal of thickness $\rightarrow dw$



CDEEP
IIT Bombay

EE 669 L 4 / Slide 8

$\therefore$ Weight of Solute lost from melt $S = dS$

$$\therefore dS = -C_S dw$$

At this instant of time

$$\text{Wt. of Melt} = W_M - W$$

$$\therefore \text{Conc. } C_L = \frac{S}{W_M - W}$$

Please note that at initial time

$C_M = \text{Conc. of Solute in Melt}$

& $W_M = \text{Weight of Melt}$

$\therefore$ Weight of Solute at $t=0$

$$S_0 = C_M \cdot W_M$$

As $k_0 = \frac{C_S}{C_L}$, we have

~~$$dS = -C_S dw$$~~

$$dS = -C_S dw$$



$$\therefore ds = -k_0 C_L dw$$

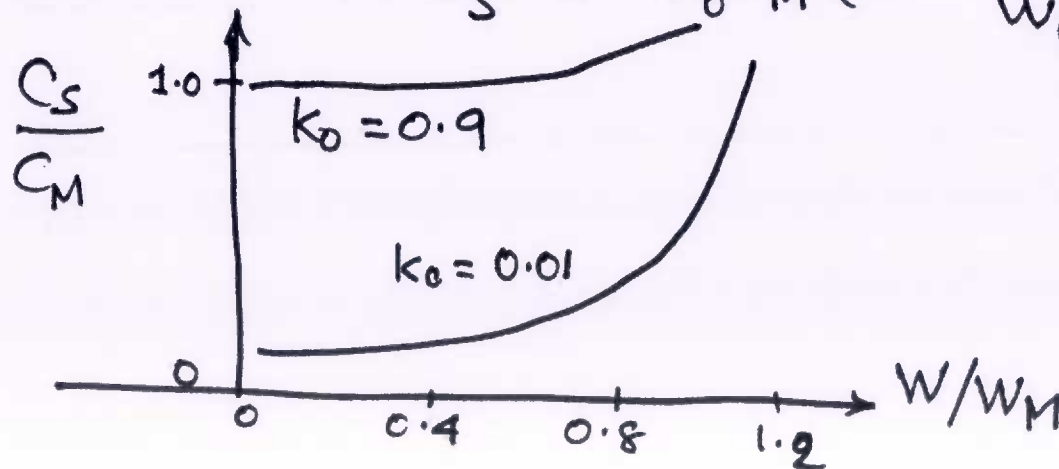
$$= -k_0 \frac{s}{w_M - w} \cdot dw$$

$$\text{or } \frac{ds}{s} = -k_0 \frac{dw}{w_M - w}$$

$$\therefore \int_{s_0}^s \frac{ds}{s} = -k_0 \int_0^w \frac{dw}{w_M - w}$$

$$\underline{s_0 = w_M C_M}$$

$$\therefore C_s = k_0 C_M \left(1 - \frac{w}{w_M}\right)^{k_0 - 1}$$



Partial - Stirring Cond's



CDEEP
IIT Bombay

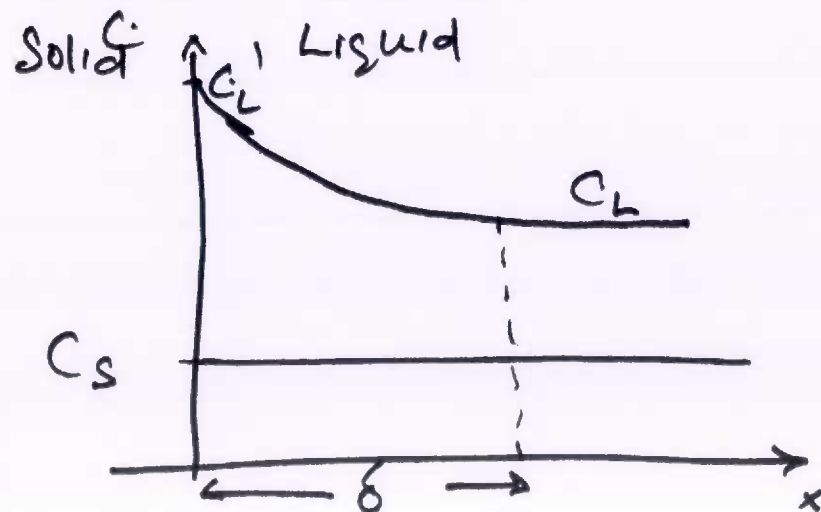
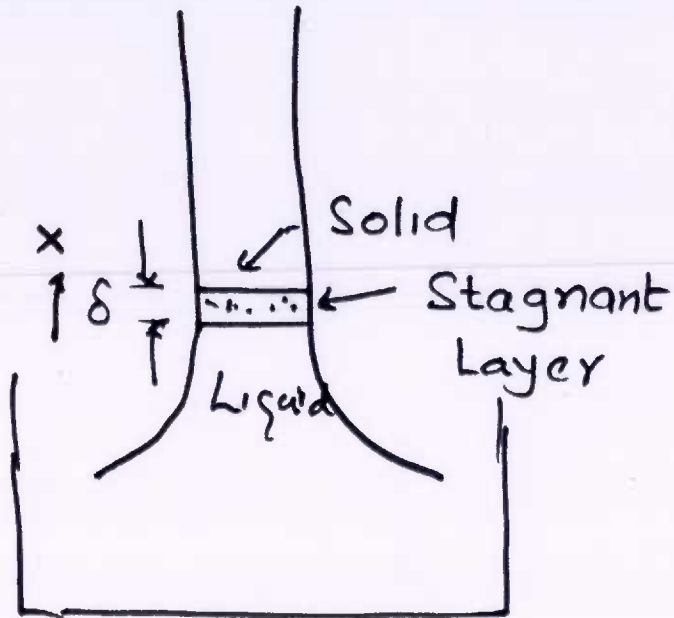
EE 669 L 4 / Slide 10

Slow Stirring creates a Stagnant Layer of thickness δ between Solid & Liquid.

The dopant diffuses through the Stagnant layer (δ) from Liquid into Solid.

Solving diffusion equation it can be shown that

effective Segregation Coeff- k_e is larger than k_0



If we pull the crystal, Solid-Liquid Interface also is pulled up by same pull rate.

If R = Growth Rate of Crystal

Δ D = Diffusion coefficient of Solute atoms

In the Liquid (Top portion of Melt)

Typically $D = 5 \times 10^{-5} \text{ cm}^2/\text{sec}$ for most impurities

Since impurities diffuse through the Stagnant Layer giving flux to Solid region. However during segregation process, solute is also rejected back to Liquid.

In equilibrium we can write

$$D \frac{d^2C}{dx^2} + R \frac{dC}{dx} = 0$$

Forward

Reverse



CDEEP
IIT Bombay

EE 669 L 4 / Slide 11

Solution of Diff. Eq is

$$C = A e^{-Rx/D} + B$$

$$\therefore \frac{dC}{dx} = -\frac{AR}{D} e^{-Rx/D}$$

Boundary Condⁿs : (i) $C = C_L'$ at $x=0$

$$(ii) \quad \left. \frac{dC}{dx} \right|_{x=0} = -\frac{R}{D} (C_L' - C_s)$$

The equivalent Foeff $K_e = \frac{C_s}{C_L}$ & $K_o = \frac{C_s}{C_L'}$



CDEEP
IIT Bombay

EE 669 L 4 / Slide 12

It is found that $k_e = C_s/C_L$ which is now

$$k_e = \frac{k_0}{k_0 + (1 - k_0)e^{-\frac{R\delta}{D}}} \quad \text{Here } k_0 = \frac{C_s}{C_L'}$$



EE 669 L 4 / Slide 13

where R = Rate of growth of Crystal

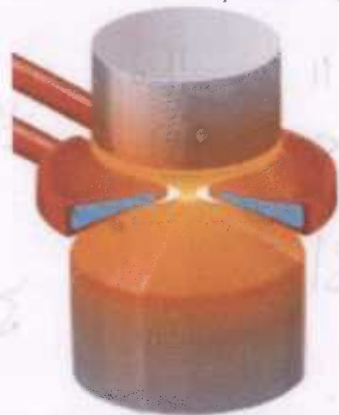
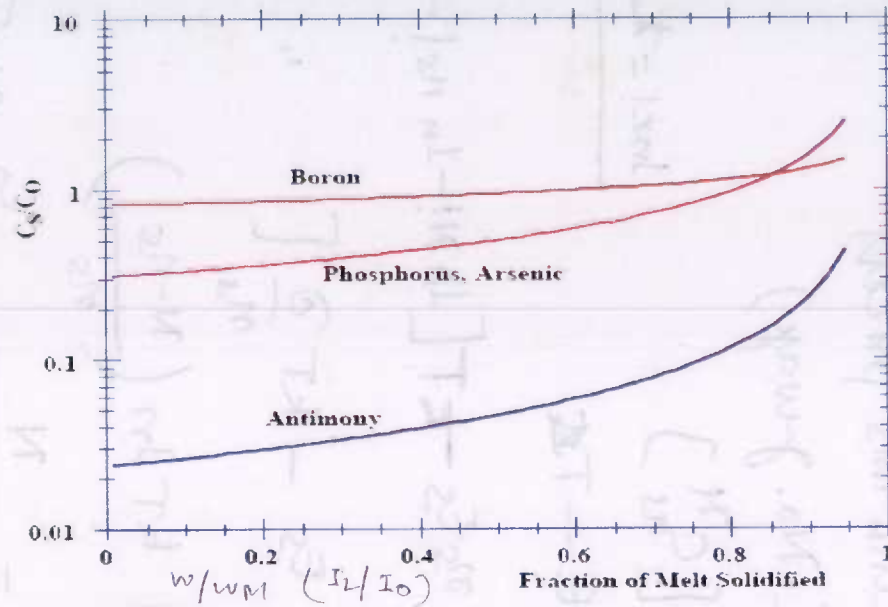
D = Diffusion Coeff of Impurities near
Liquid - Stagnant layer Interface.

Hence uniform of Doping in Crystal is Possible
if Pull rate R is High

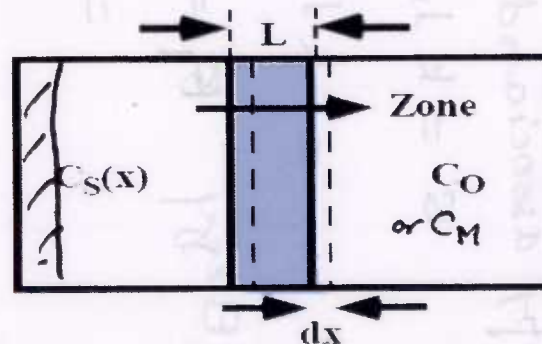
and Spin is Slow

$$\delta \propto \frac{1}{\text{Spin speed}}$$

Float Zone Process



(Left - Mitsubishi website at <http://www.egg.or.jp/MSIL/english/index-e.html>)



Zone leveling

$$C_S = k_e C_0 e^{-k_e x / L}$$

L - Molten zone length,

C_0 = doping conc in melt

$$C_S = \frac{k_e S}{A R L}$$

$$dS = C_M A P dx - \frac{k_e S}{L} dx$$

At equilibrium at $x=0$

~~dx=0~~

$$S = C_M A P L$$

$$\therefore S = \frac{C_M A P}{k_e}$$

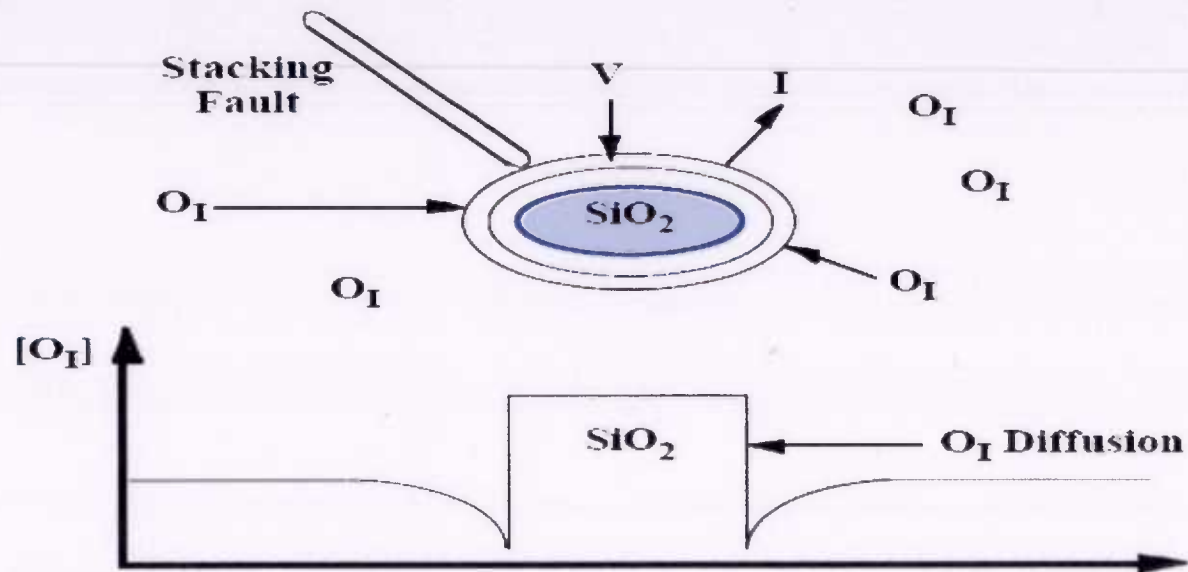
$$\times \left[1 - (1 - k_e) e^{-\frac{k_e x}{L}} \right]$$

$$C_S = C_M \left[\downarrow \right]$$

- In the float zone process, dopants and other impurities tend to stay in the liquid and therefore refining can be accomplished, especially with multiple passes.
- See the text for models of this process.

Oxygen and Carbon in CZ Silicon

- The CZ growth process inherently introduces O and C.
- Typically, $C_O \approx 10^{18} \text{ cm}^{-3}$ and $C_C \approx 10^{16} \text{ cm}^{-3}$.
- The O in CZ silicon often forms small SiO_2 precipitates in the Si crystal under normal processing conditions.



- O and these precipitates can actually be very useful.
 - Provide mechanical strength.
 - Internal gettering (described later in Chapter 4).