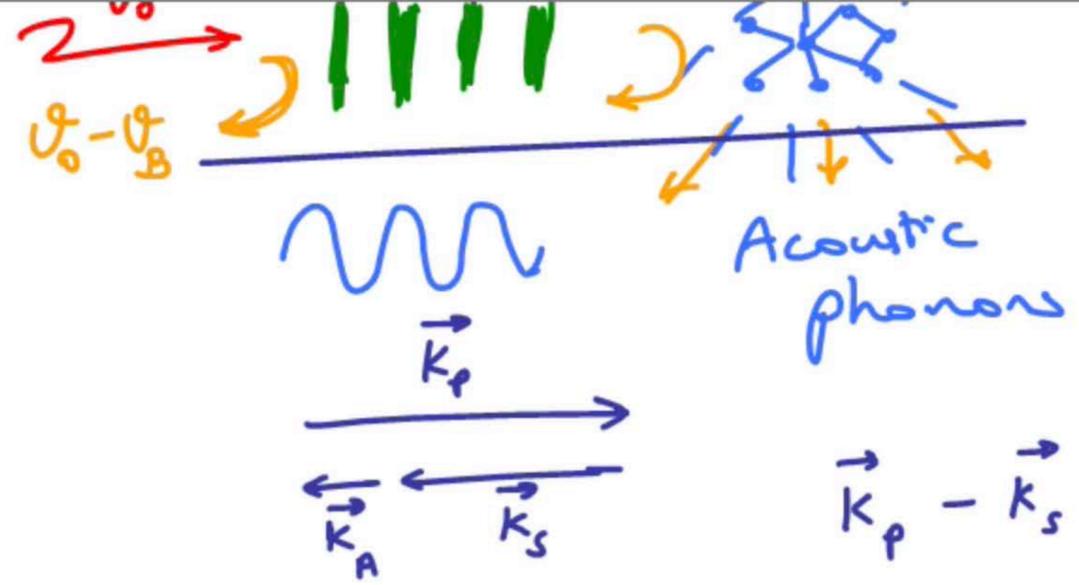


If source is highly coherent



$$\vec{k}_p - \vec{k}_s = \vec{k}_A$$

$$\text{If } |k_p| \approx |k_s| \quad 2|k_p| = |k_A|$$

$$2 \cdot \frac{2\pi}{\lambda_p} n_{\text{eff}} = \frac{2\pi \nu_B}{v_A}$$

$$n_{\text{eff}} \approx 1.5$$

$$v_A = 6 \text{ km/s}$$

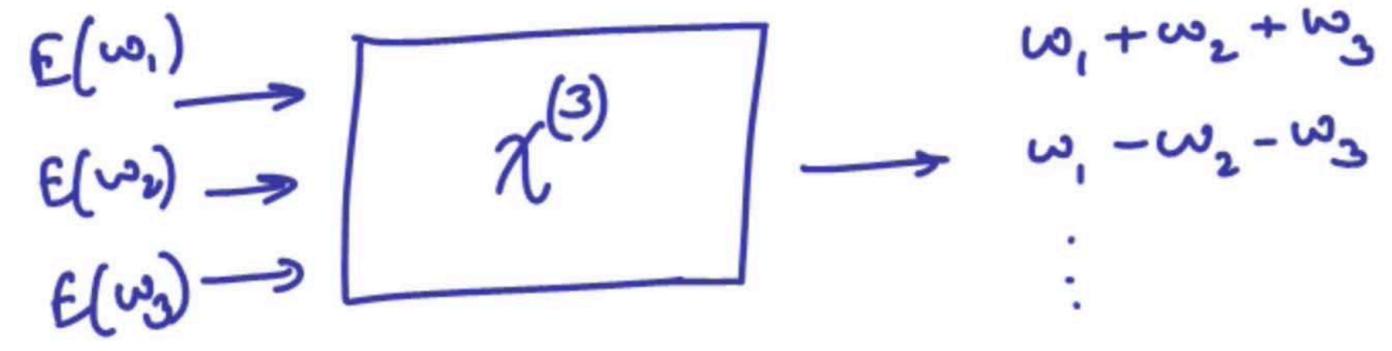
$$\lambda_p = 1.5 \text{ } \mu\text{m}$$

$$\Rightarrow \nu_B = 12 \text{ GHz}$$

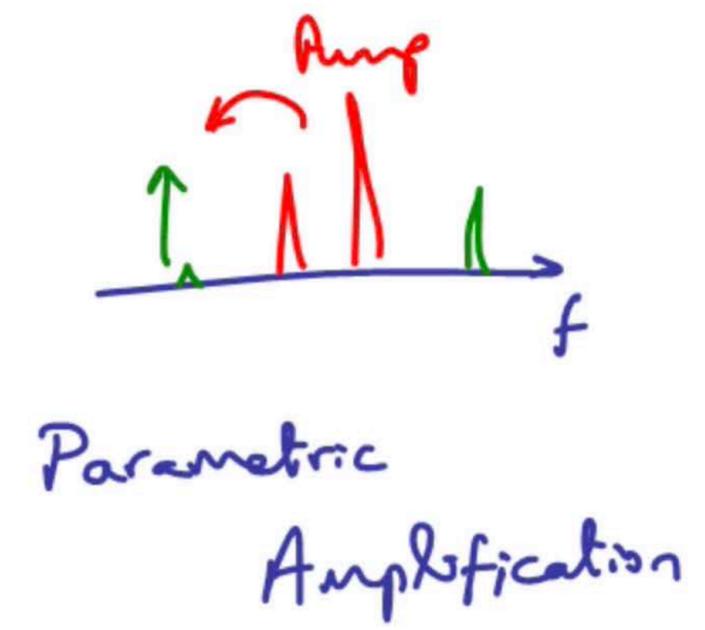
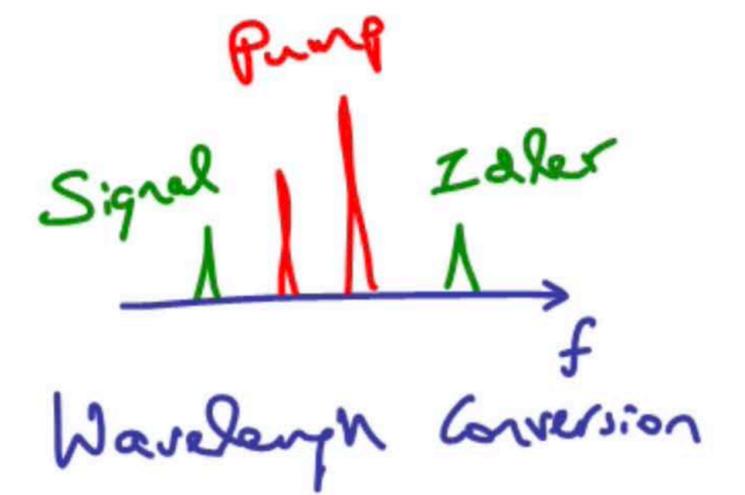
$$\nu_B = \frac{2 n_{\text{eff}} v_A}{\lambda_p}$$

Energy Conservation
 $\omega_1 + \omega_2 = \omega_3 + \omega_4$

Momentum Conservation
 $\vec{k}_1 + \vec{k}_2 = \vec{k}_3 + \vec{k}_4$



- Four-wave mixing
- Self Phase Modulation
- Kerr effect
- Stimulated Raman Scattering
- Stimulated Brillouin Scattering



Energy Conservation

$$\omega_1 + \omega_2 = \omega_3 + \omega_4$$

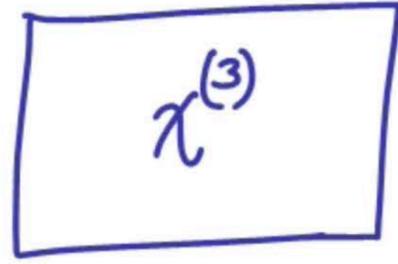
Momentum Conservation

$$\vec{k}_1 + \vec{k}_2 = \vec{k}_3 + \vec{k}_4$$

$$E(\omega_1) \rightarrow$$

$$E(\omega_2) \rightarrow$$

$$E(\omega_3) \rightarrow$$

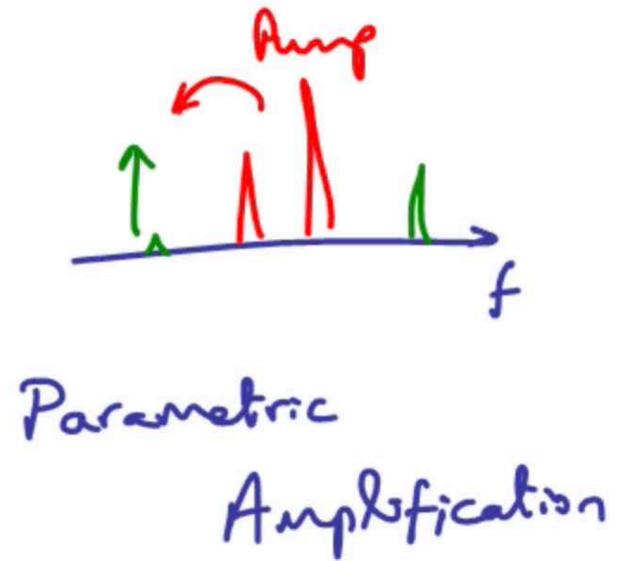
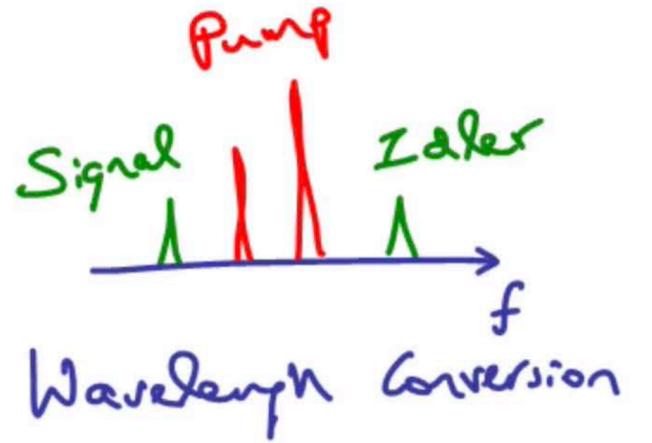


$$\omega_1 + \omega_2 + \omega_3$$

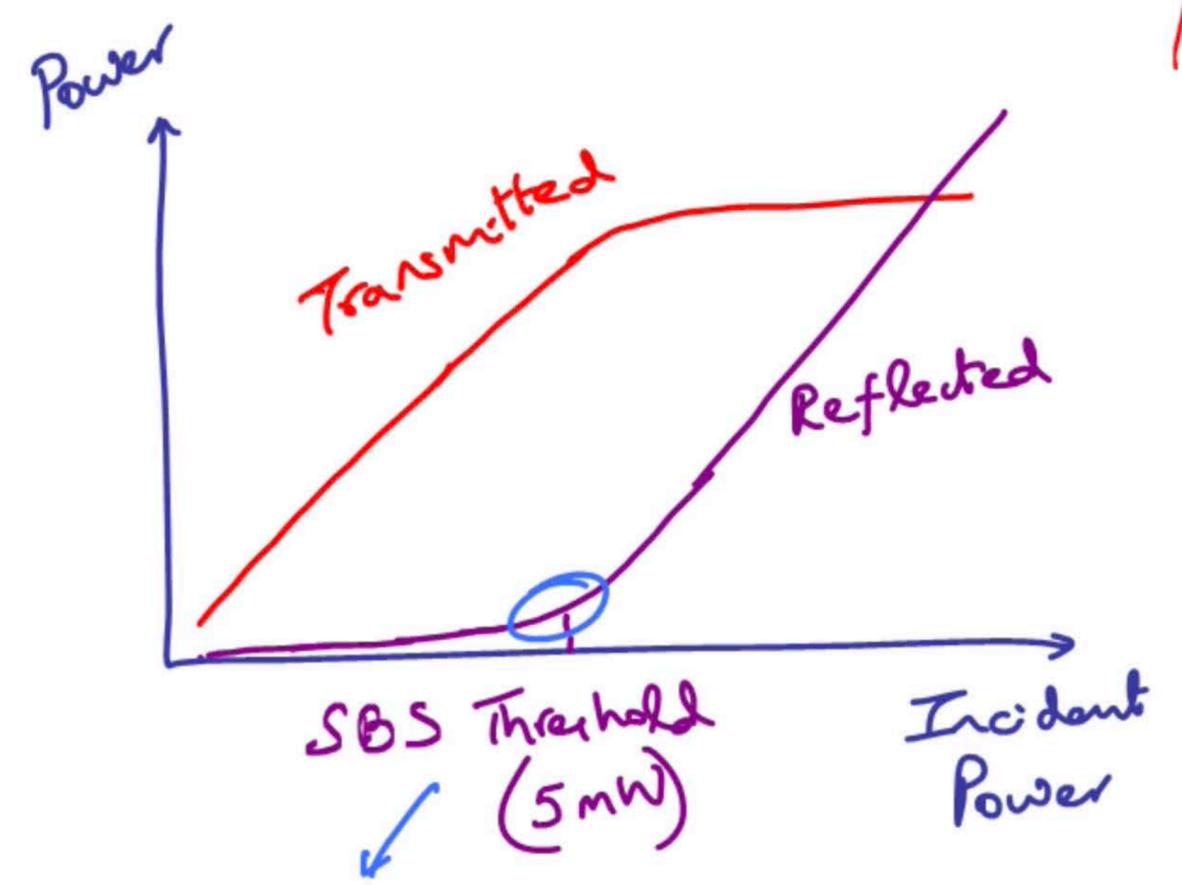
$$\omega_1 - \omega_2 - \omega_3$$

⋮

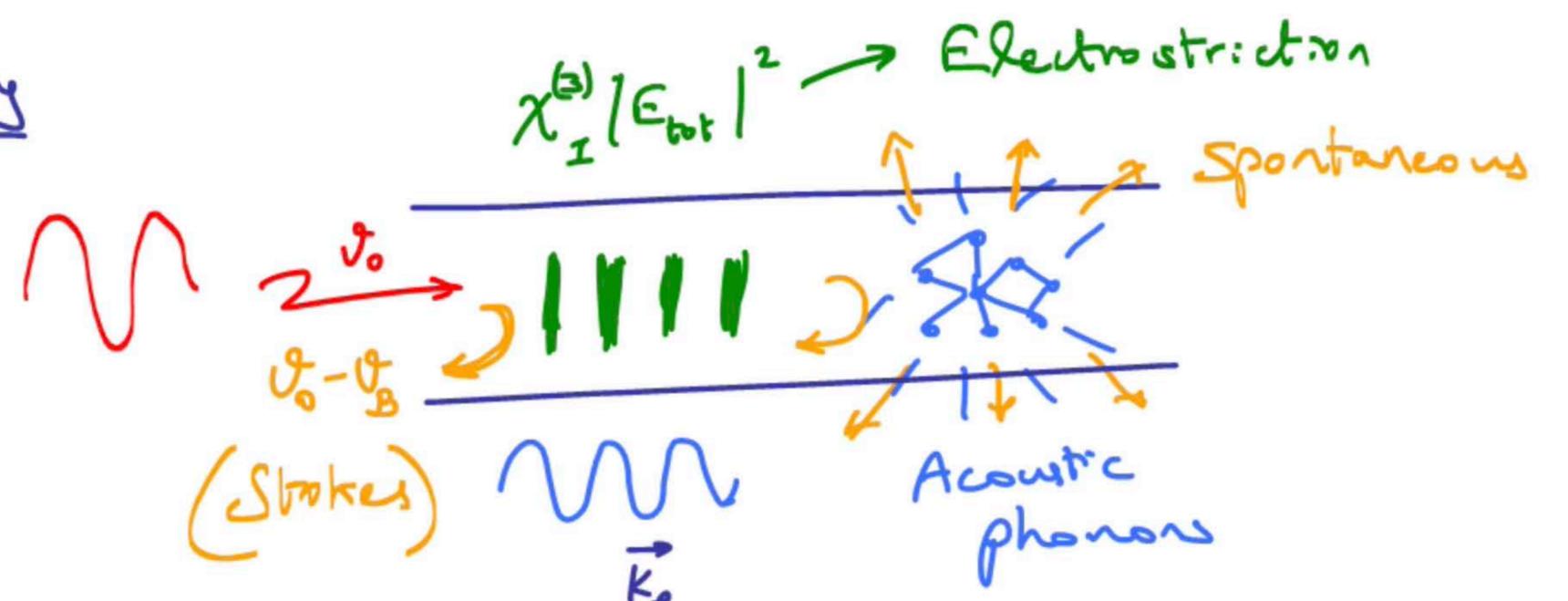
- ✓ Four-wave mixing
- ✓ Self Phase Modulation/
Kerr effect
- ✓ Stimulated Raman Scattering
- ✓ Stimulated Brillouin Scattering



Stimulated Brillouin Scattering



If source is highly coherent
 Optical Communications
 Optical Sensing



$$\vec{k}_p - \vec{k}_s = \vec{k}_A$$

$$I_{\text{th}} \quad |\vec{k}_p| \approx |\vec{k}_s| \quad 2|\vec{k}_p| = |\vec{k}_A|$$

$$2 \cdot \frac{2\pi}{\lambda_p} n_{\text{eff}} = \frac{2\pi \nu_B}{V_A}$$

$$n_{\text{eff}} \approx 1.5$$

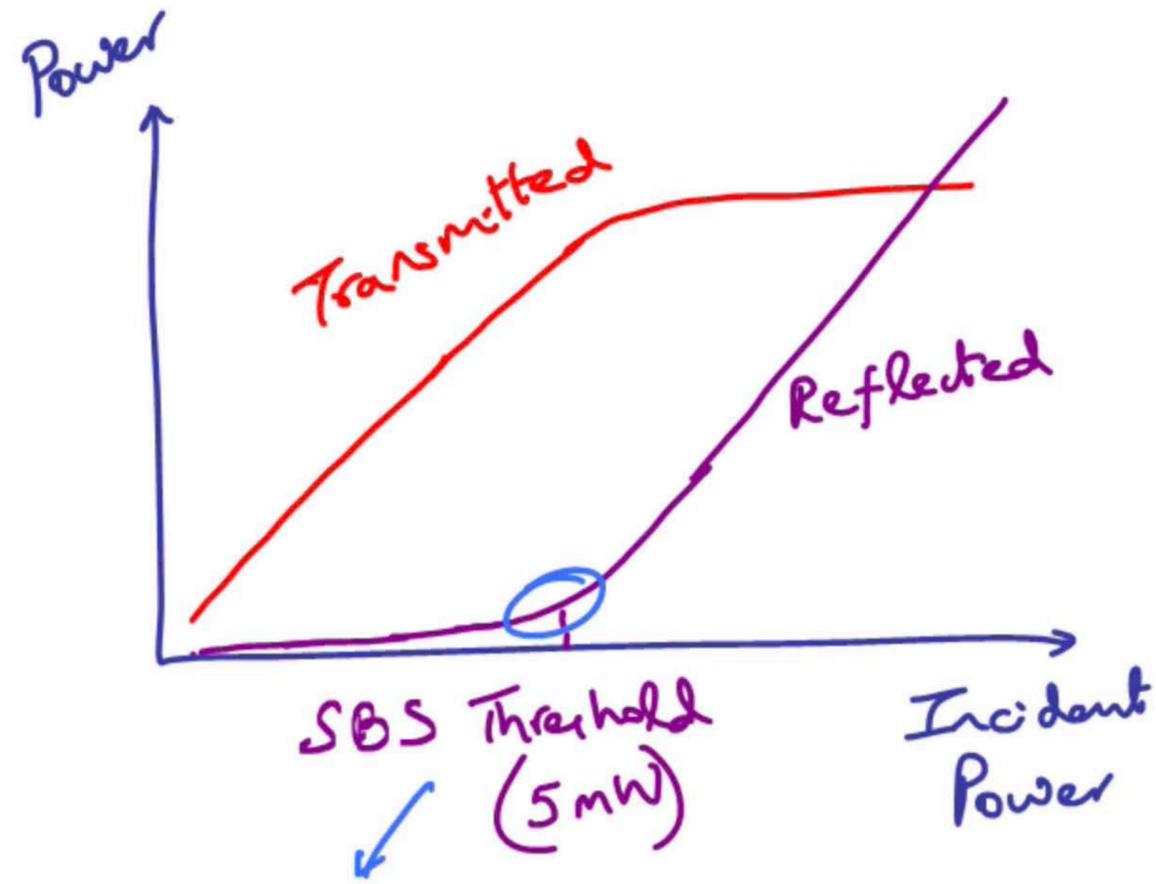
$$V_A = 6 \text{ km/s}$$

$$\lambda_p = 1.5 \text{ }\mu\text{m}$$

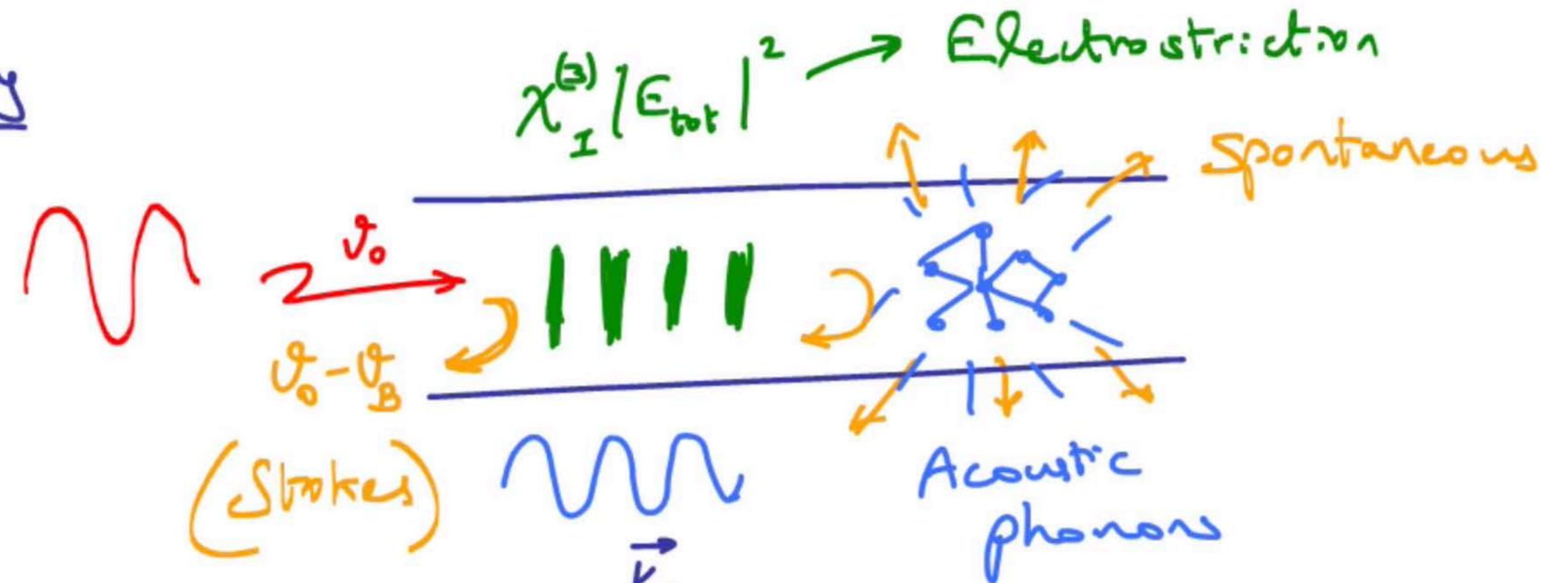
$$\Rightarrow \nu_B = 12 \text{ GHz}$$

$$\nu_B = \frac{2 n_{\text{eff}} V_A}{\lambda_p}$$

Stimulated Brillouin Scattering



If source is highly coherent
 Optical Communications
 Optical Sensing



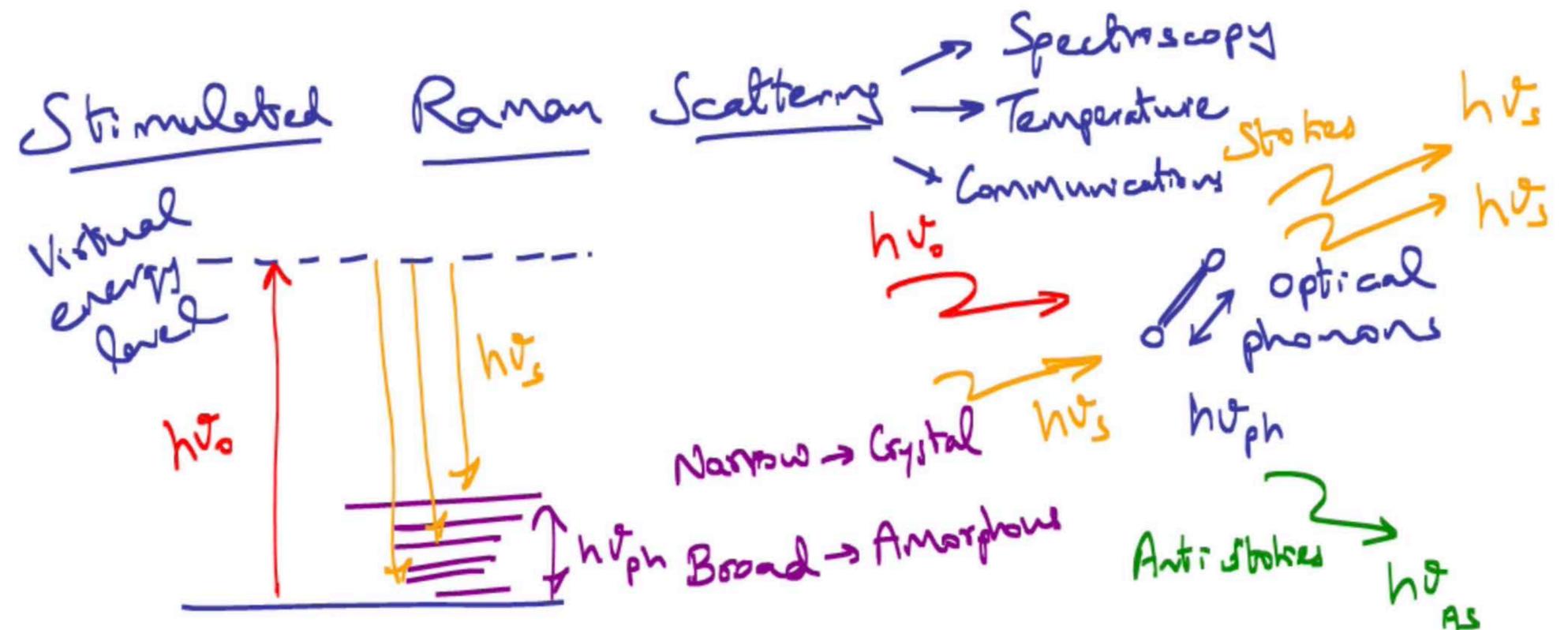
$$\vec{k}_p - \vec{k}_s = \vec{k}_A$$

$$\text{If } |\vec{k}_p| \approx |\vec{k}_s| \quad 2|\vec{k}_p| = |\vec{k}_A|$$

$$2 \cdot \frac{2\pi}{\lambda_p} n_{eff} = \frac{2\pi \nu_B}{V_A}$$

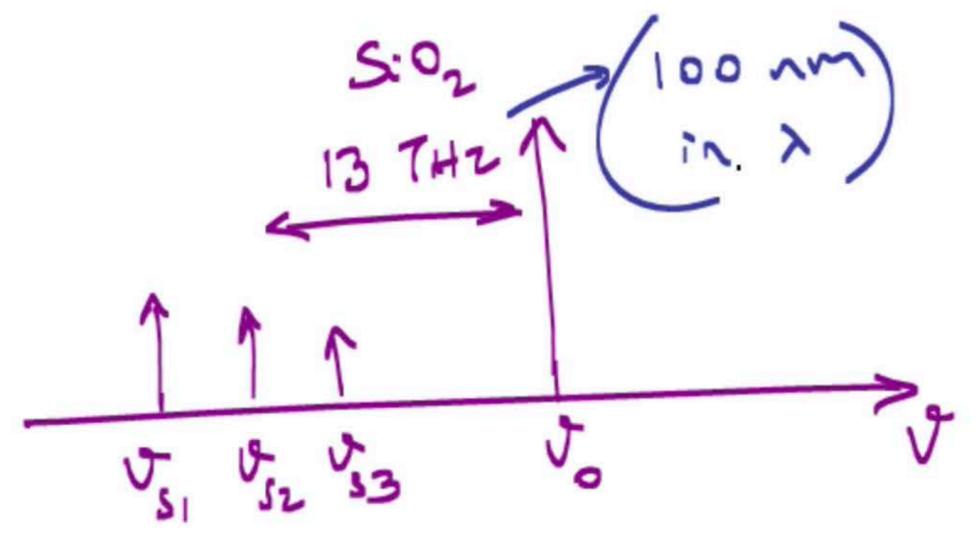
$n_{eff} \approx 1.5$
 $V_A = 6 \text{ km/s}$
 $\lambda_p = 1.5 \mu\text{m}$
 $\Rightarrow \nu_B = 12 \text{ GHz}$

$$\nu_B = \frac{2 \cdot n_{eff} \cdot V_A}{\lambda_p}$$

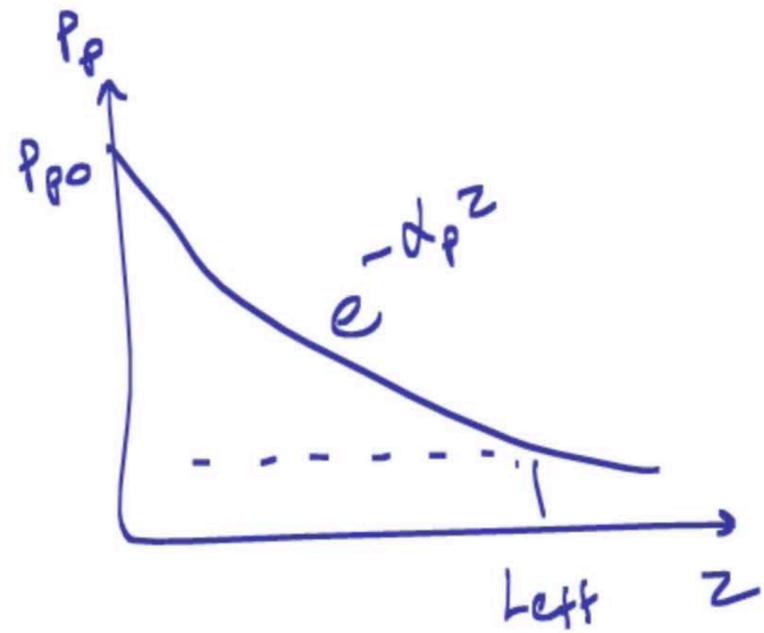


(Amplification)

Stokes scattering
 (10^{-7})



$$R = \frac{P_{AS}}{P_S} = \left(\frac{\lambda_s}{\lambda_{AS}} \right)^4 \exp\left(-\frac{h\nu_{ph}}{k_B T} \right)$$



$$\frac{dP_s}{dz} = g_R \frac{P_p}{A_{\text{eff}}} \cdot P_s - \alpha_s P_s$$

SRS Attenuation

Amplifier gain $G_R = \exp\left(\frac{g_R P_{po} \cdot L_{\text{eff}}}{A_{\text{eff}}}\right)$

To achieve 20 dB gain,

$$g_B = 6 \times 10^{-11} \text{ m/W}$$

$$g_R = 6 \times 10^{-14} \text{ m/W}$$

$$L_{\text{eff}} = 20 \text{ km}$$

$$A_{\text{eff}} = 50 \mu\text{m}^2$$

$$P_{po} = \underline{\underline{0.2 \text{ W}}}$$