

Tutorial Session on Ray Optics & Wave Optics:

8/3/2018

Example 1: Dispersion in a prism (min) $\lambda \rightarrow \frac{c}{n(\lambda)} \rightarrow$ velocity of light within a medium

$$n_{\text{blue}} = 1.34$$

$$n_{\text{red}} = 1.33$$

Paraxial approximation

$$n_1 \theta_1 = n_2 \theta_2$$

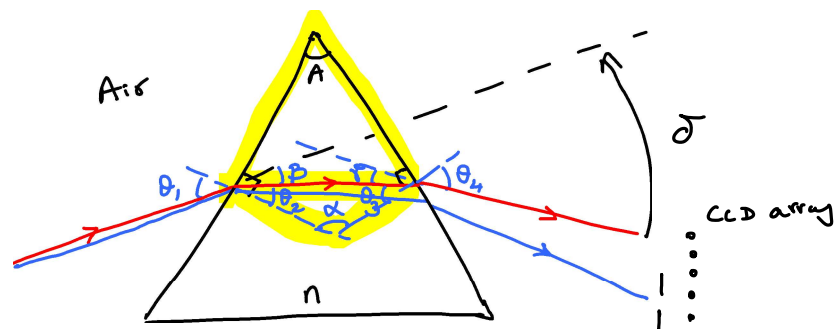
$$\sigma = (n-1)A$$

$$A = 10^\circ$$

$$\sigma_{\text{red}} = (1.33 - 1)10^\circ = 3.3^\circ$$

$$\sigma_{\text{blue}} = (1.34 - 1)10^\circ = 3.4^\circ$$

$$\Rightarrow 0.1 \text{ deg}$$

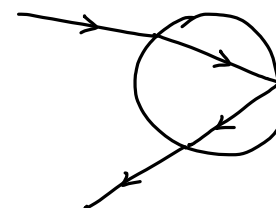


$$\alpha + A = 180^\circ$$

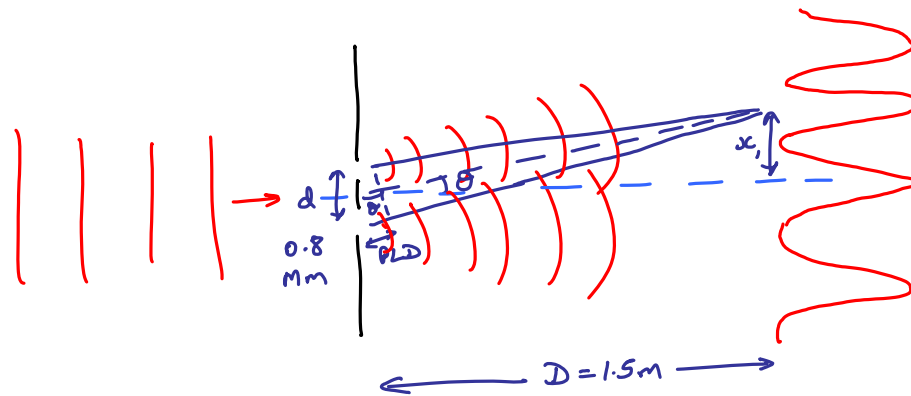
$$\theta_2 + \theta_3 + \alpha = 180^\circ$$

$$\Rightarrow A = \theta_2 + \theta_3$$

$$\begin{aligned} \sigma &= \beta + \gamma = \theta_1 - \theta_2 + \theta_4 - \theta_3 = \theta_1 + \theta_4 - A \\ &= n\theta_2 + n\theta_3 - A = (n-1)A \end{aligned}$$



Example 2: Can you discriminate different colours using Young's double slit?



$$\lambda_{\text{red}} = 650 \text{ nm}$$

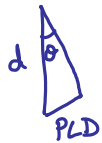
$$\lambda_{\text{orange}} = 600 \text{ nm}$$

$$x_1^r = D \tan(\theta_r) = \underline{1.218 \text{ mm}}$$

$$x_1^o = \underline{1.125 \text{ mm}}$$

$$x_1^r - x_1^o = 93 \mu\text{m}$$

$$\text{slit width} = \frac{x_1^r - x_1^o}{2} = \underline{46.5 \mu\text{m}}$$



$$\sin \theta = \frac{\text{PLD}}{d}$$

$$\text{PLD} = d \sin \theta$$

$$\phi_1 - \phi_2 = 2\pi m$$

$$\frac{2\pi}{\lambda} n d \sin \theta_m = 2\pi m \quad (\text{Constructive interference})$$

$$\text{For } m=1 \quad \theta_1^r = \sin^{-1}\left(\frac{\lambda_r}{d}\right) = \sin^{-1}\left(\frac{0.65 \times 10^{-6}}{0.8 \times 10^{-3}}\right) = 0.8 \text{ mrad}$$