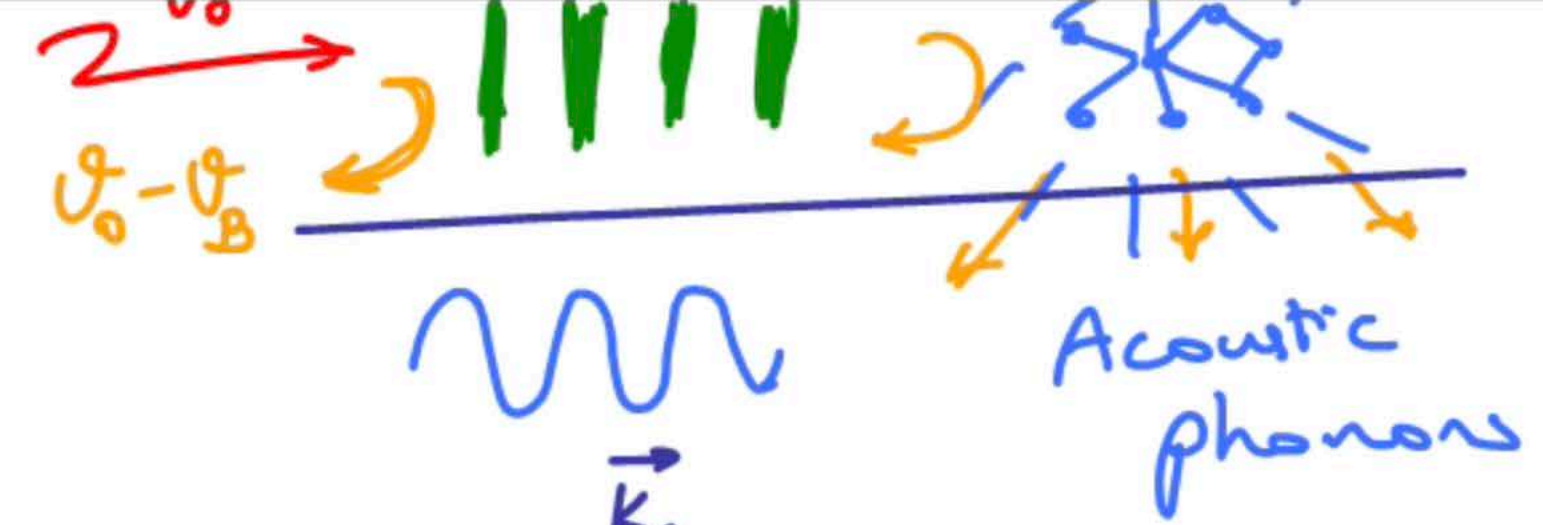


If source is highly coherent



$$\vec{K}_p - \vec{K}_s = \vec{K}_A$$

$$\text{If } |\vec{K}_p| \approx |\vec{K}_s| \quad 2|\vec{K}_p| = |\vec{K}_A|$$

$$2 \cdot \frac{2\pi}{\lambda_p} n_{\text{eff}} = \frac{2\pi V_B}{V_A}$$

$$n_{\text{eff}} \approx 1.5$$

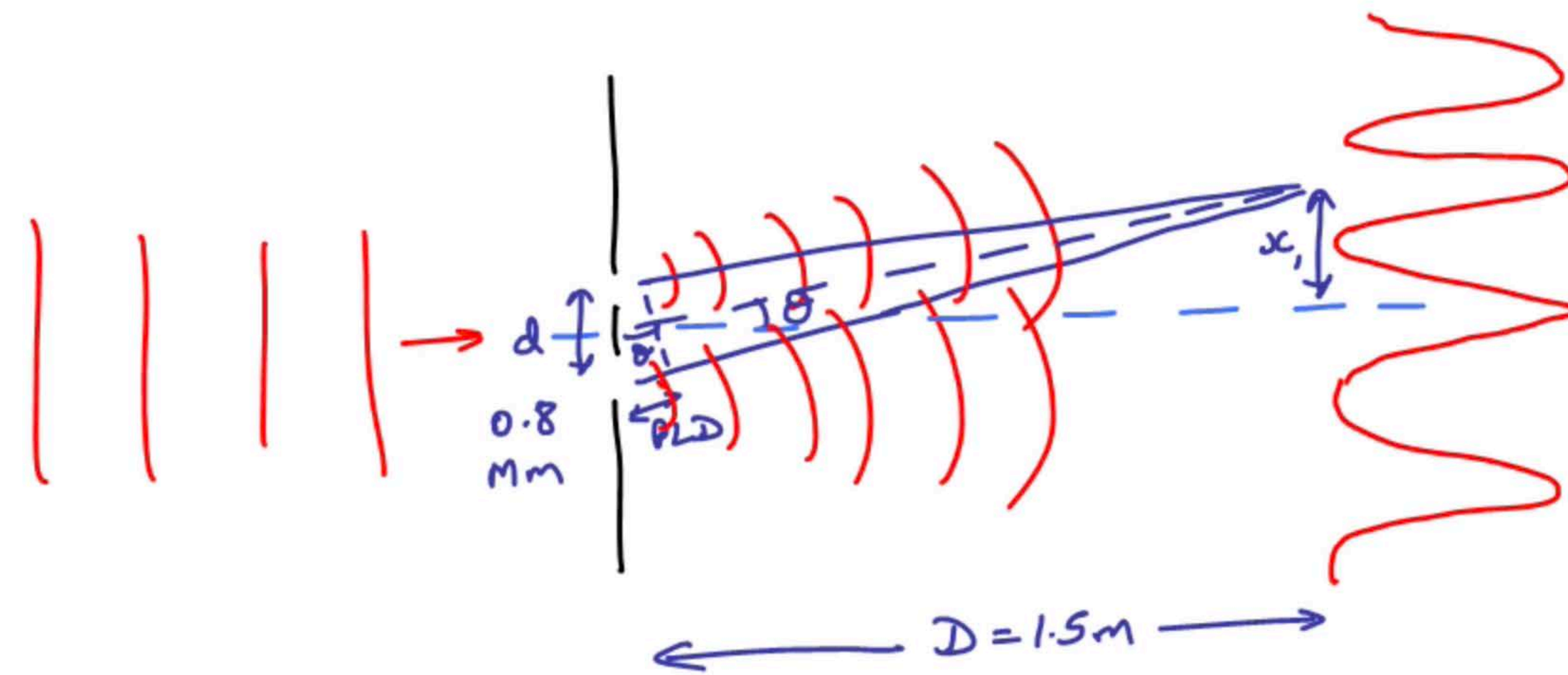
$$V_A = 6 \text{ km/s}$$

$$\lambda_p = 1.5 \text{ } \mu\text{m}$$

$$\Rightarrow V_B = 12 \text{ GHz}$$

$$V_B = \frac{2 n_{\text{eff}} V_A}{\lambda_p}$$

Example 2: Can you discriminate different colours using Young's double slit?



$$\lambda_{\text{red}} = 650 \text{ nm}$$

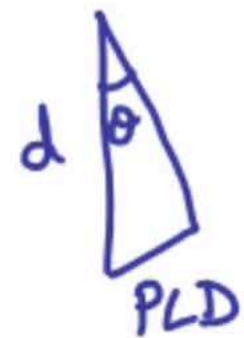
$$\lambda_{\text{orange}} = 600 \text{ nm}$$

$$x_1^r = D \tan(\theta_r) \\ = \underline{1.218 \text{ mm}}$$

$$x_1^o = \underline{1.125 \text{ mm}}$$

$$x_1^r - x_1^o = 93 \mu\text{m}$$

$$\text{slit width} = \frac{x_1^r - x_1^o}{2} = \underline{46.5 \mu\text{m}}$$



$$\sin \theta = \frac{PLD}{d}$$

$$PLD = d \sin \theta$$

$$\phi_1 - \phi_2 = 2\pi m$$

$$\frac{2\pi}{\lambda} n d \sin \theta_m = 2\pi m \quad (\text{Constructive interference})$$

$$\text{For } m=1 \quad (n=1) \quad \theta_1^r = \sin^{-1}\left(\frac{\lambda_r}{d}\right) = \sin^{-1}\left(\frac{0.65 \times 10^{-6}}{0.8 \times 10^{-3}}\right) = 0.8 \text{ mrad}$$

Energy Conservation

$$\omega_1 + \omega_2 = \omega_3 + \omega_4$$

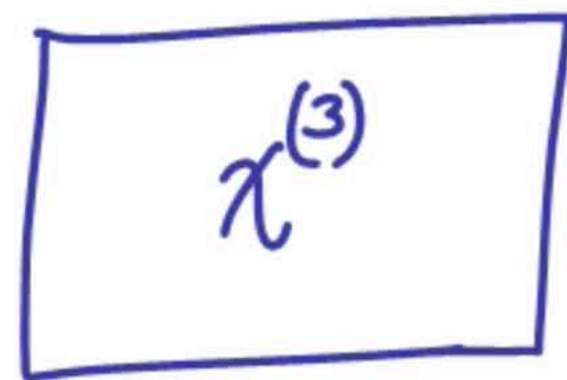
Momentum Conservation

$$\vec{k}_1 + \vec{k}_2 = \vec{k}_3 + \vec{k}_4$$

$$E(\omega_1) \rightarrow$$

$$E(\omega_2) \rightarrow$$

$$E(\omega_3) \rightarrow$$



$$\omega_1 + \omega_2 + \omega_3$$

$$\omega_1 - \omega_2 - \omega_3$$

\vdots

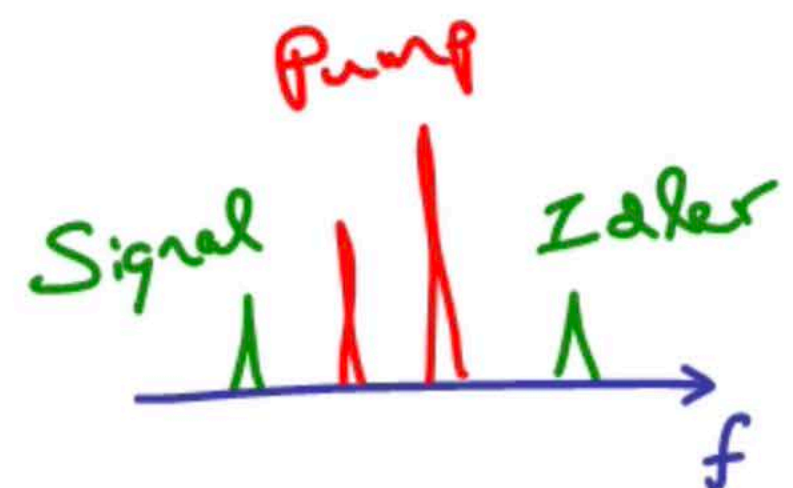
Four-wave mixing

Self Phase Modulation/

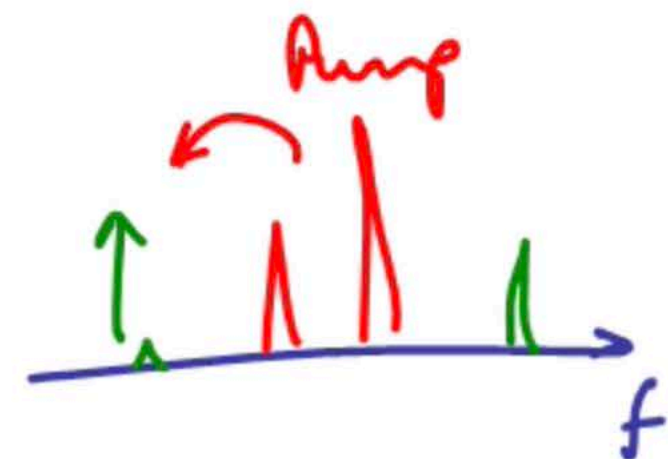
Kerr effect

Stimulated Raman Scattering

Stimulated Brillouin Scattering

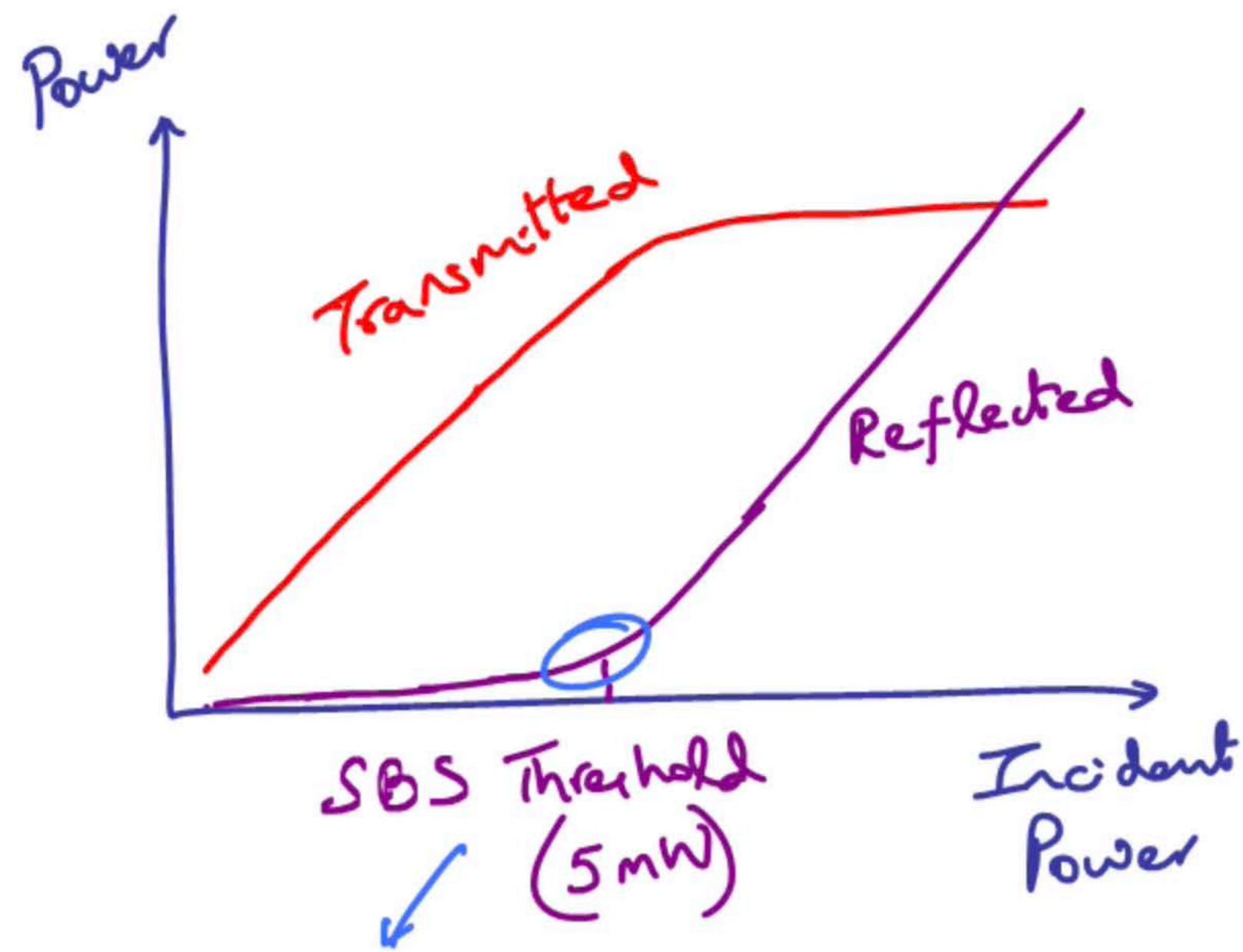


Wavelength Conversion



Parametric Amplification

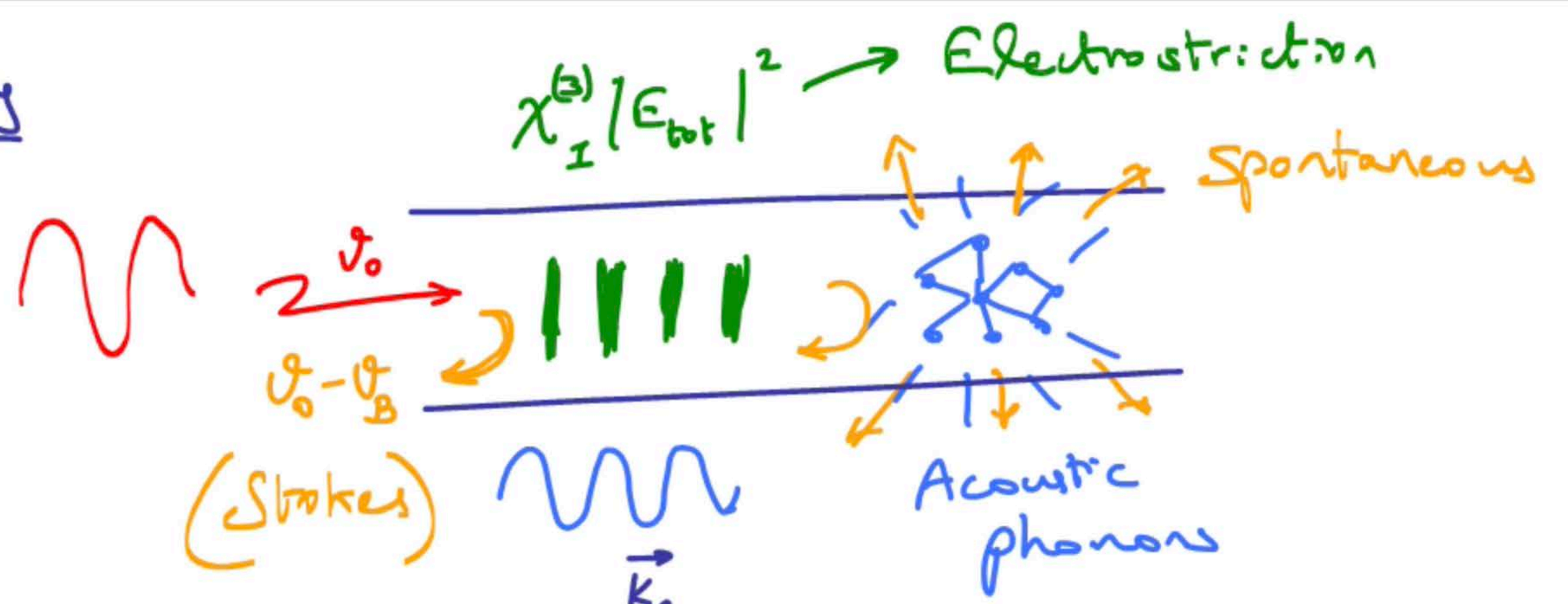
Stimulated Brillouin Scattering



If source is highly coherent

Optical Communications

Optical Sensing



$\chi^{(2)} |\vec{E}_{\text{opt}}|^2 \rightarrow$ Electrostriction

$$\vec{k}_p - \vec{k}_s = \vec{k}_A$$

$$\text{If } |\vec{k}_p| \approx |\vec{k}_s| \quad 2|\vec{k}_p| = |\vec{k}_A|$$

$$2 \cdot \frac{2\pi}{\lambda_p} n_{\text{eff}} = \frac{2\pi \omega_B}{V_A}$$

$$n_{\text{eff}} \approx 1.5$$

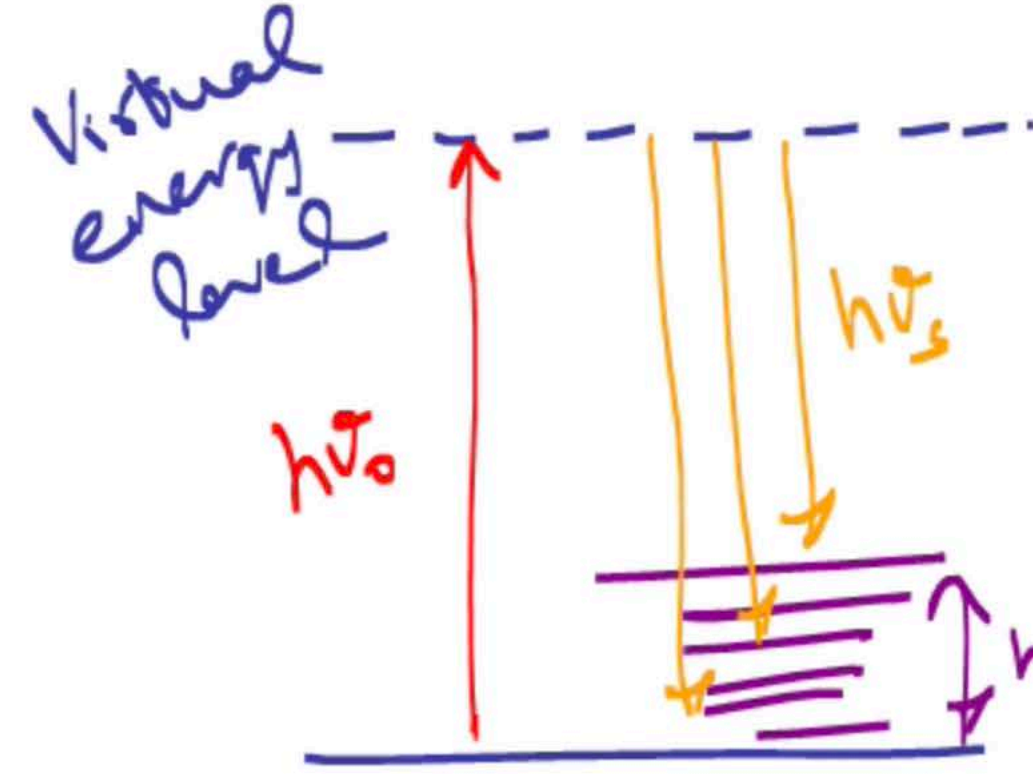
$$V_A = 6 \text{ km/s}$$

$$\lambda_p = 1.5 \mu\text{m}$$

$$\Rightarrow \omega_B = 12 \text{ GHz}$$

$$\omega_B = \frac{2 n_{\text{eff}} V_A}{\lambda_p}$$

Stimulated Raman Scattering → Spectroscopy
 → Temperature
 → Communications

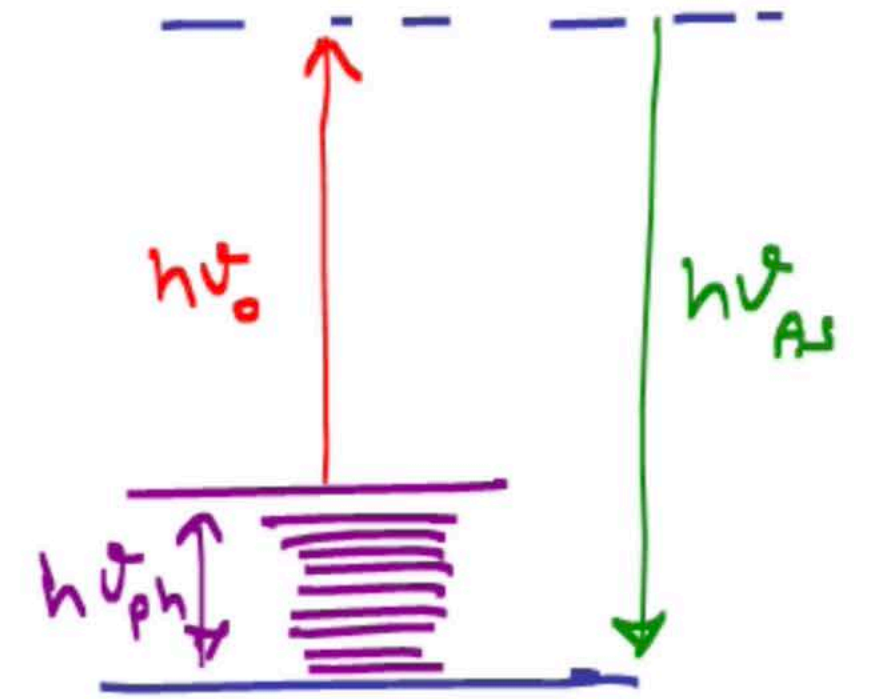


Narrow → Crystal
 Broad → Amorphous

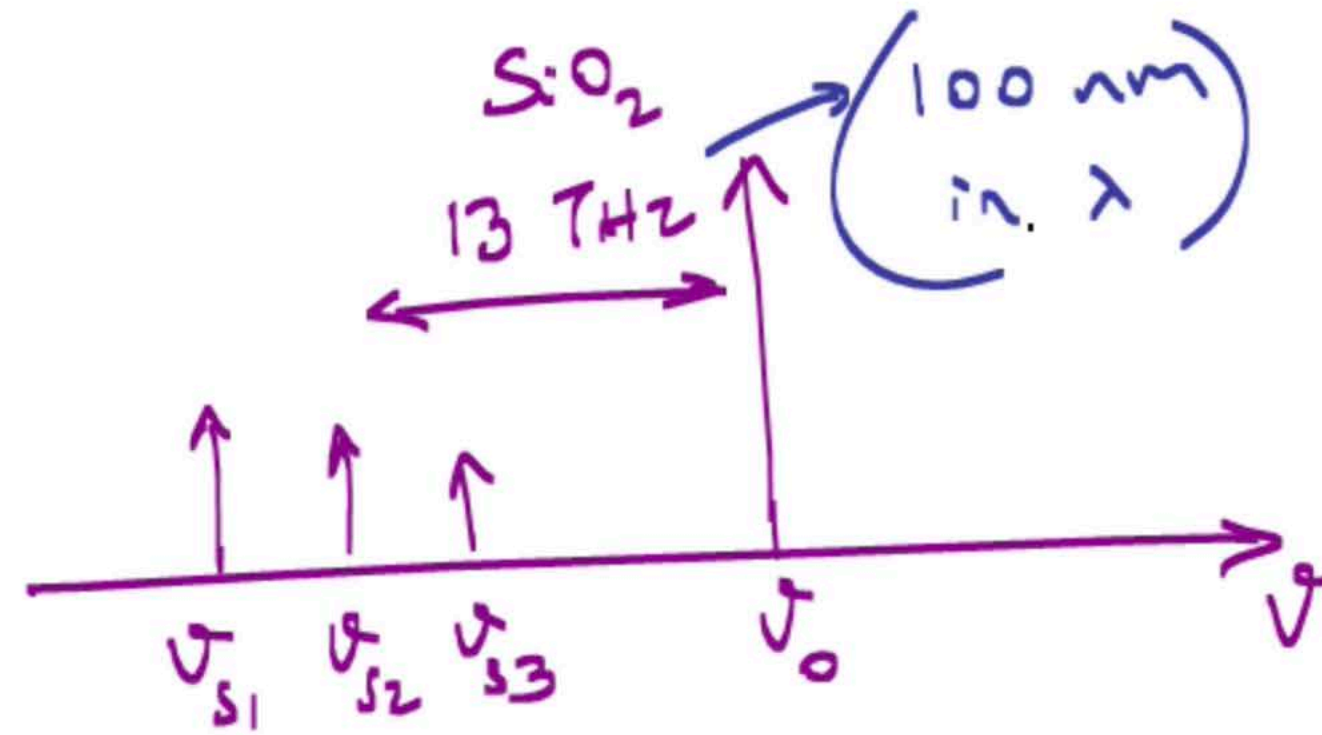
optical
 phonons

Anti-Stokes $h\nu_{AS}$

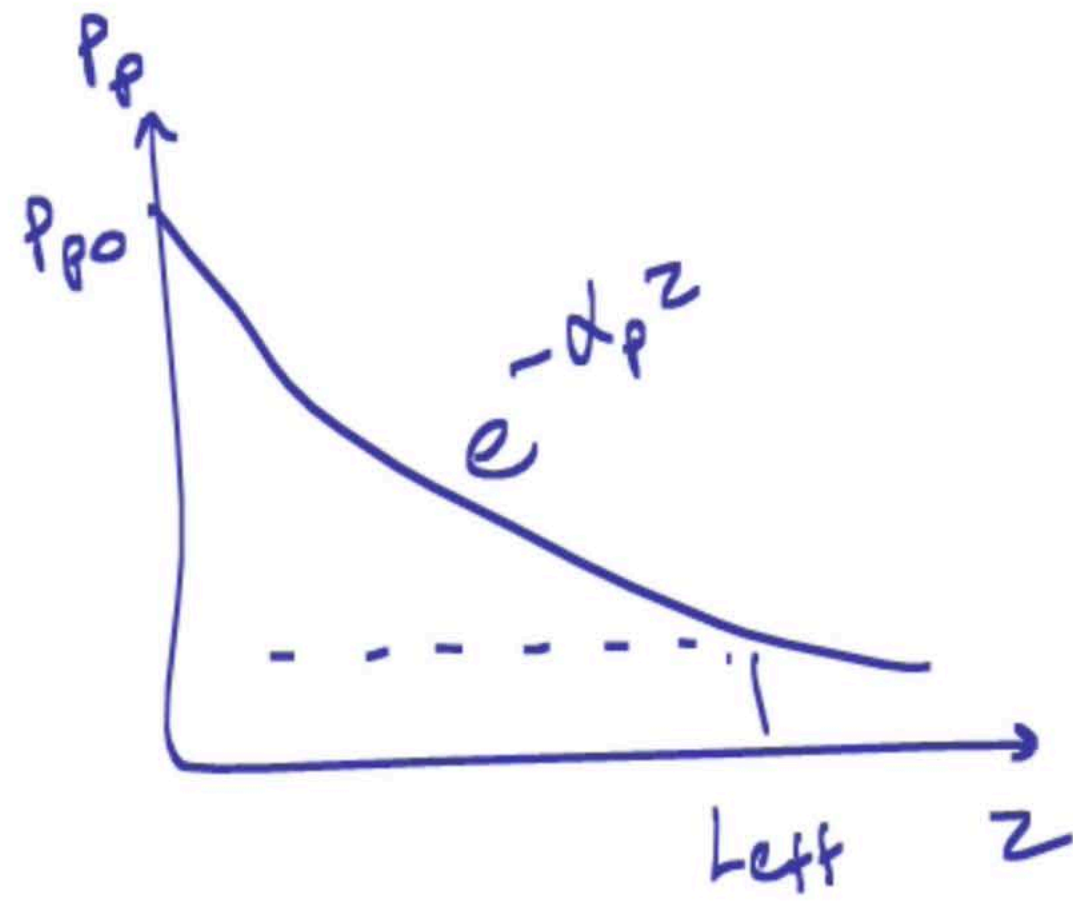
(Amplification)



Stokes scattering
 (10^{-7})



$$R = \frac{P_{AS}}{P_S} = \left(\frac{\lambda_S}{\lambda_{AS}} \right)^4 \exp\left(-\frac{h\nu_{ph}}{k_B T} \right)$$



$$\frac{dP_s}{dz} = \overset{\text{SRS}}{g_R \frac{P_p}{A_{eff}} \cdot P_s} - \overset{\text{Attenuation}}{\alpha_s P_s}$$

Amplifier gain $G_R = \exp\left(\frac{g_R}{A_{eff}} P_{po} \cdot L_{eff}\right)$

To achieve 20 dB gain,

$$g_B = 6 \times 10^{-11} \text{ m/W}$$

$$g_R = 6 \times 10^{-14} \text{ m/W}$$

$$L_{eff} = 20 \text{ km}$$

$$A_{eff} = 50 \text{ } \mu\text{m}^2$$

$$P_{po} = \underline{\underline{0.2 \text{ W}}}$$