



m proteins



L = length of DNA

N : binding sites

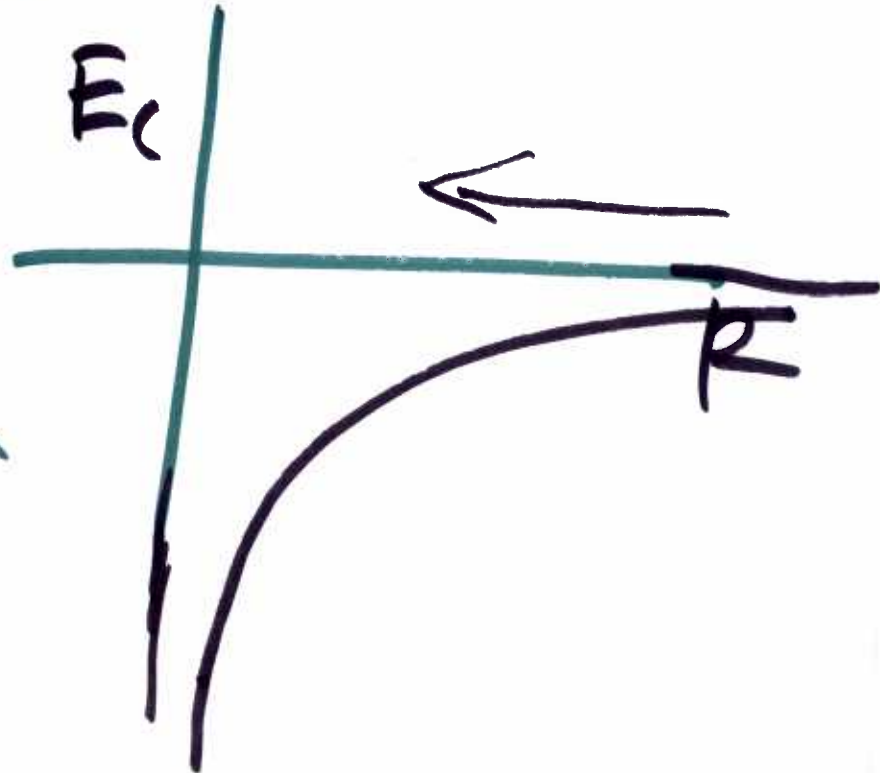


If there are N binding sites & m proteins, at equilibrium, how many of the proteins will be bound on to the DNA?



$$F_c =$$

$$\frac{-q^2}{4\pi k R}$$



$$- \epsilon k_B T$$

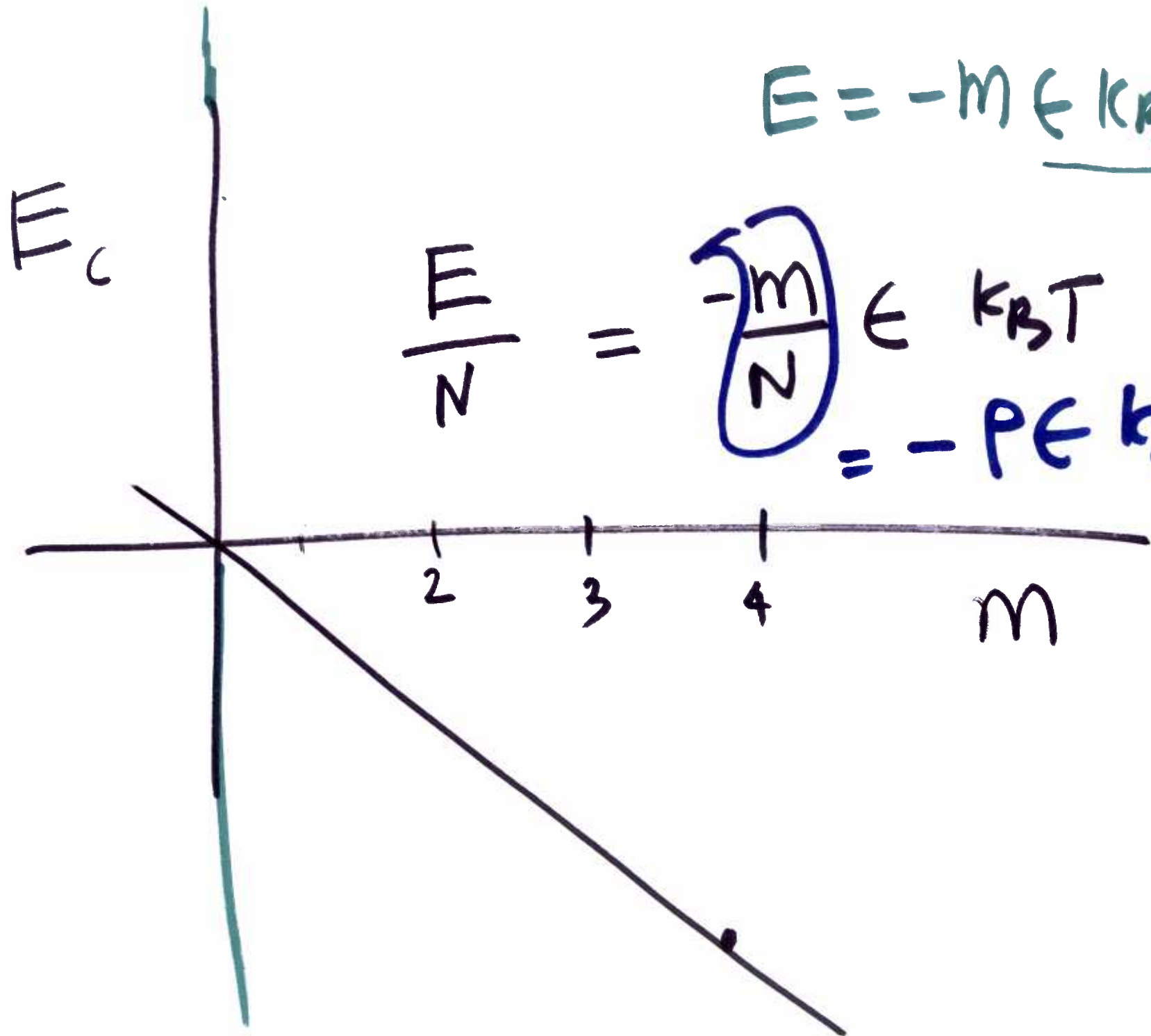

Energy gained when

1 protein binds to DNA

$$1: -\epsilon \in k_B T$$

$$2: -2\epsilon \in k_B T$$

$$m: -m\epsilon \in k_B T$$



$$E = -m \in \underline{K_{BT}}$$

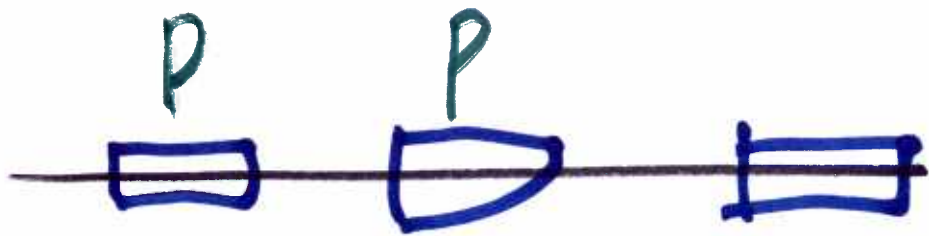
$$\frac{E}{N} = \frac{-m}{N} \in K_{BT} \\ = -P \in K_{BT}$$

$$F = E - TS$$

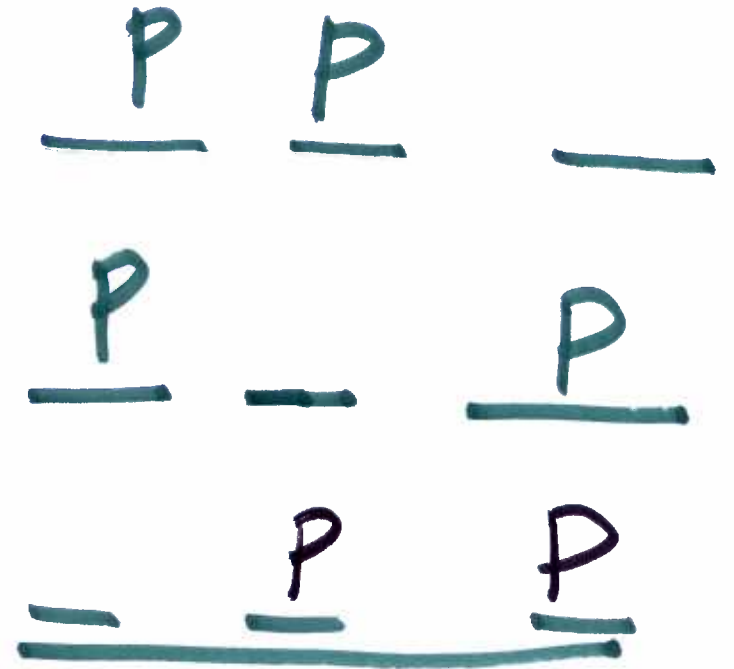
$$G = H - TS$$

$$S = k_B \ln \Omega$$

3 binding sites & 2 proteins



$$\Omega = 3$$



P P - - - P - P

P - P - - P P -
- - P P

P - - P

-

$$\Omega = 6$$

P P P P

$$\Omega = 1$$

$$k_B \ln \Omega = 0$$

$${}^N C_m = \frac{N!}{m! (N-m)!}$$

$$\ln \left[\frac{N!}{m! (N-m)!} \right]$$

$$\ln N! - \ln (m! (N-m)!)$$

$$\ln N! - \ln m! - \ln (N-m)!$$

$$\ln N! \approx N(\ln N - 1)$$

$$N(\ln N - 1) - (m \ln m - m)$$

$$- ((N-m) \ln (N-m))$$

$$\frac{m}{N} = p$$

$$\frac{m}{N} = \rho$$

fraction of sites

that is occupied by

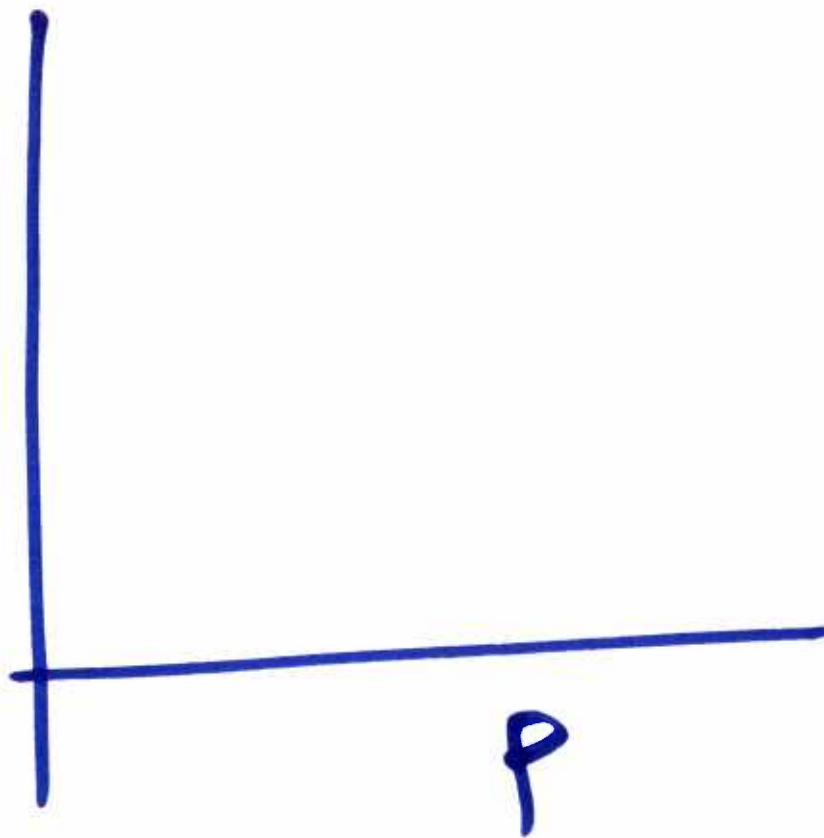
proteins

$$F(p)$$

$$\frac{\partial F}{\partial p} = 0$$

$$\frac{F}{Nk_B T}$$

$$\frac{F}{Nk_B T}$$



$$E = -Np k_B T$$

$$S = p \ln p + (1-p) \ln(1-p)$$