



Jet Aircraft Propulsion

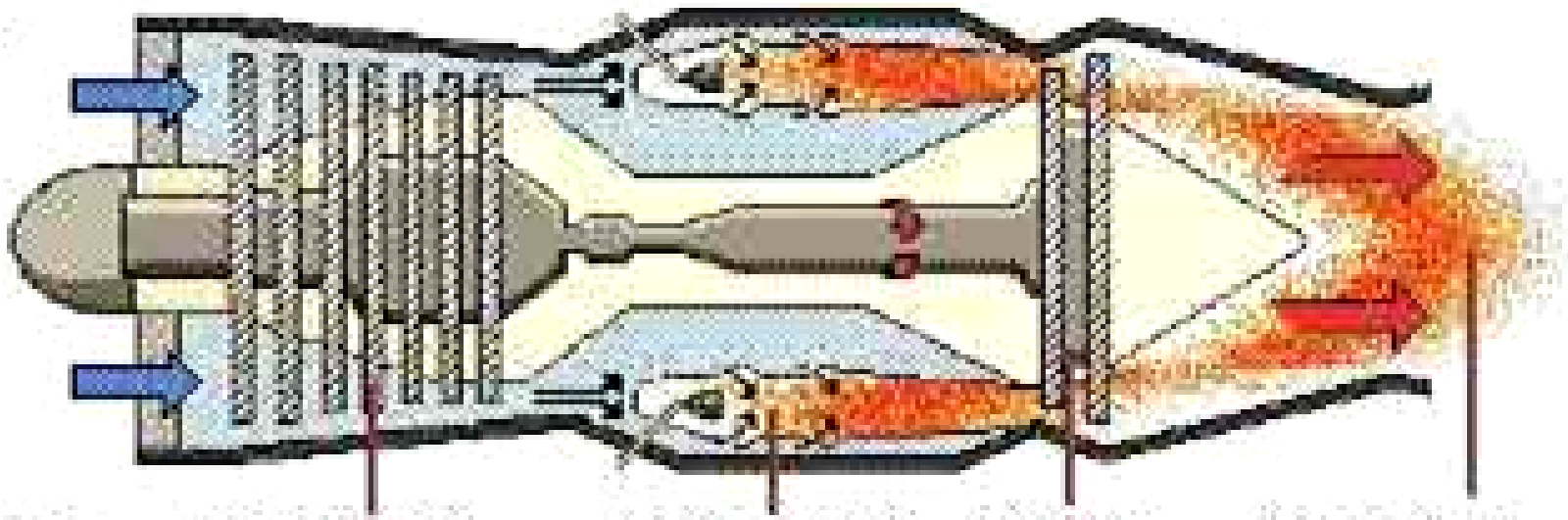
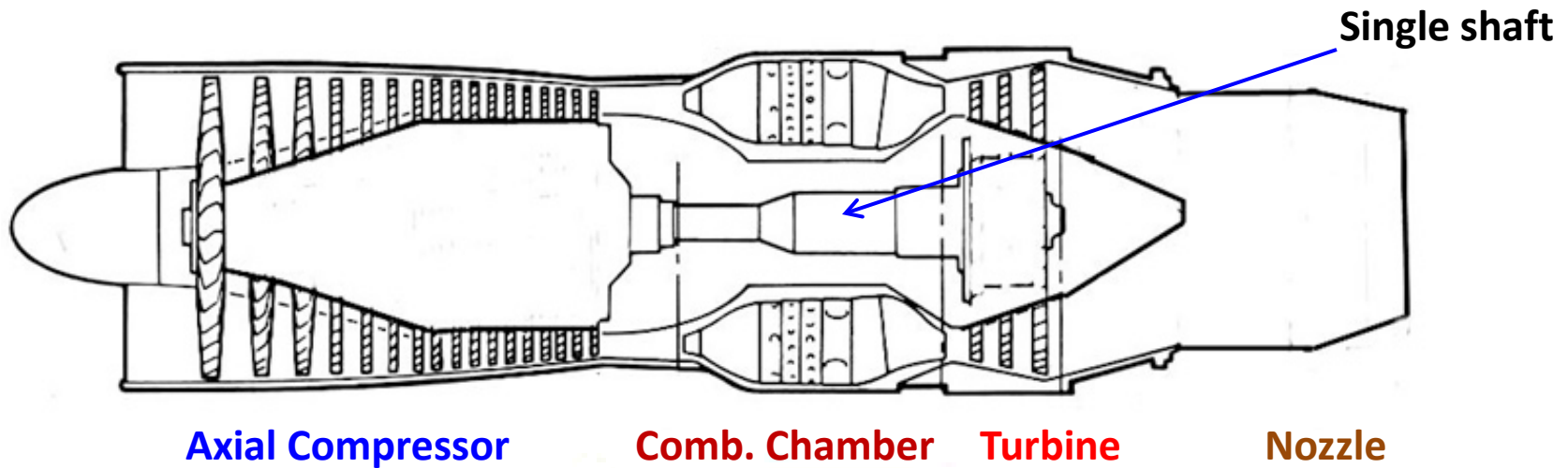
Prof. Bhaskar Roy, Prof. A M Pradeep

Department of Aerospace Engineering,
IIT Bombay

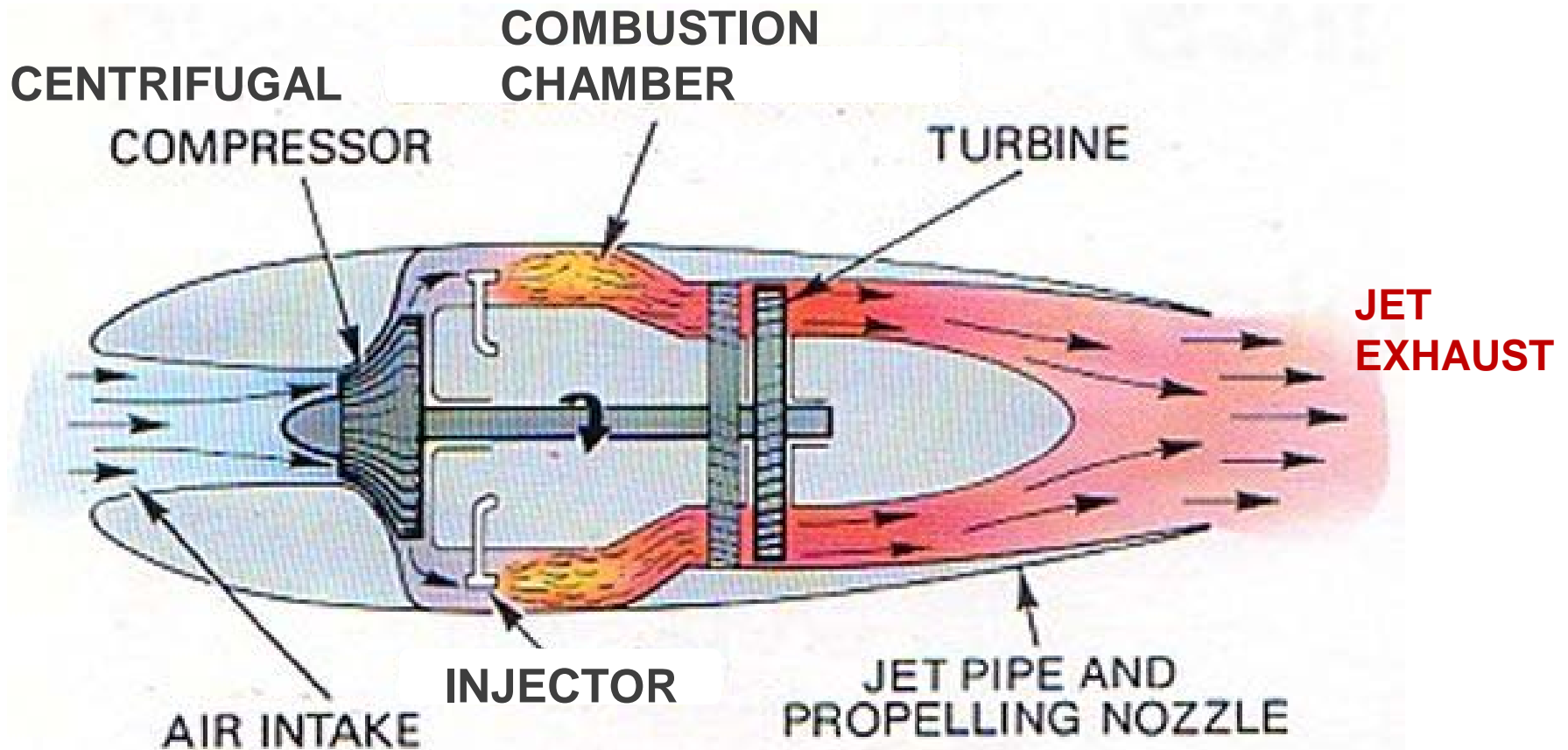
Lecture 4

Performance of a basic Jet engine

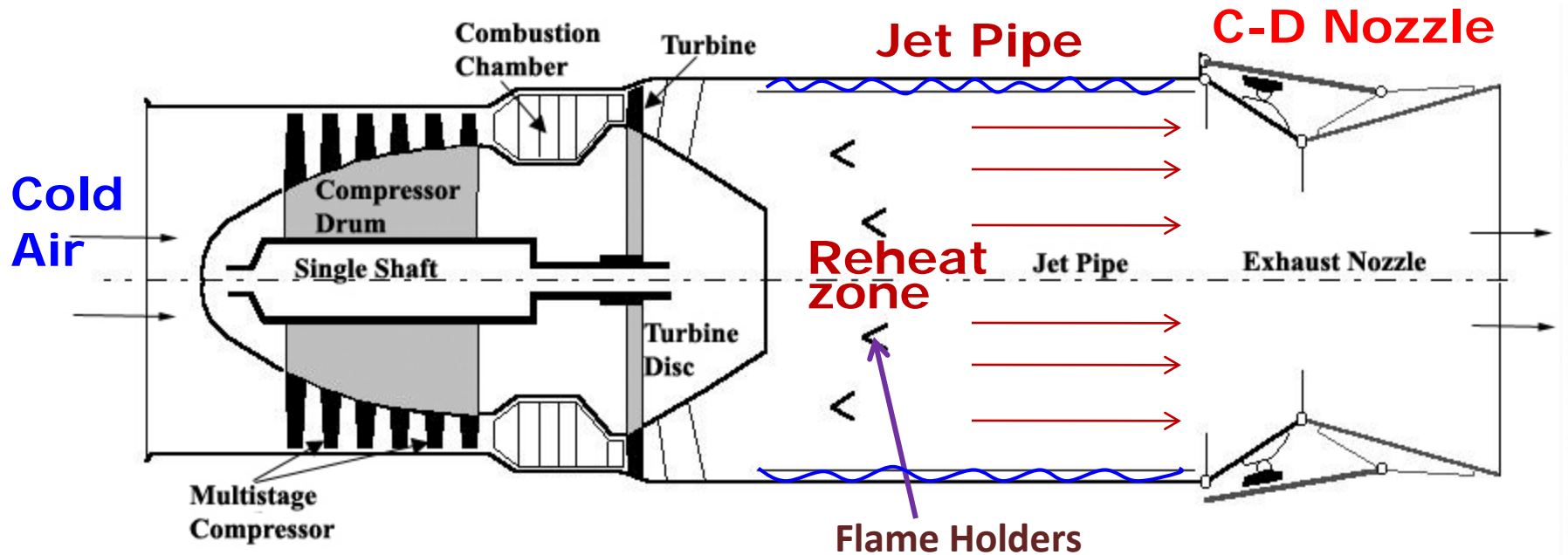
Simple single spool turbojet engine



Single Spool Turbojet Engine



Single Spool Turbojet Engine with Reheat



Consider the Thrust Equation

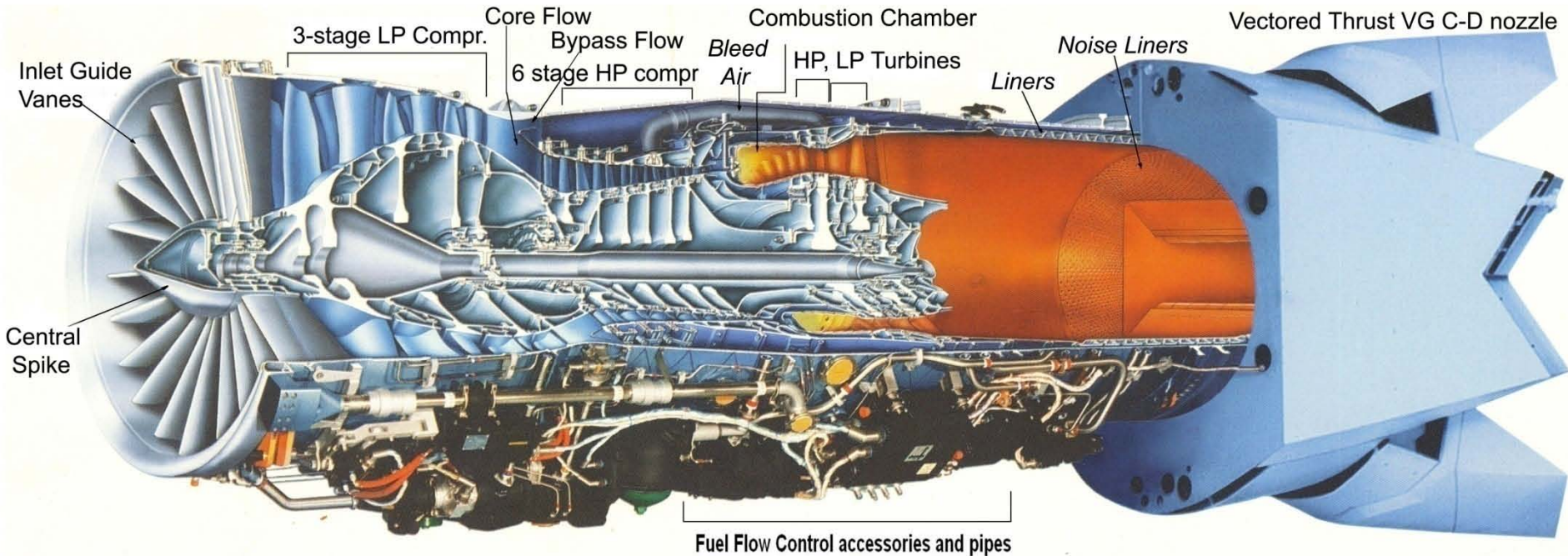
$$F_n = \dot{m} \cdot V_e - \dot{m} \cdot V_a + A_e \cdot (P_e - P_a)$$

- By Reheating it is intended to increase magnitude of the exit velocity V_e **by** employing Convergent-Divergent nozzle which can produce supersonic exit velocity
- Increased V_e would decrease P_e and take it below P_a
- This would result in a negative pressure thrust
- Hence, it is necessary that a reheat engine has sufficient pressure after the turbine to create high velocity jet. For this a larger compressor is required.

Compressors 9 stages

Jet Pipe

Nozzle system



A modern afterburning very low bypass turbofan engine

Thrust of a basic turbojet engine (momentum thrust)

$$F_n = (\dot{m}_a + \dot{m}_f) V_e - \dot{m}_a \cdot V_a$$

Where, \dot{m}_a is the air mass flow through the engine

\dot{m}_f is the fuel mass flow injected in to the engine

V_e , V_a are the air velocity into the engine and the same exiting the engine

V_e is dependant on η_{energy}

V_e is also dependant on $\eta_{\text{propulsive}}$

Thrust of a reheat turbojet engine (momentum thrust)

$$F_n = (\dot{m}_a + \dot{m}_{f-CC} + \dot{m}_{f-Rht})V_e - \dot{m}_a \cdot V_a$$

Where $\dot{m}_{f-Reheat}$ is the fuel input during the reheat or afterburning process

V_e is dependant on η_{energy} ,
and $\eta_{propulsive}$

Hence unless the fuel is burn efficiently and then energy is converted efficiently to V_e thrust production will not be efficient

The overall engine efficiencies are given by

$$\sigma = \frac{\dot{m} \cdot V_a \cdot (V_e - V_a)}{\dot{m}_f \cdot \dot{Q}_{\text{fuel}}} = \sigma_p \cdot \sigma_e$$

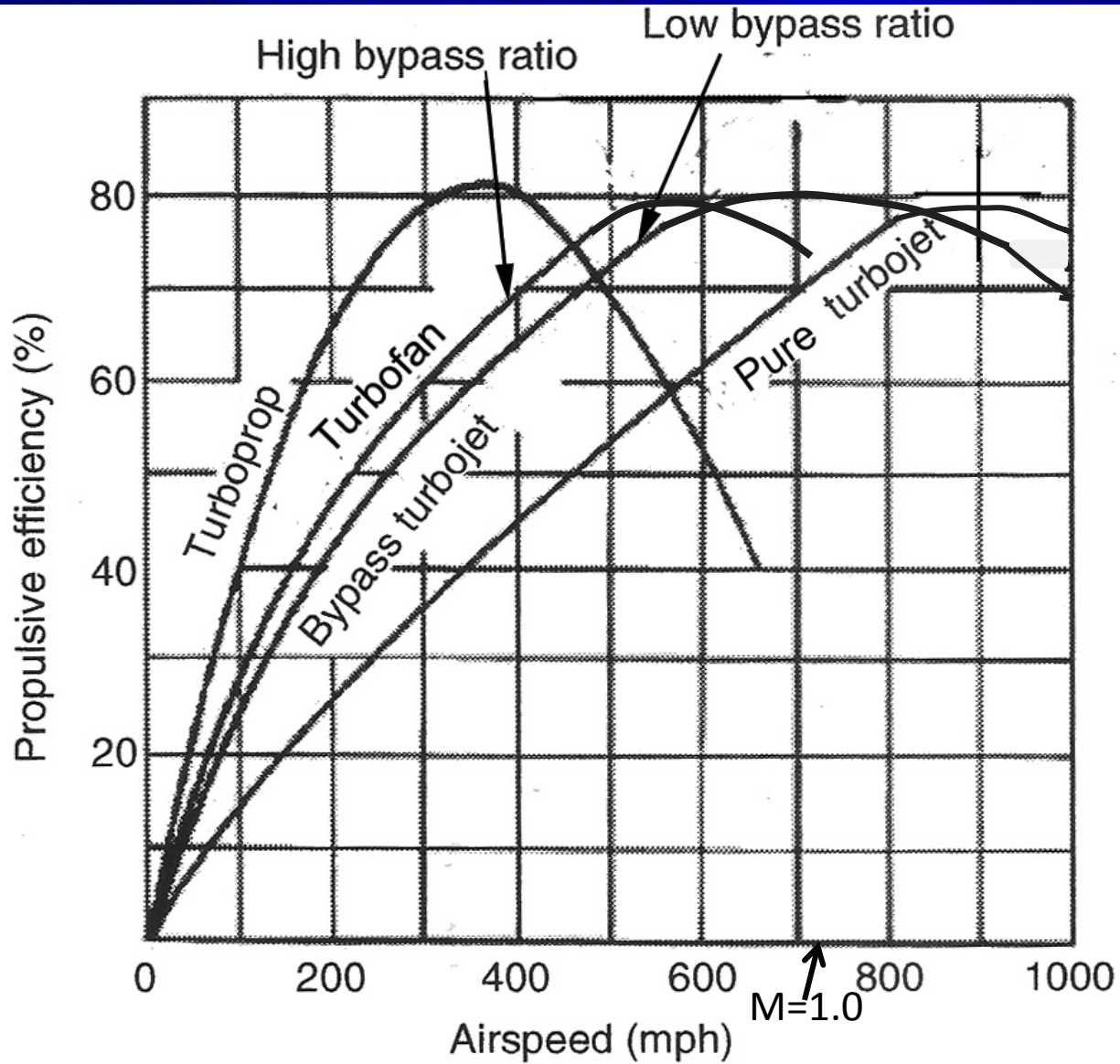
$$\sigma_{\text{-reheat}} = \frac{\dot{m} \cdot V_a \cdot (V_e - V_a)}{[\dot{m}_{f\text{-cc}} + \dot{m}_{f\text{-rht}}] \cdot \dot{Q}_{\text{fuel}}} = \sigma_{p\text{-AB}} \cdot \sigma_{e\text{-AB}}$$

Specific fuel consumptions

$$SFC = \frac{\dot{m}_{f\text{-cc}}}{F_n}$$

$$SFC_{\text{Reheat}} = \frac{\dot{m}_{f\text{-cc}} + \dot{m}_{f\text{-rht}}}{F_{n\text{-reheat}}}$$

- For jet engines with reheat or afterburning, the fuel consumption would be quite high, and SFC would show up as high value.
- In such operation sheer thrust requirement outweighs the high SFC.



Thrust of a bypass engine

$$F_n = [(\dot{m}_a + \dot{m}_f)v_{e-hot} - \dot{m}_a \cdot v_a]_{hot-jet} + \dot{m}_{a-bypass} [v_{e-bypass} - v_a]$$

SFC of a bypass engine

$$SFC = \frac{\dot{m}_{f-cc}}{F_{n-hot} + F_{n-cold}}$$

Overall Efficiency of Bypass Jet engine

$$\eta_o = \frac{\dot{m} \cdot V_a \cdot (V_e - V_a)}{\dot{m}_f \cdot \dot{Q}_{fuel}} = \eta_p \cdot \eta_e$$

Exhaust Jet waste

$$\frac{\dot{m}_{hot} \cdot (V_{e-hot} - V_a)^2 + \dot{m}_{cold} \cdot (V_{e-bypass} - V_a)^2}{2}$$

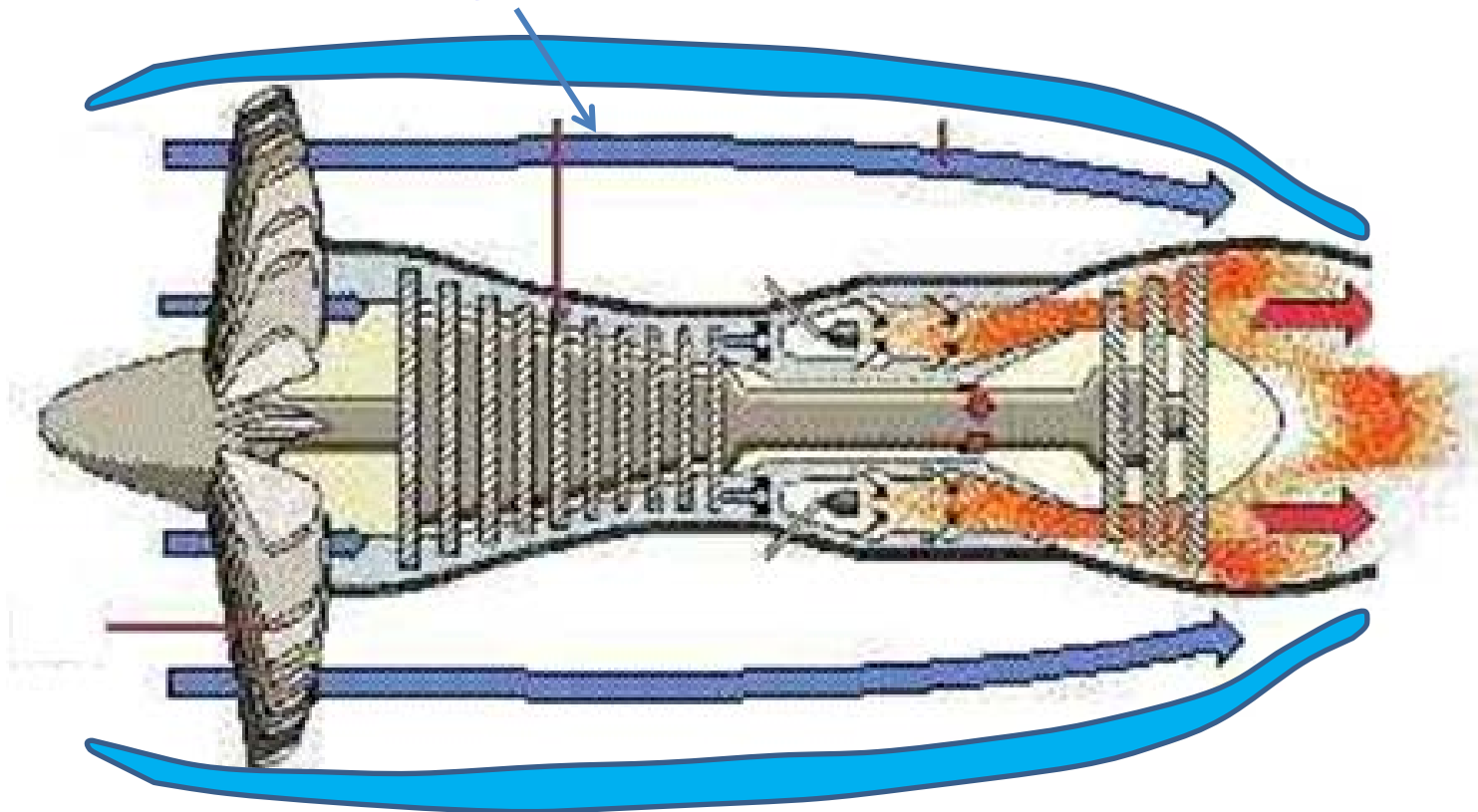
Propulsive Efficiency of the bypass jet engine

$$\eta_p = \frac{[\dot{m}_a \cdot V_a \cdot (V_e - V_a)]_{hot} + [\dot{m}_a \cdot V_a \cdot (V_e - V_a)]_{bypass}}{\dot{m}_{a-core} \cdot [V_a \cdot (V_e - V_a)]_{hot} + \dot{m}_{a-bypass} [V_a \cdot (V_e - V_a)]_{bypass} + \dot{m}_{a-core} \frac{(V_{e-hot} - V_a)^2}{2} + \dot{m}_{a-bypass} \frac{(V_{e-cold} - V_a)^2}{2}}$$

$$= \frac{2}{1 + \frac{V_{e-average}}{V_a}} \quad \text{where, } V_{e-average} = \frac{\dot{m}_{a-hot} \cdot V_{e-hot} + \dot{m}_{a-bypass} \cdot V_{e-bypass}}{\dot{m}_{a-hot} + \dot{m}_{a-bypass}}$$

Single Spool Turbofan engine

Cold Bypass



Next class :

Multi-spool Turbojet and Turbofan engines