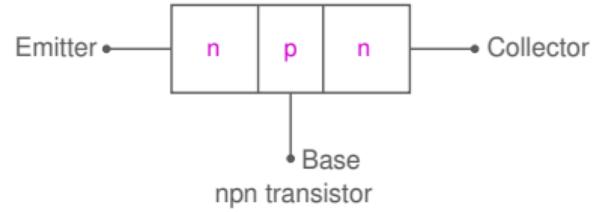
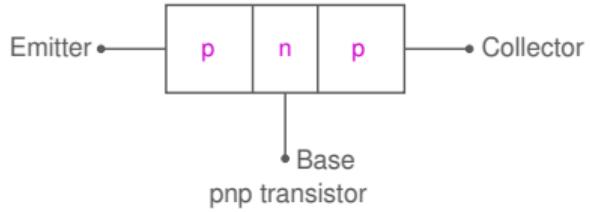
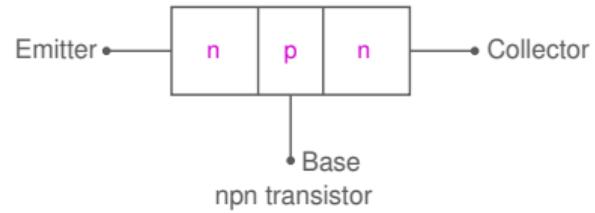
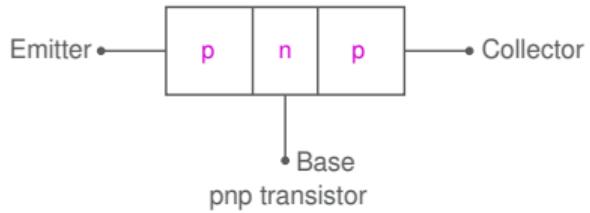


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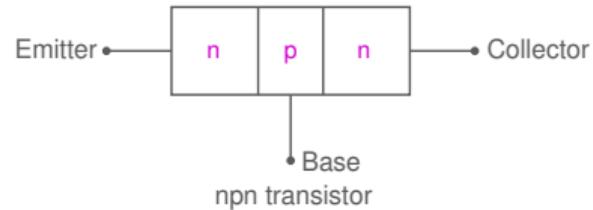
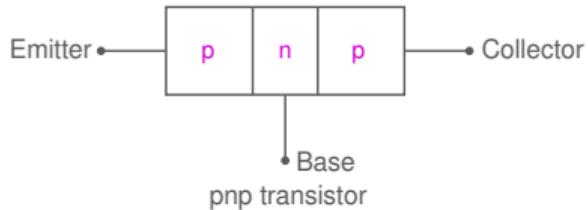


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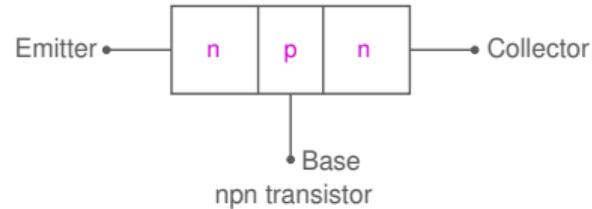
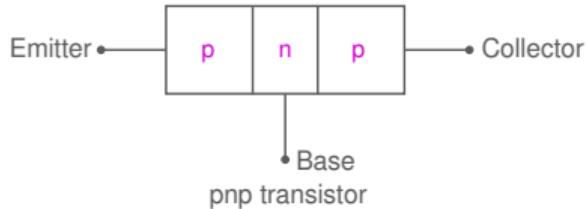
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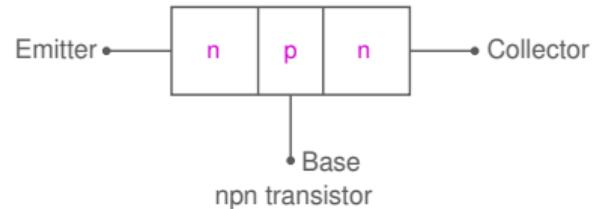
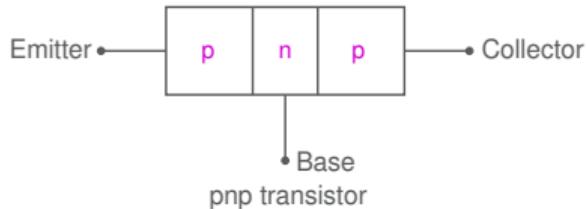


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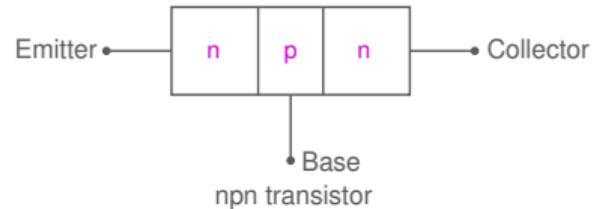
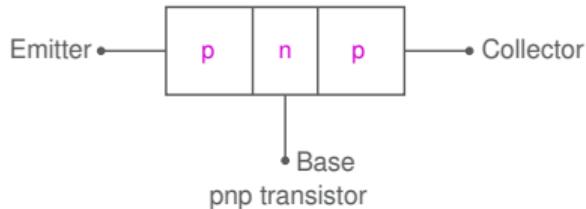
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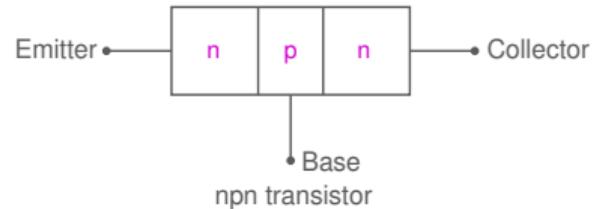
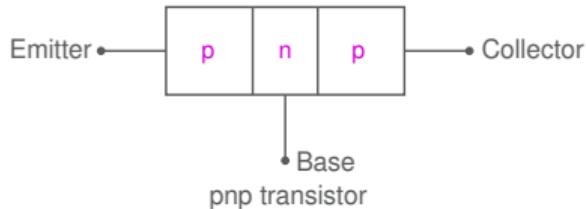
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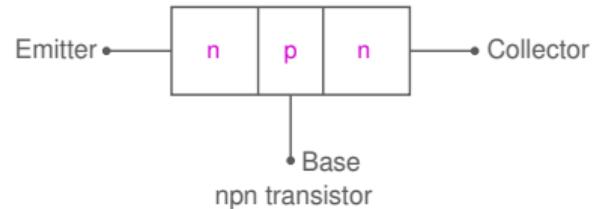
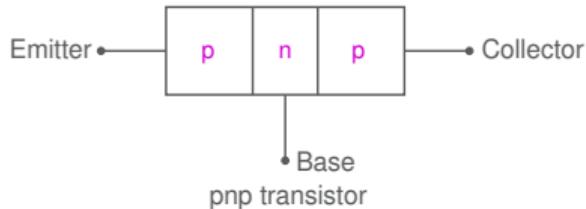
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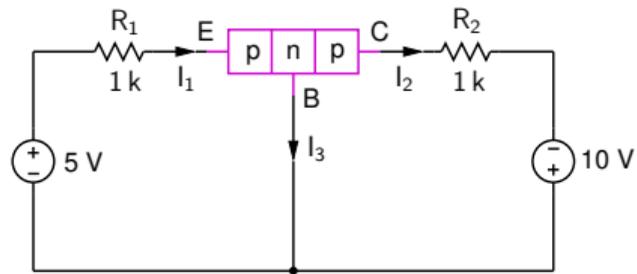
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**WRONG!** Let us see why.

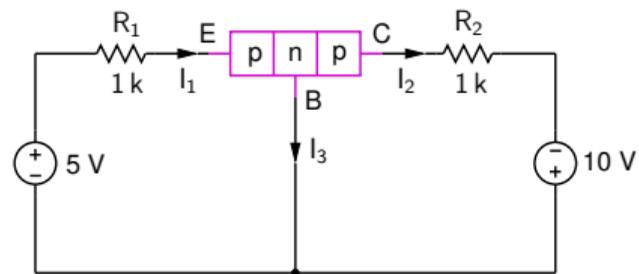
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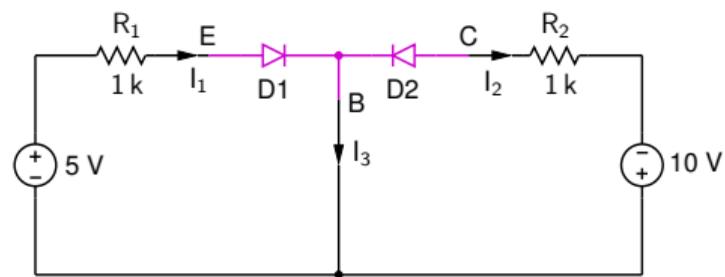


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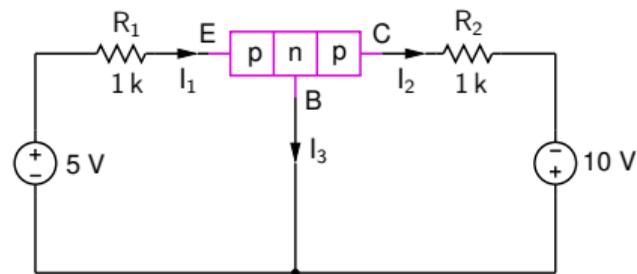


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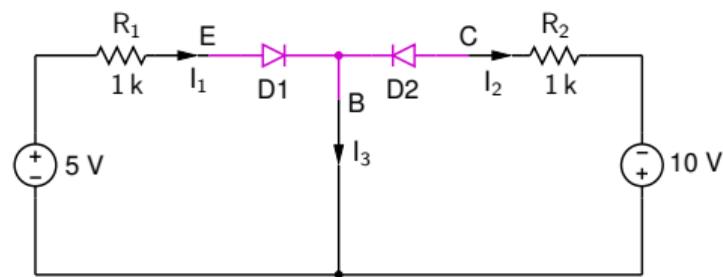


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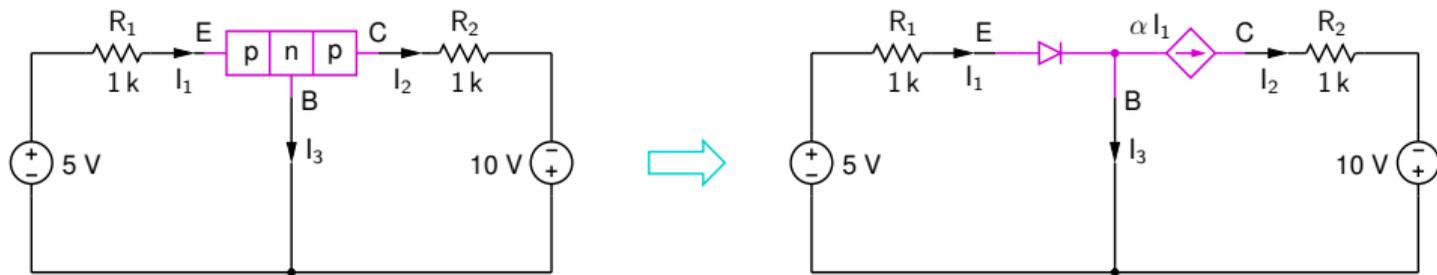
Assuming  $V_{on} = 0.7 V$  for D1, we get

$$I_1 = \frac{5V - 0.7V}{R_1} = 4.3 \text{ mA},$$

$I_2 = 0$  (since D2 is reverse biased), and  $I_3 \approx I_1 = 4.3 \text{ mA}$ .

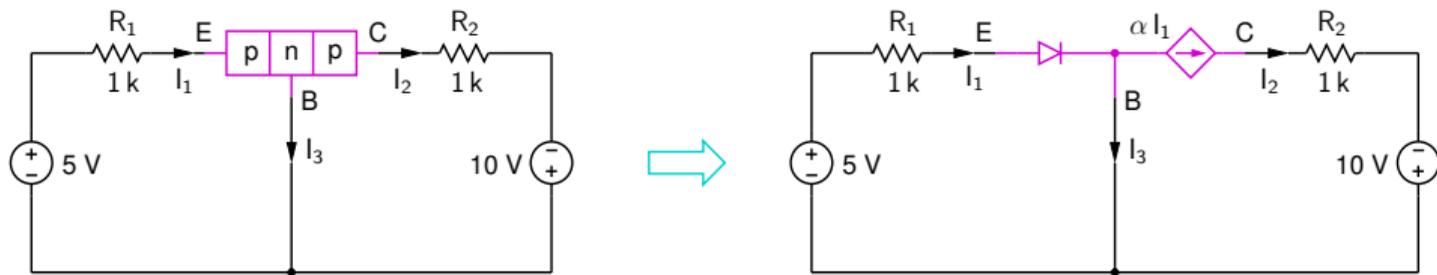
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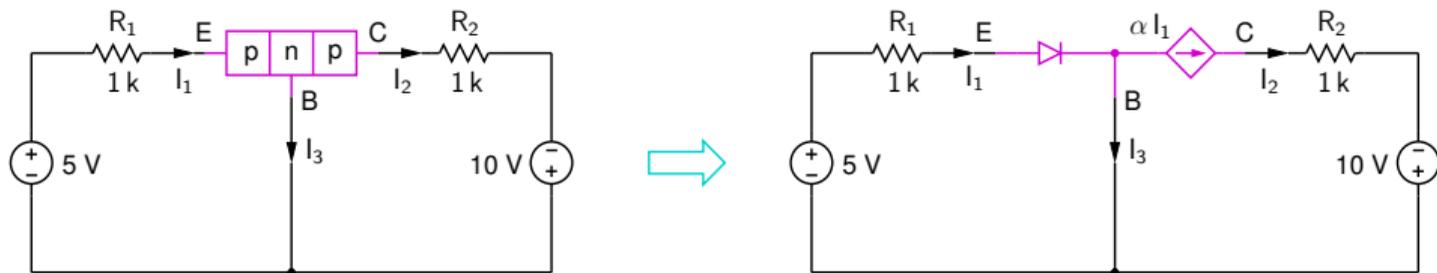


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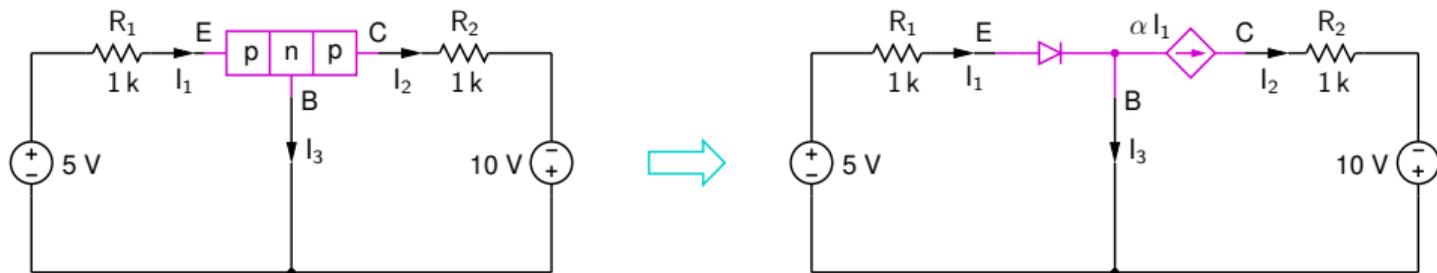
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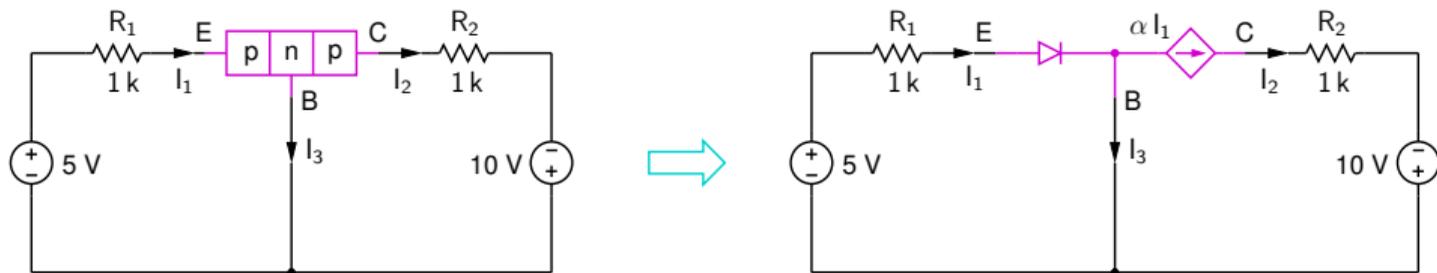
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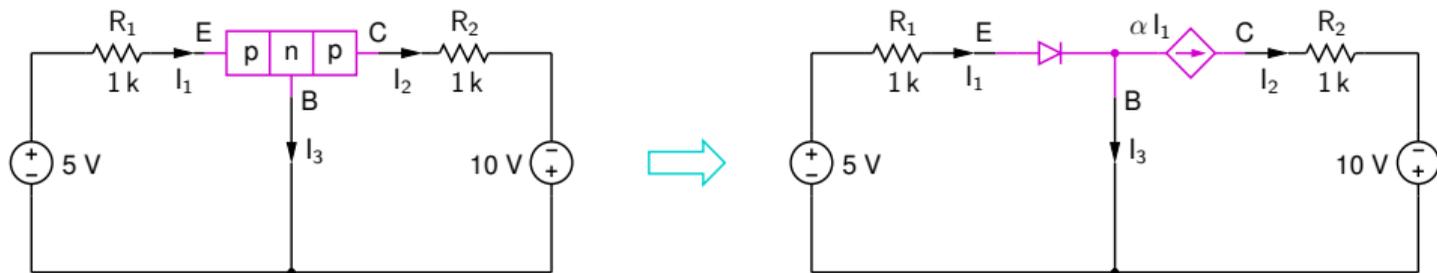
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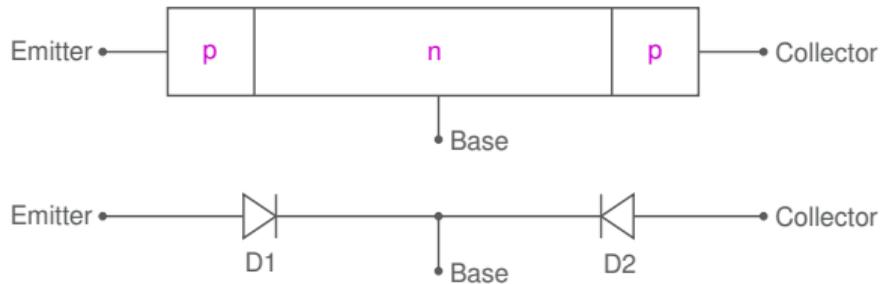
Conclusion: A BJT is NOT the same as two diodes connected back-to-back (although it does have two *p-n* junctions).

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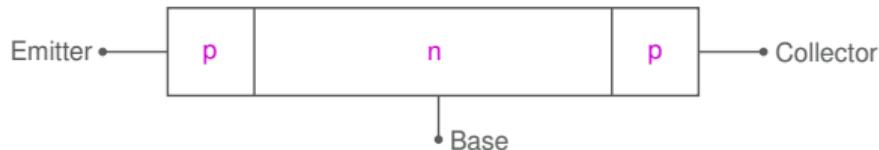
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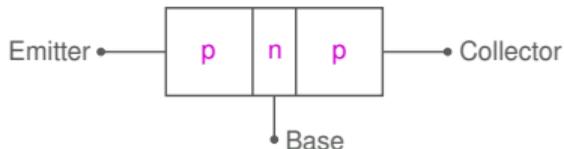
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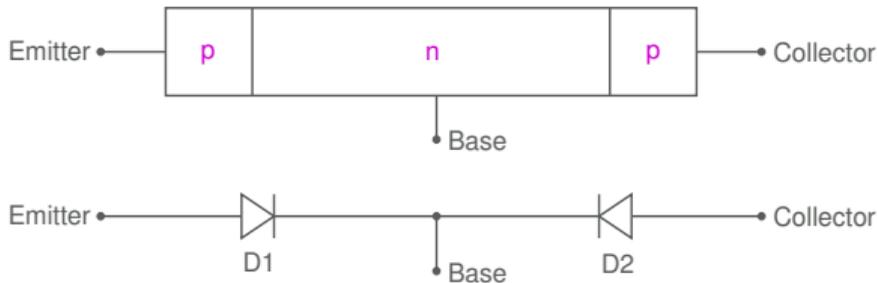
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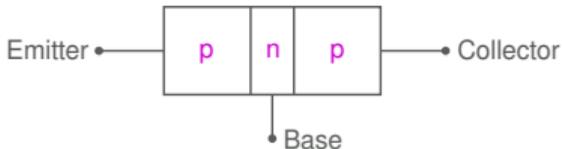
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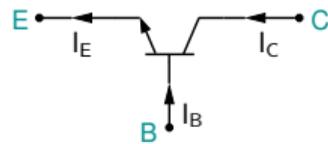
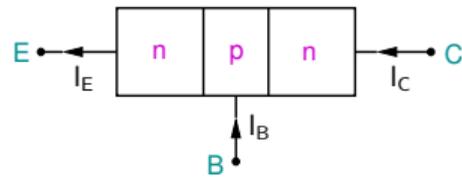
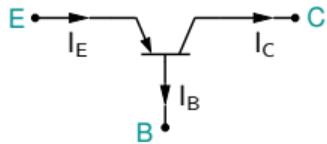
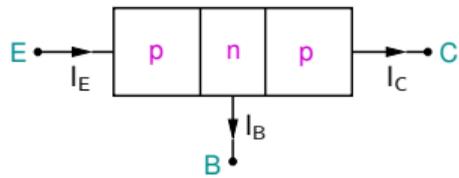


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- \* Later, we will look at the “Ebers-Moll model” of a BJT, which is a fairly accurate representation of the transistor action.

# BJT in active mode



## BJT in active mode



\* In the active mode of a BJT, the B-E junction is under forward bias, and the B-C junction is under reverse bias.

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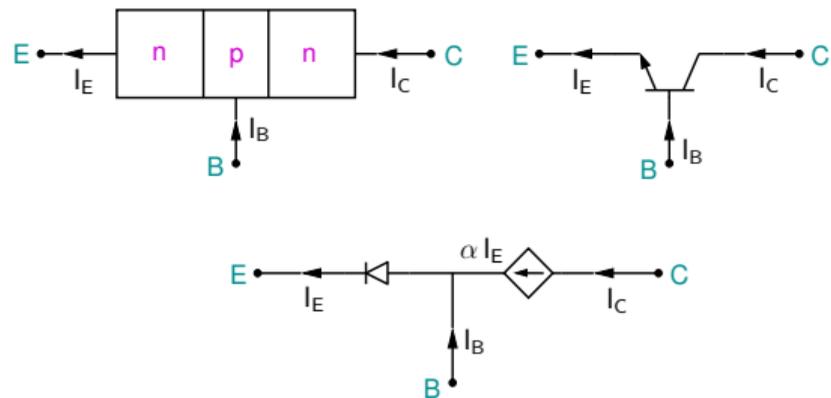
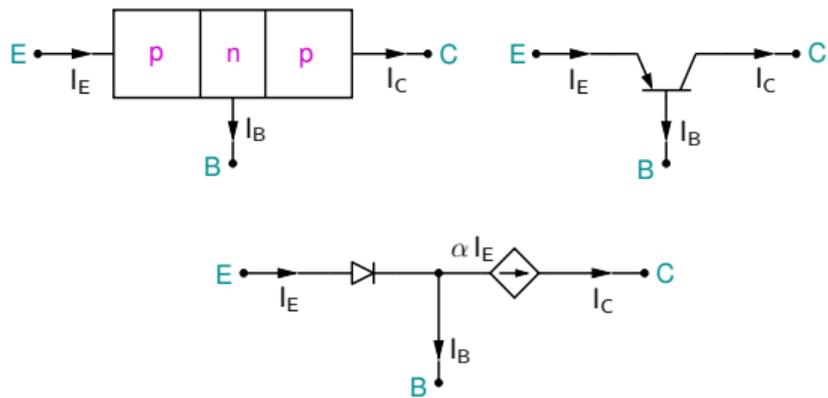
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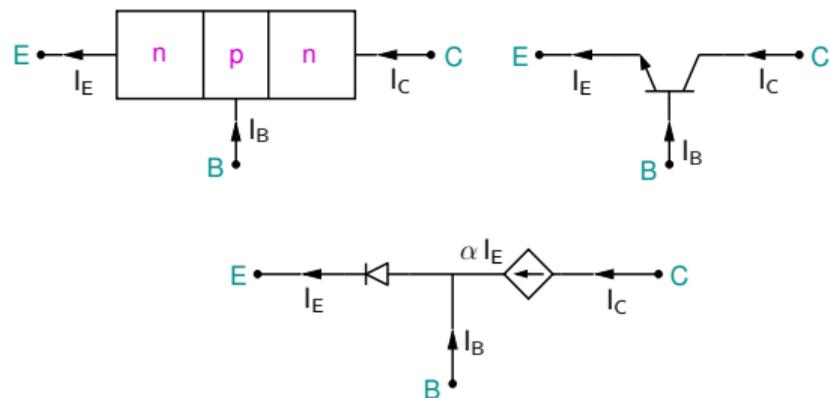
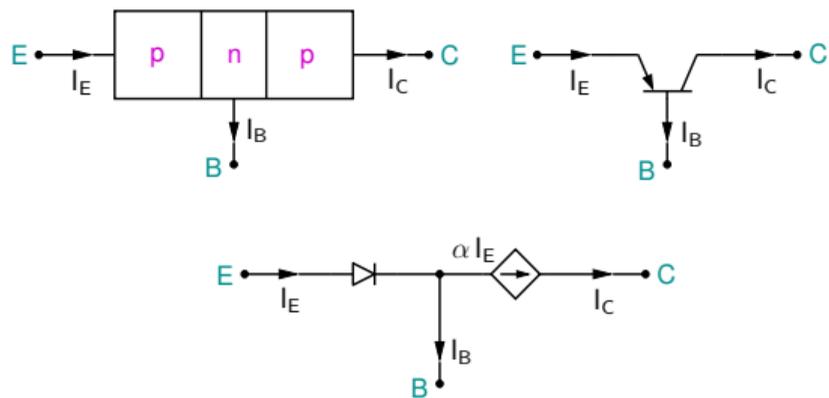


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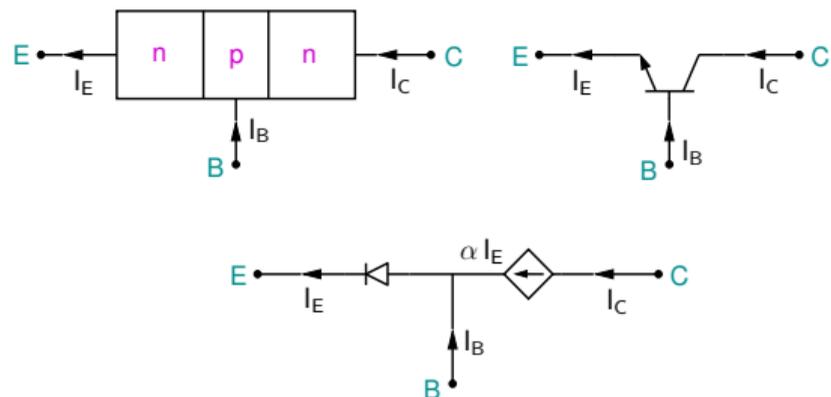
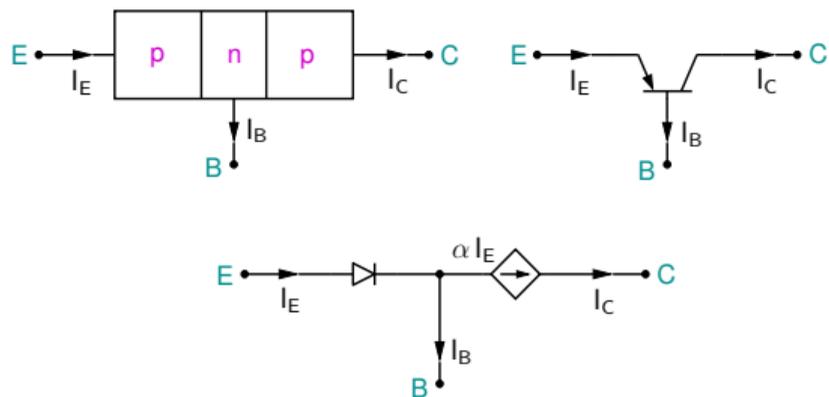


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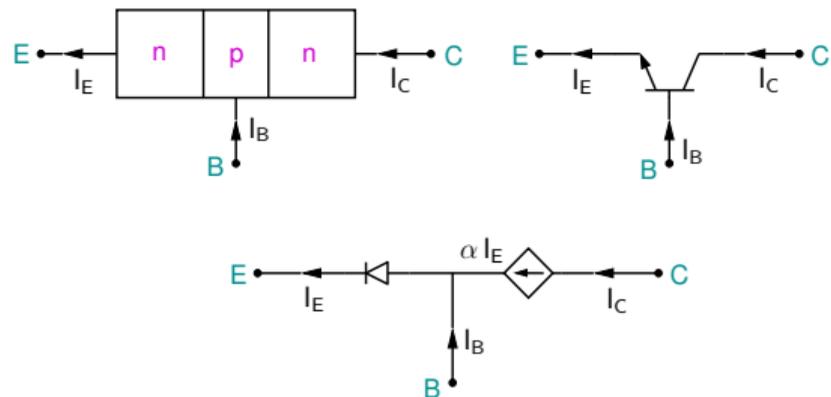
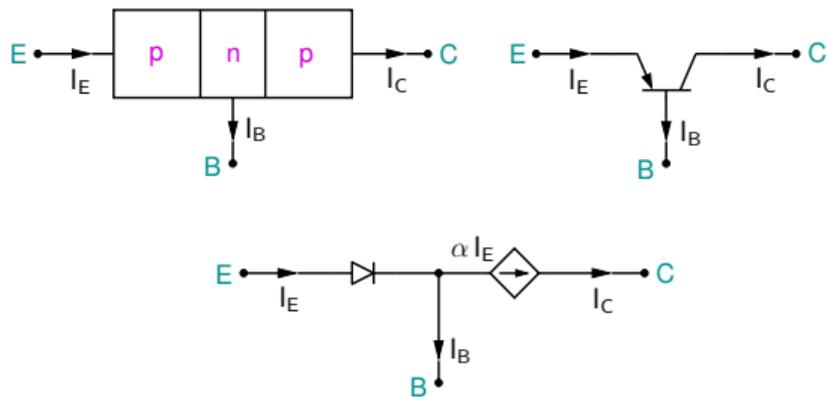
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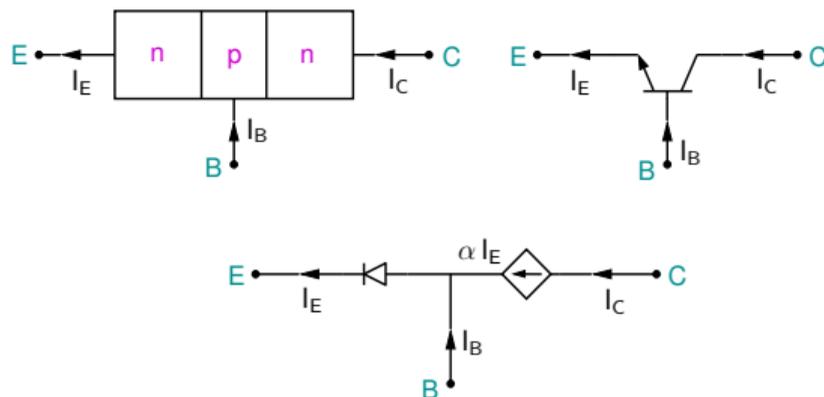
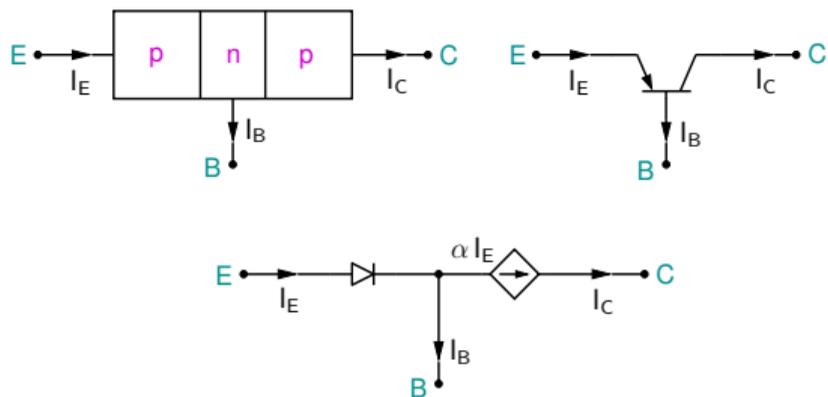
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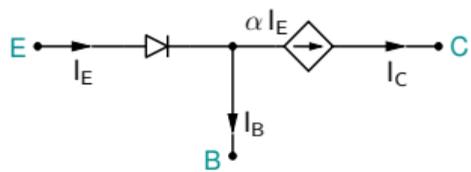
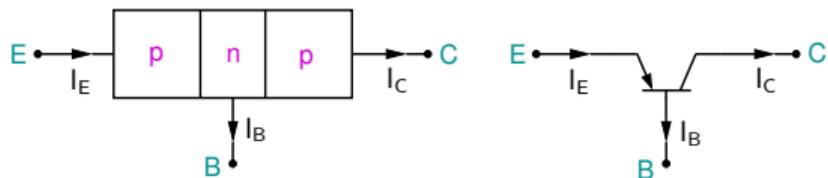
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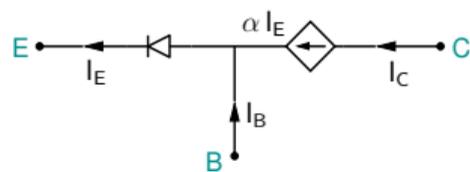
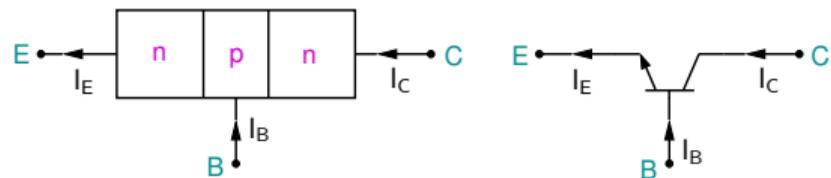
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\*  $\beta$  is a function of  $I_C$  and temperature. However, we will generally treat it as a constant, a useful approximation to simplify things and still get a good insight.

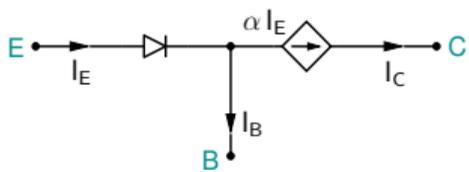
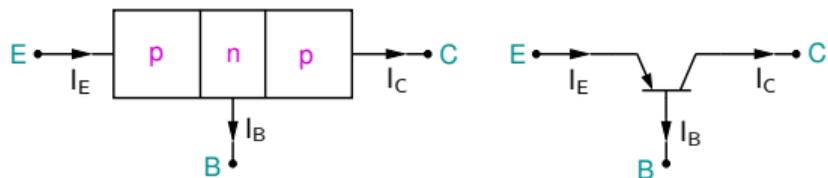
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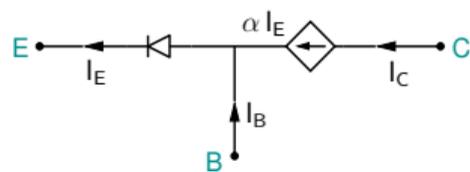
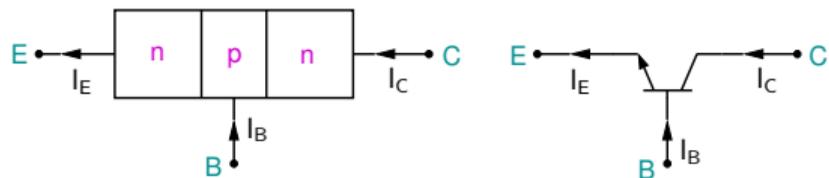


# BJT in active mode

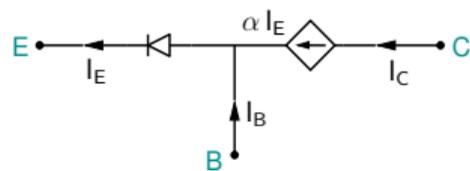
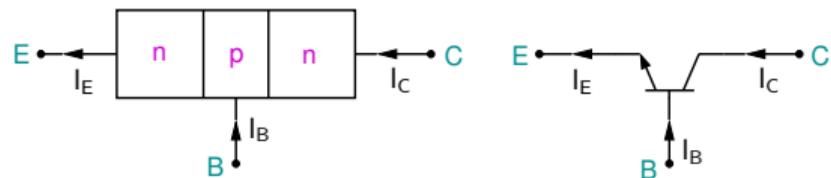
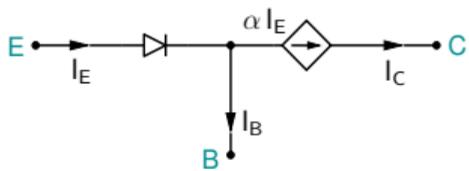
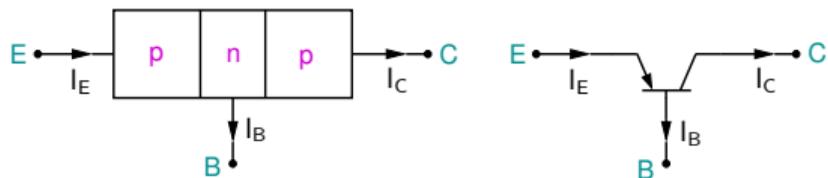


$$\beta = \frac{I_C}{I_B} = \frac{\alpha}{1 - \alpha}$$

$\alpha$	$\beta$
0.9	9
0.95	19
0.99	99
0.995	199



# BJT in active mode

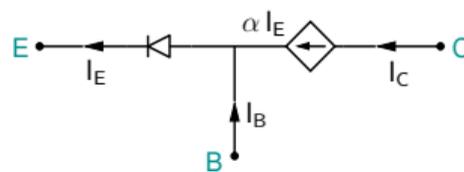
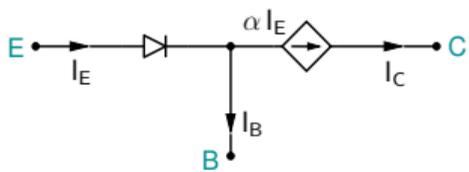
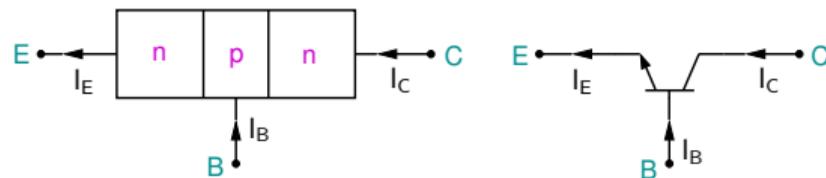
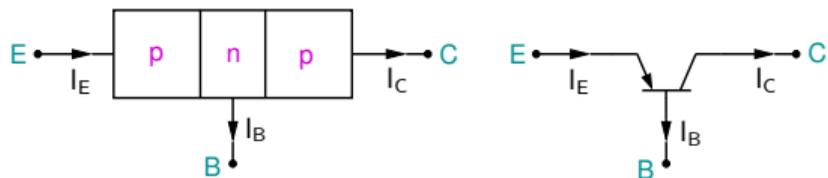


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\*  $\beta$  increases substantially as  $\alpha \rightarrow 1$ .

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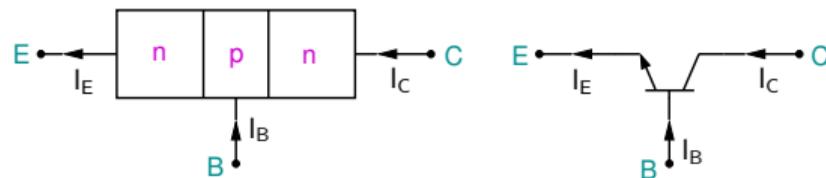
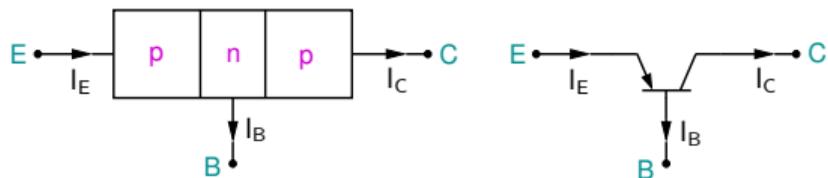


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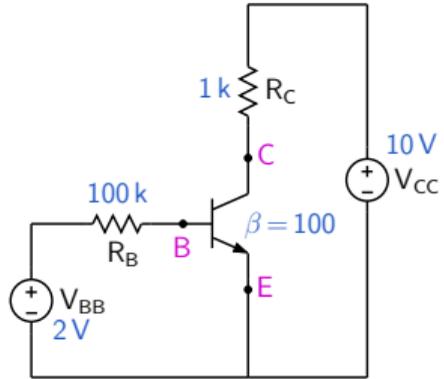


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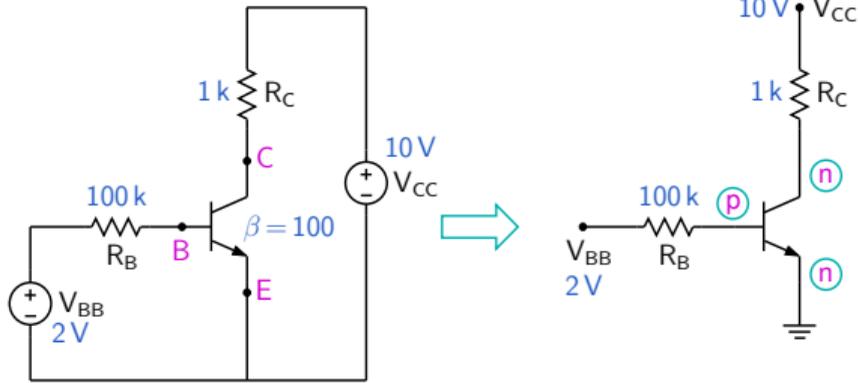
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- \*  $\beta$  increases substantially as  $\alpha \rightarrow 1$ .
- \* Transistors are generally designed to get a high value of  $\beta$  (typically 100 to 250, but can be as high as 2000 for "super- $\beta$ " transistors).
- \* A large  $\beta \Rightarrow I_B \ll I_C$  or  $I_E$  when the transistor is in the active mode.

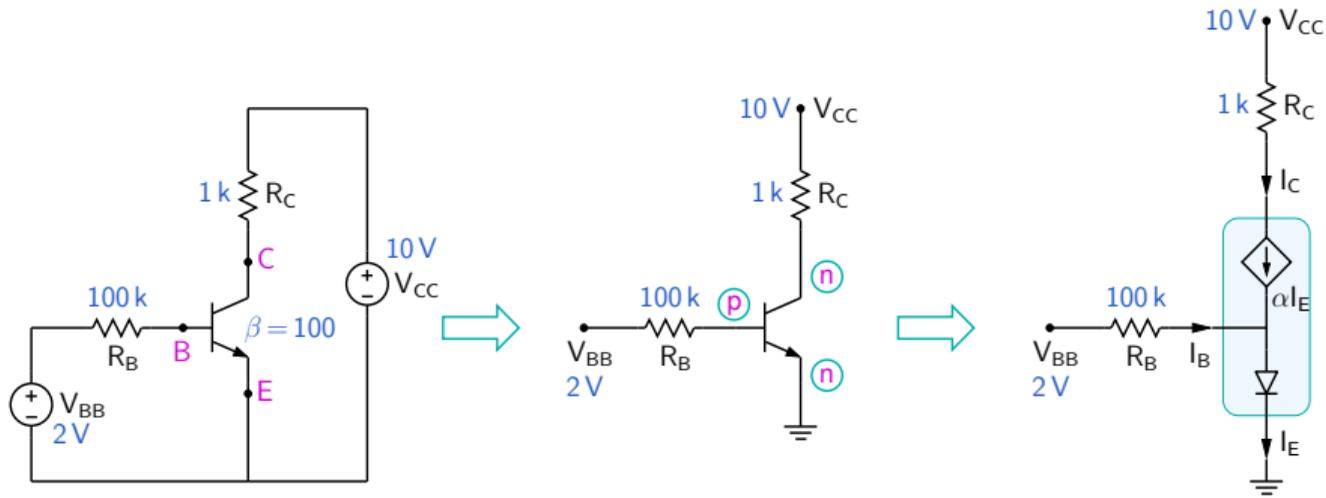
## A simple BJT circuit



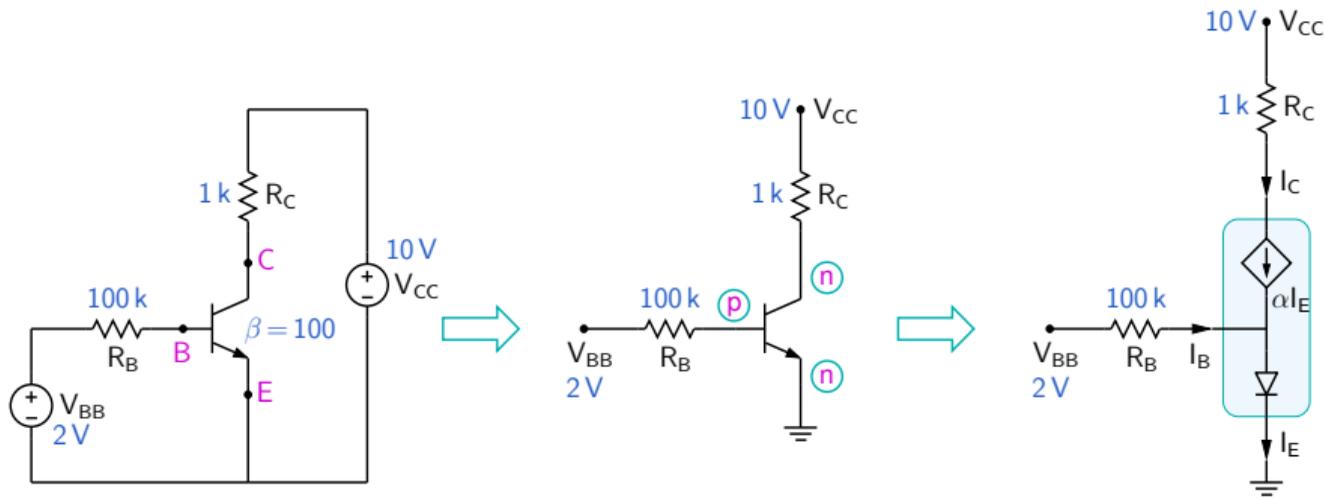
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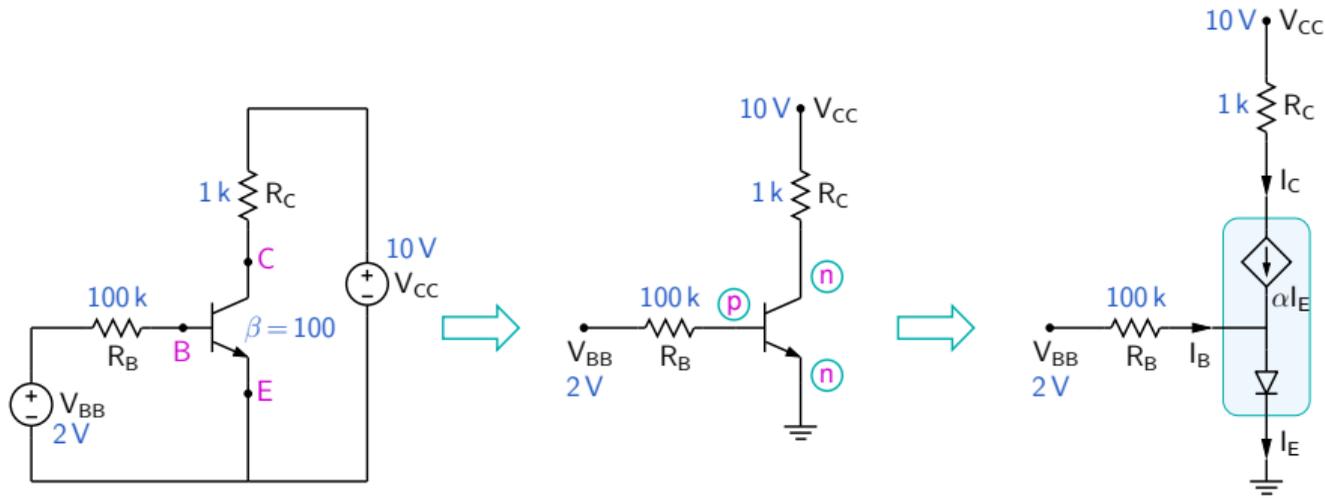


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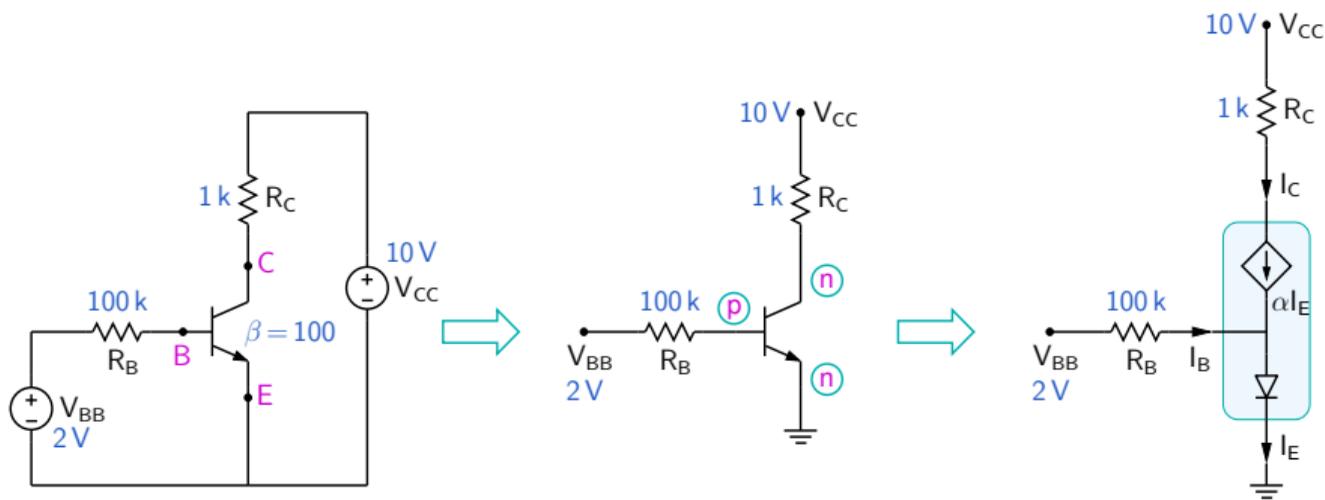
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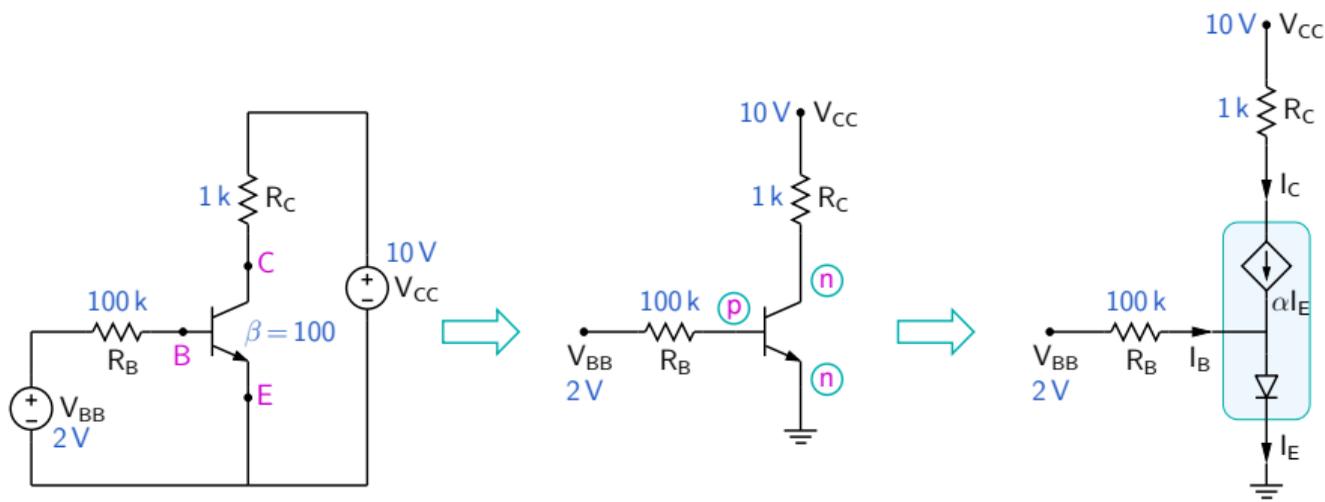


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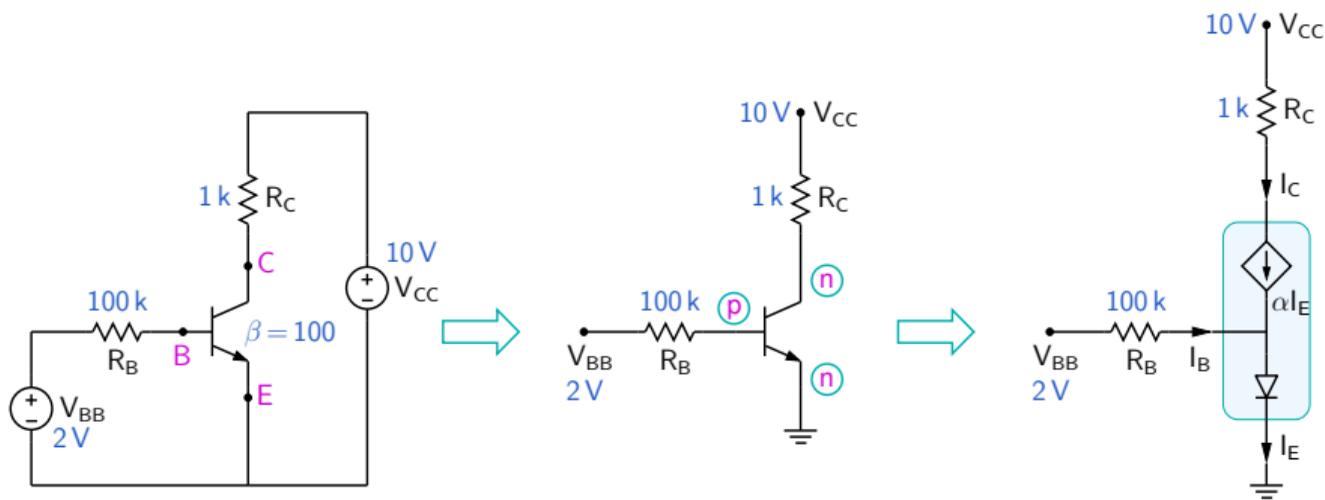
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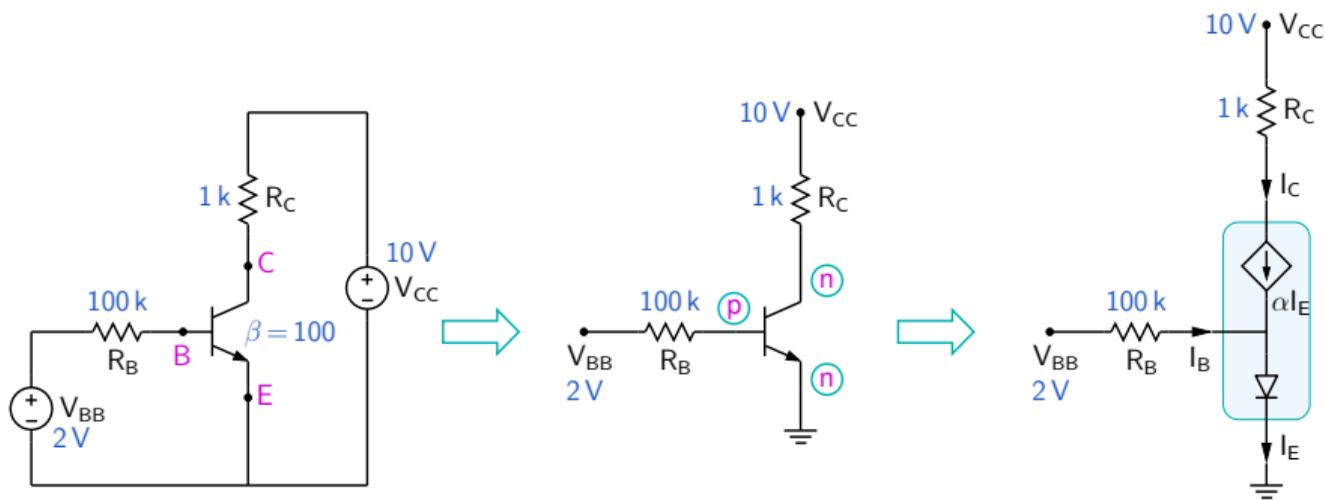
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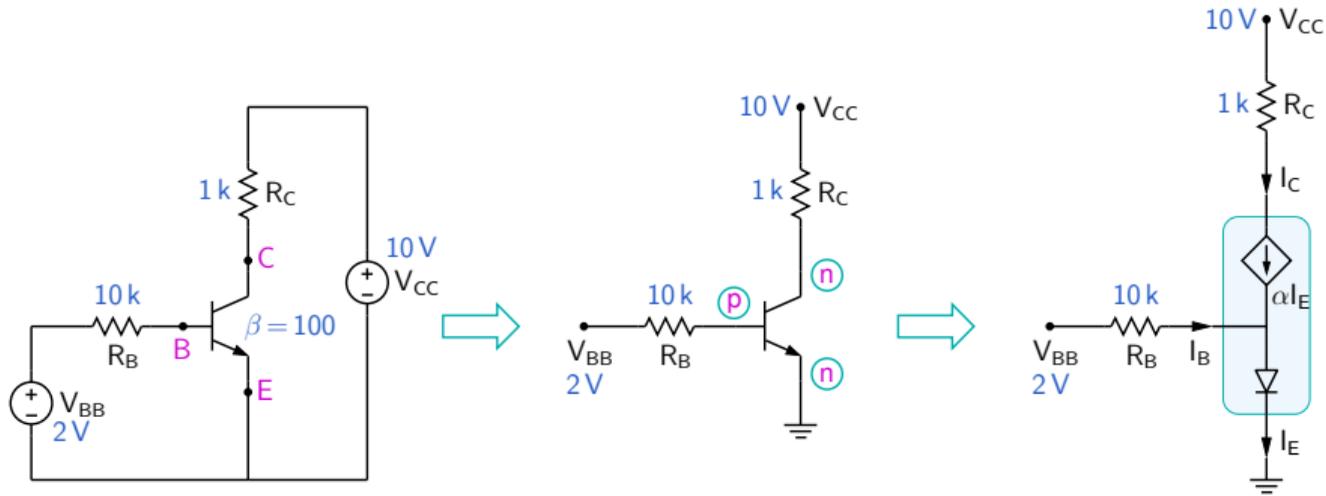
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$$V_{BC} = V_B - V_C = 0.7 \text{ V} - 8.7 \text{ V} = -8.0 \text{ V},$$

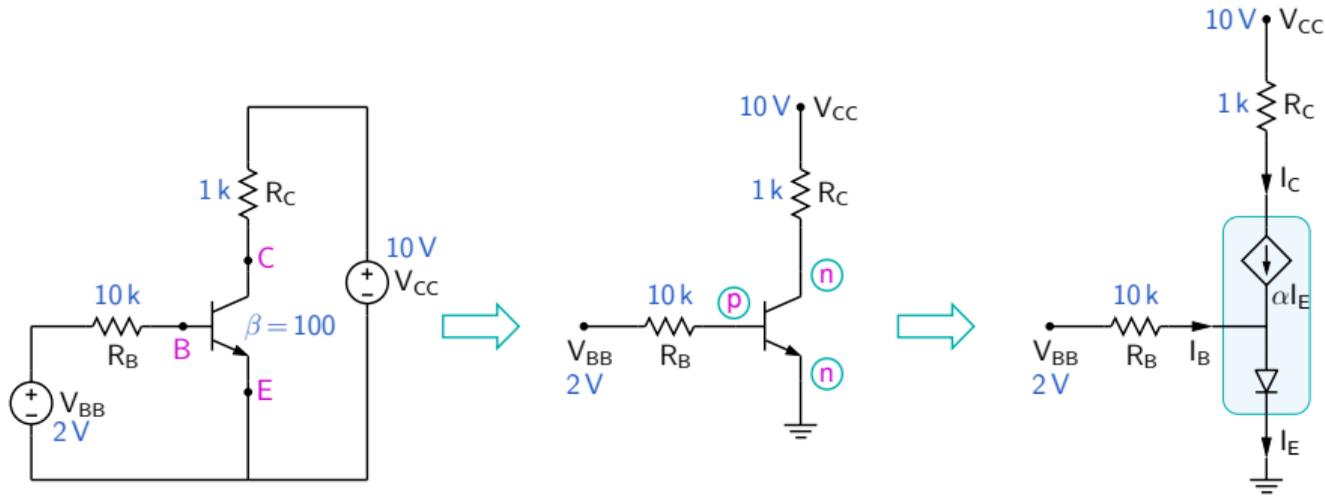
i.e., the B-C junction is indeed under reverse bias.

## A simple BJT circuit: continued



What happens if  $R_B$  is changed from 100 k to 10 k?

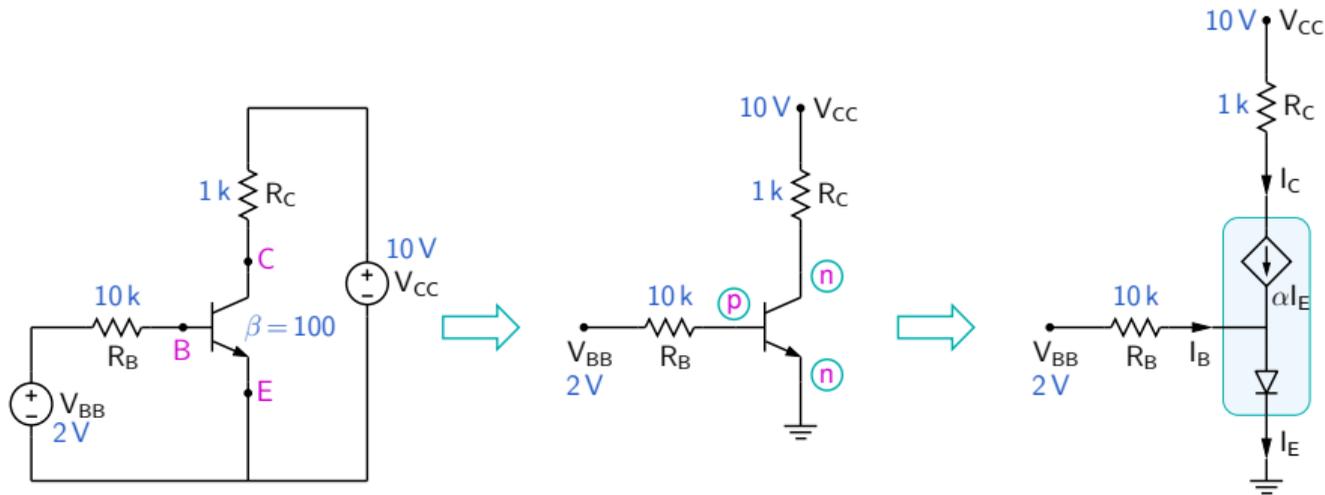
## A simple BJT circuit: continued



What happens if  $R_B$  is changed from  $100k$  to  $10k$ ?

Assuming the BJT to be in the active mode again, we have  $V_{BE} \approx 0.7V$ , and  $I_C = \beta I_B$ .

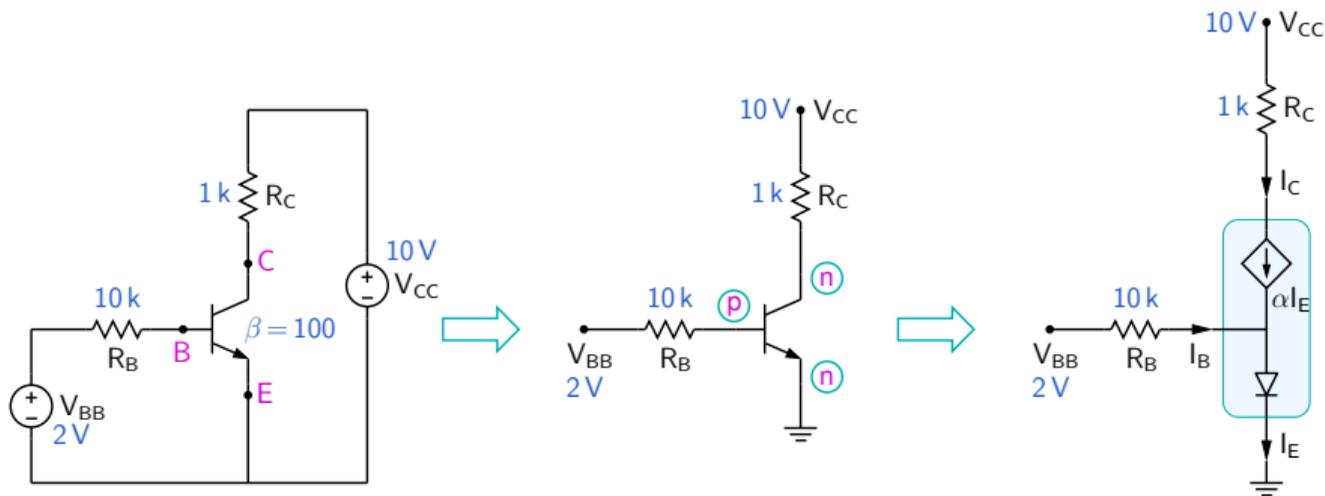
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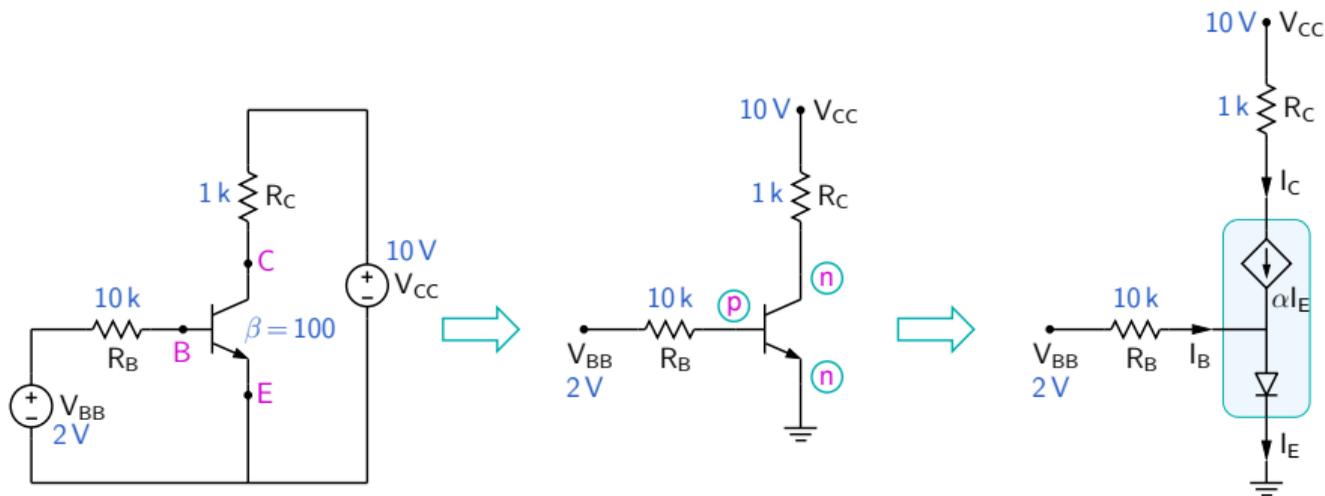
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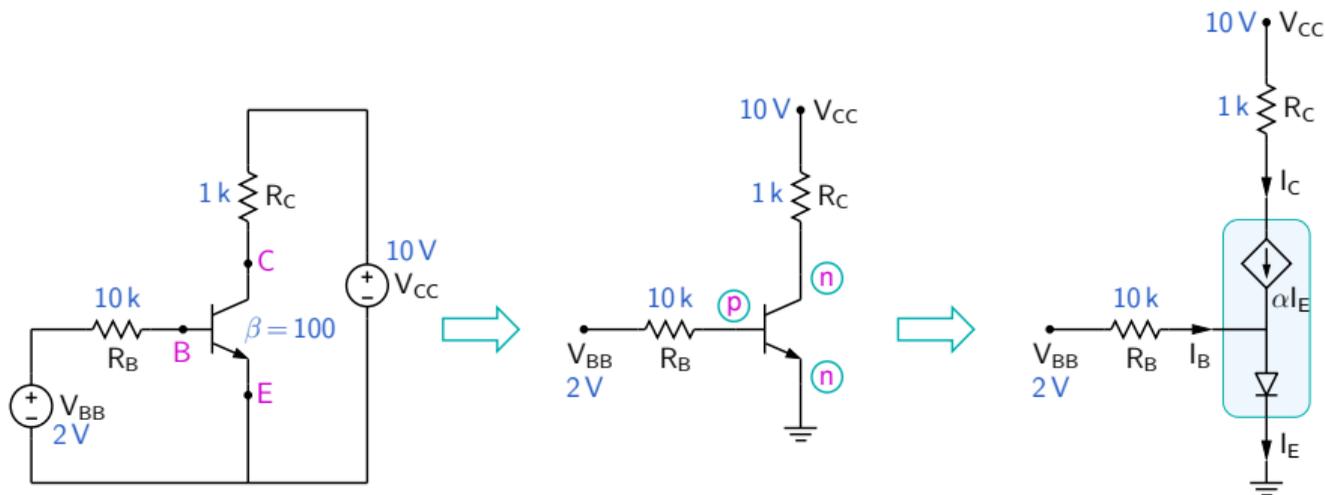


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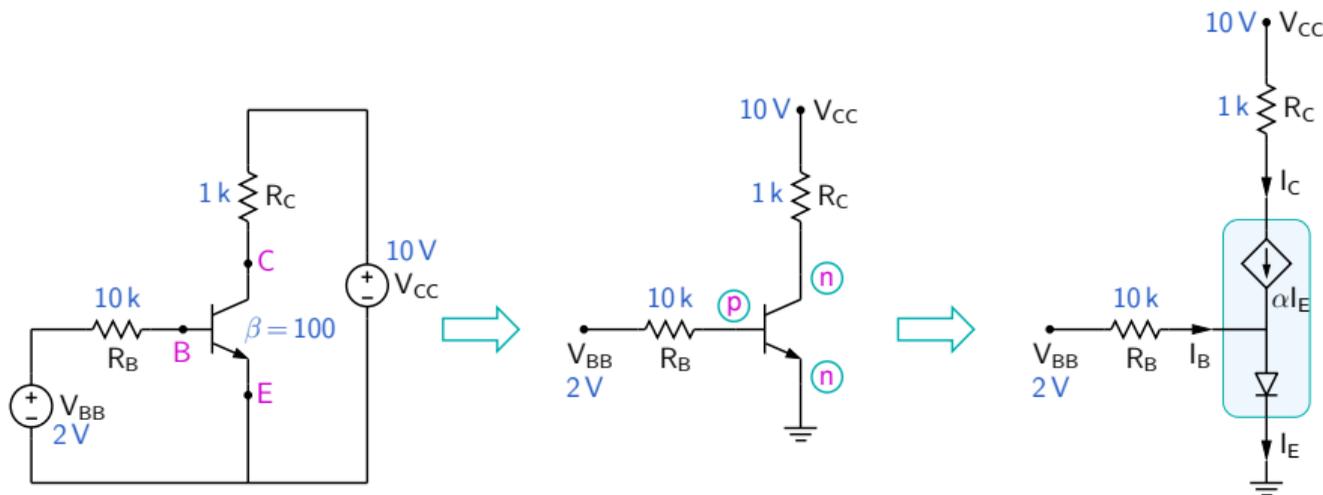
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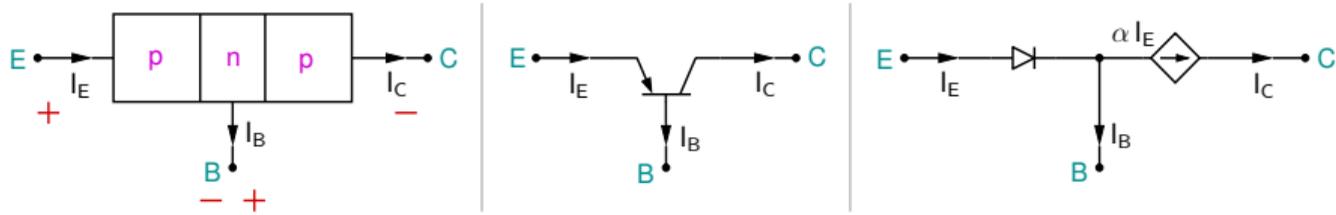
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$V_{BC}$  is not only positive, it is *huge*!

$\rightarrow$  The BJT cannot be in the active mode, and we need to take another look at the circuit.

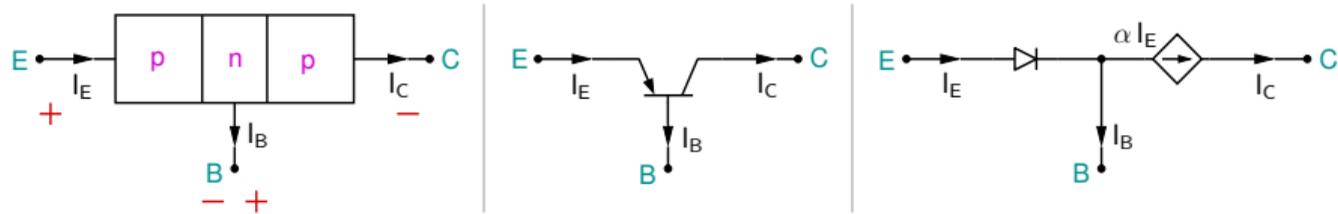
# Ebers-Moll model for a *pn*p transistor

Active mode ("forward" active mode): B-E in f.b. B-C in r.b.

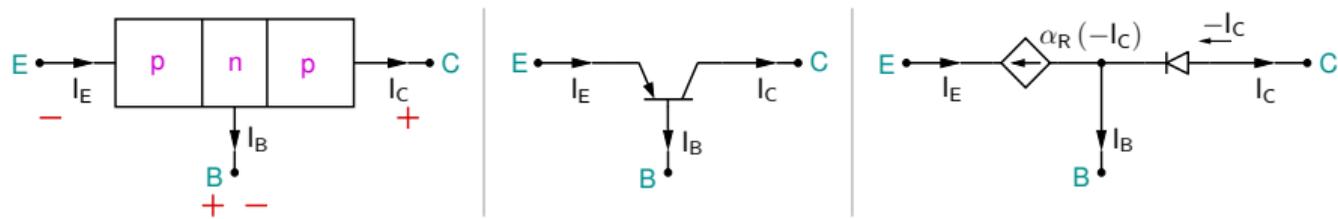


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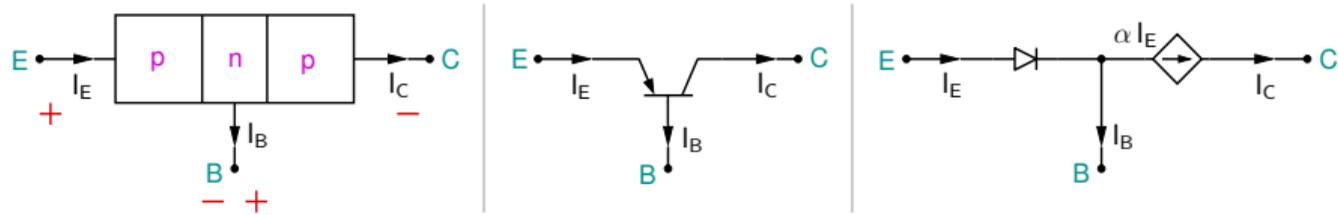


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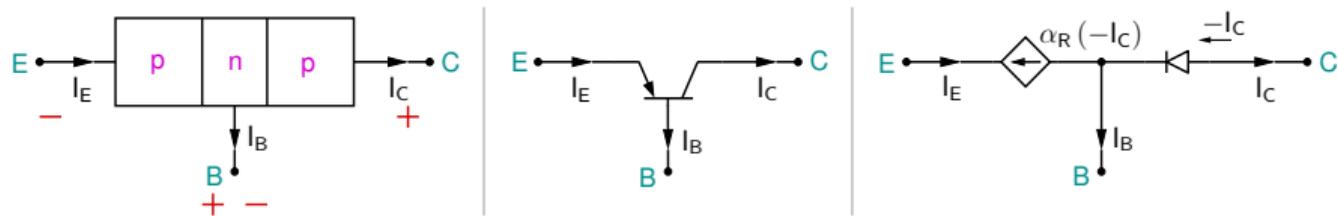


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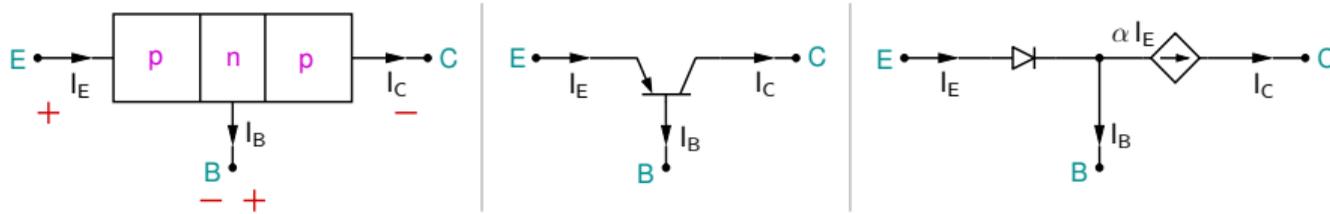
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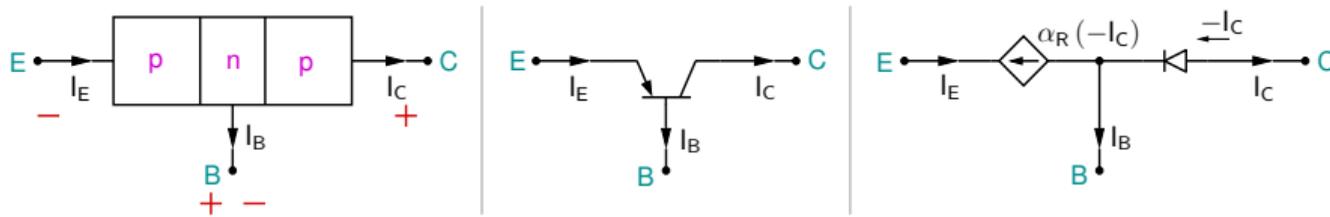
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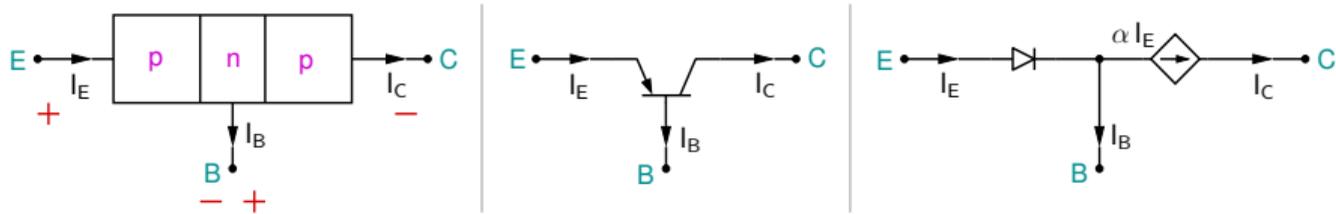


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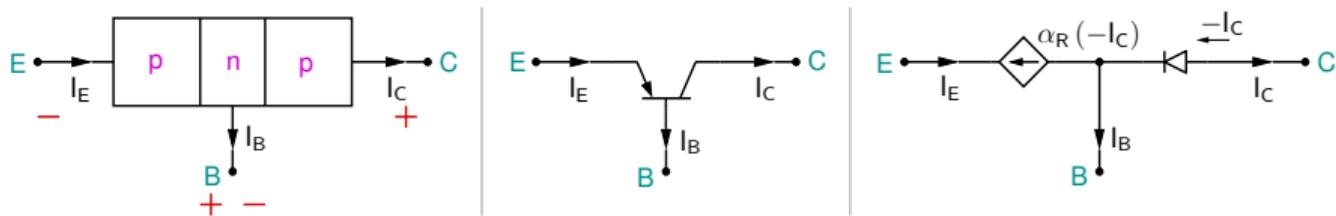
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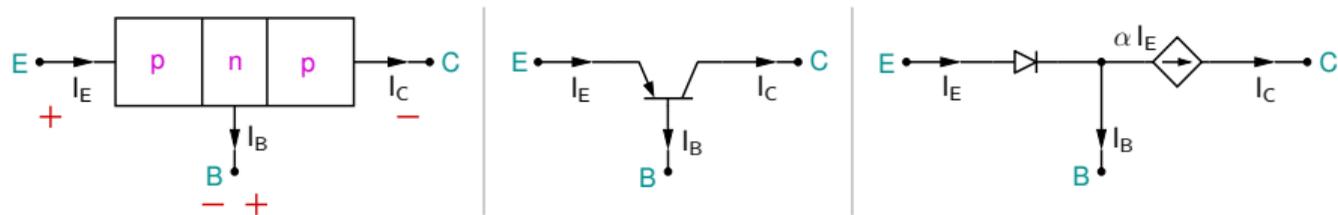
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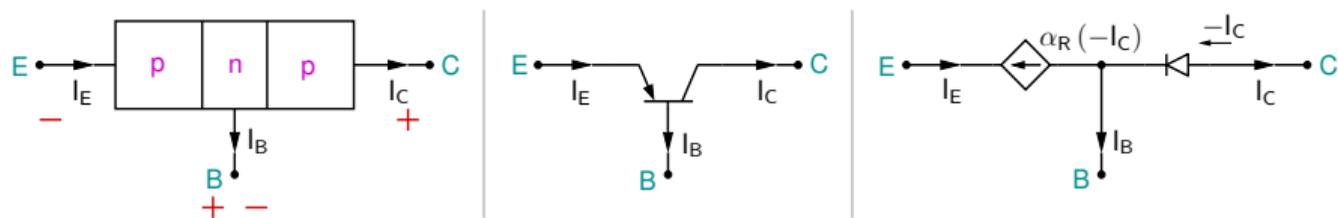
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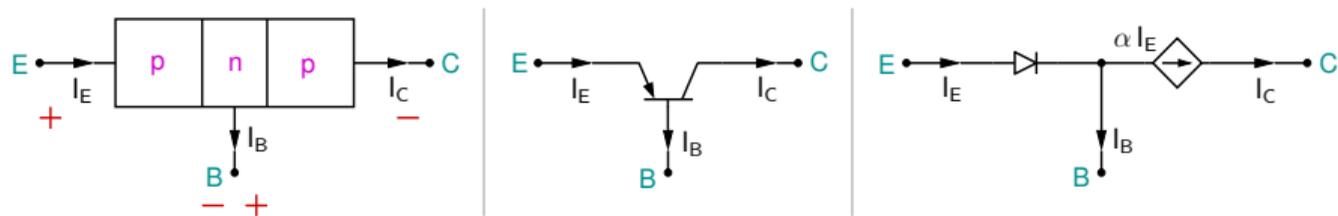
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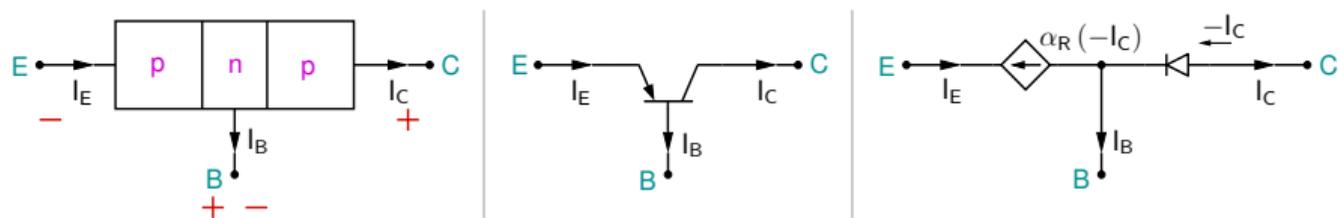
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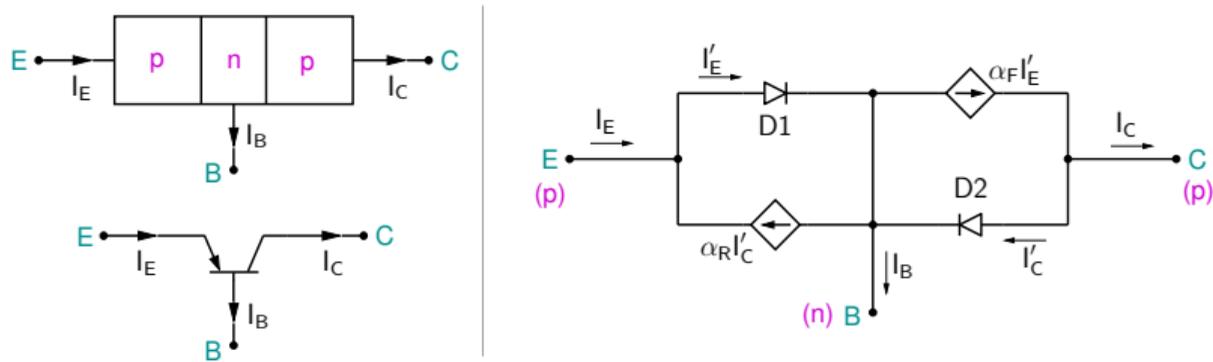
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In amplifiers, the BJT is biased in the forward active mode (simply called the "active mode") in order to make use of the higher value of  $\beta$  in that mode.

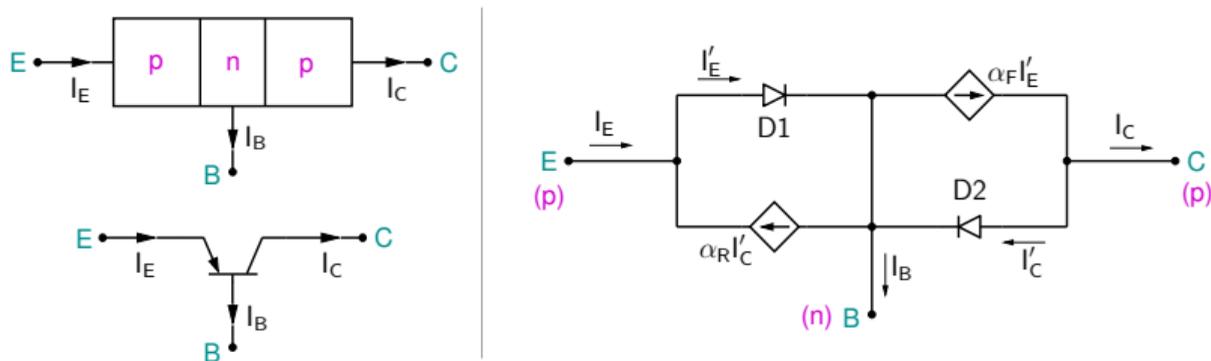
## Ebers-Moll model for a *pnp* transistor

The Ebers-Moll model combines the forward and reverse operations of a BJT in a single comprehensive model.



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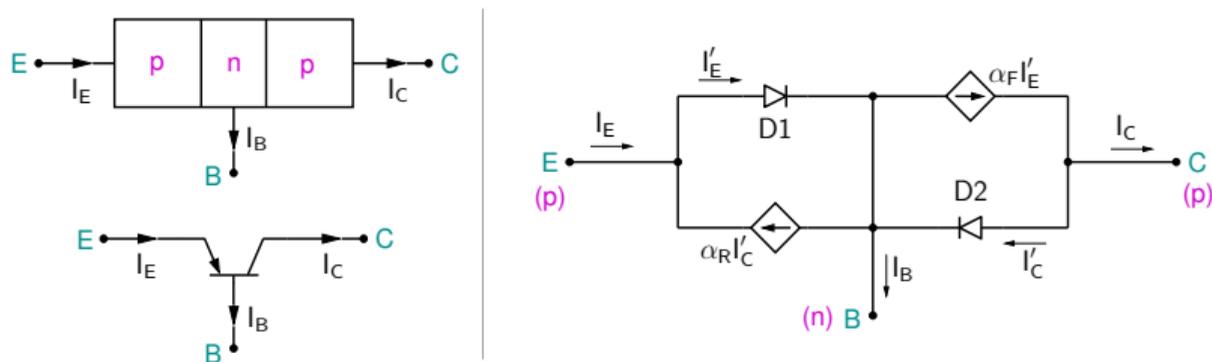


The currents  $I'_E$  and  $I'_C$  are given by the Shockley diode equation:

$$I'_E = I_{ES} \left[ \exp\left(\frac{V_{EB}}{V_T}\right) - 1 \right], \quad I'_C = I_{CS} \left[ \exp\left(\frac{V_{CB}}{V_T}\right) - 1 \right].$$

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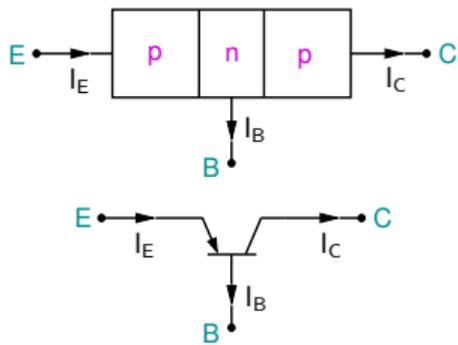


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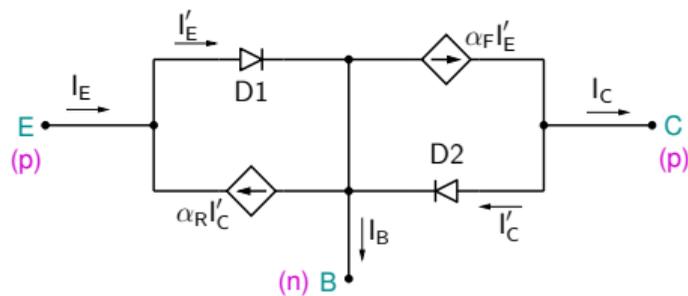
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Mode	B-E	B-C	
Forward active	forward	reverse	$I'_E \gg I'_C$
Reverse active	reverse	forward	$I'_C \gg I'_E$
Saturation	forward	forward	$I'_E$ and $I'_C$ are comparable.
Cut-off	reverse	reverse	$I'_E$ and $I'_C$ are negligible.

# Ebers-Moll model

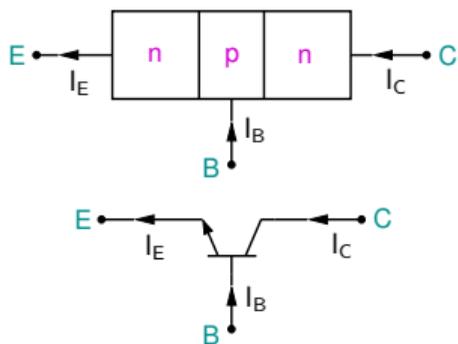


pnp transistor

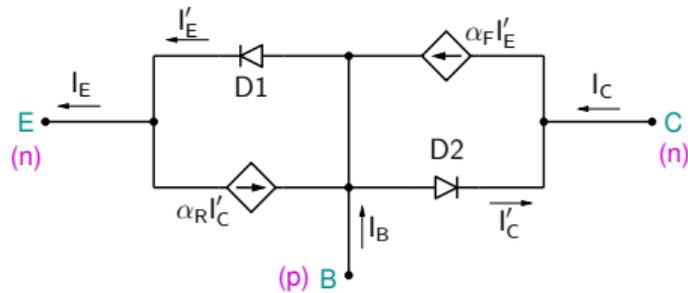


$$I'_E = I_{ES} [\exp(V_{EB}/V_T) - 1]$$

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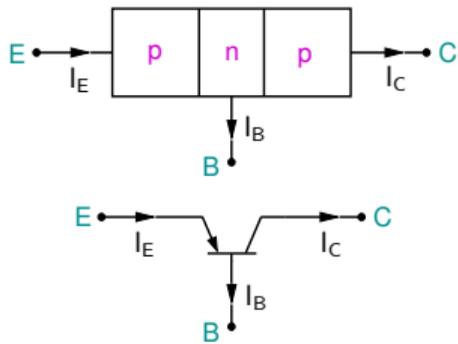


npn transistor

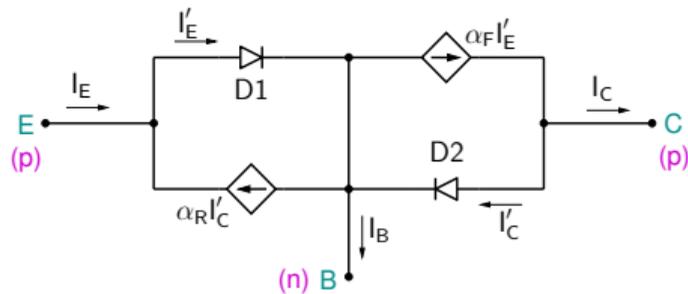


$$I'_E = I_{ES} [\exp(V_{BE}/V_T) - 1]$$

$$I'_C = I_{CS} [\exp(V_{BC}/V_T) - 1]$$

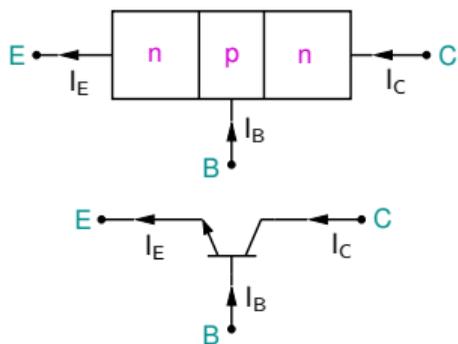


pnp transistor

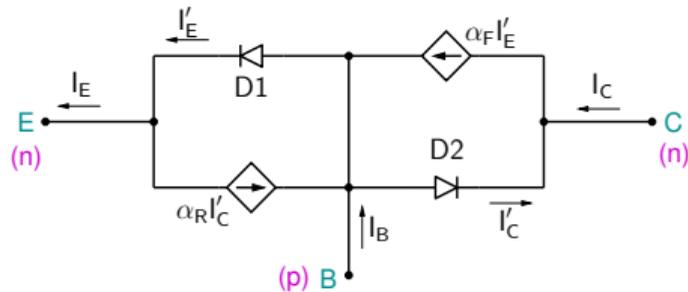


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npn transistor

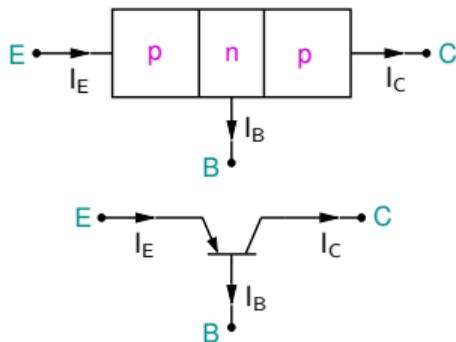


$$I'_E = I_{ES} [\exp(V_{BE}/V_T) - 1]$$

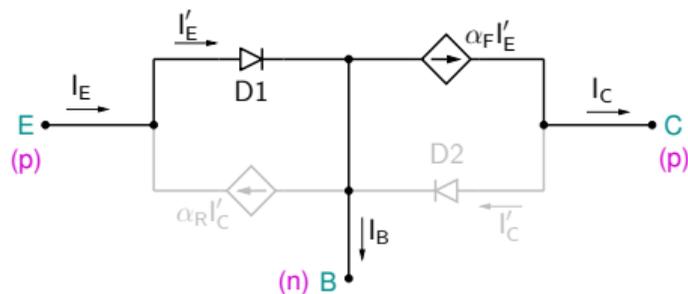
$$I'_C = I_{CS} [\exp(V_{BC}/V_T) - 1]$$



# Ebers-Moll model in active mode



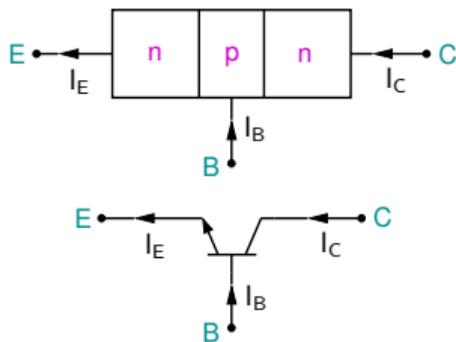
pn<sub>p</sub> transistor



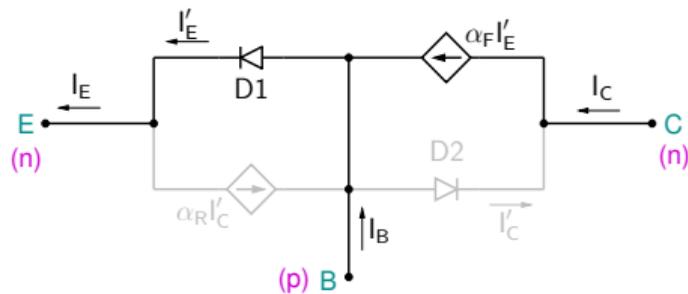
$$I'_E = I_{ES} [\exp(V_{EB}/V_T) - 1]$$

$$I'_C = I_{CS} [\exp(V_{CB}/V_T) - 1]$$

$$I_C = \alpha_F I_E = \beta_F I_B$$



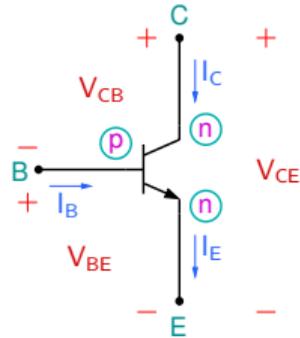
np<sub>n</sub> transistor

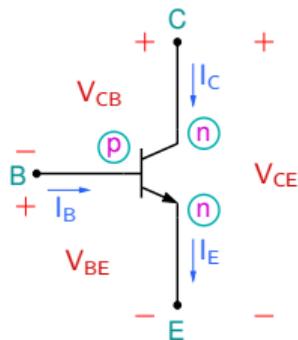


$$I'_E = I_{ES} [\exp(V_{BE}/V_T) - 1]$$

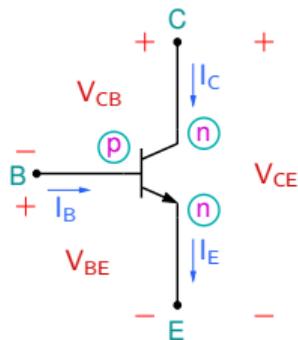
$$I'_C = I_{CS} [\exp(V_{BC}/V_T) - 1]$$

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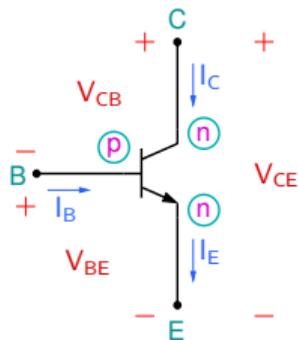




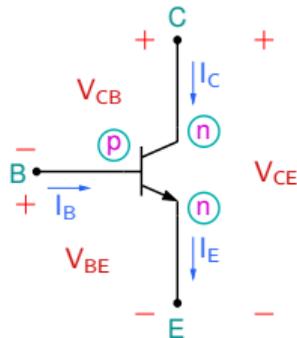
- \* Since BJT is a three-terminal device, its behaviour can be described in many different ways, e.g.,



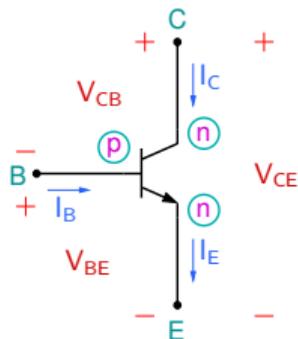
- \* Since BJT is a three-terminal device, its behaviour can be described in many different ways, e.g.,
  - $I_C$  versus  $V_{CB}$  for different values of  $I_E$



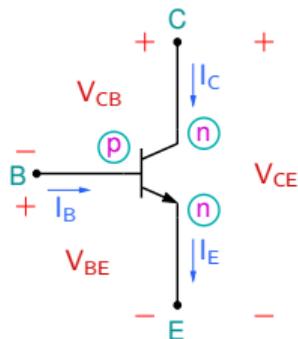
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  - $I_C$  versus  $V_{CE}$  for different values of  $V_{BE}$



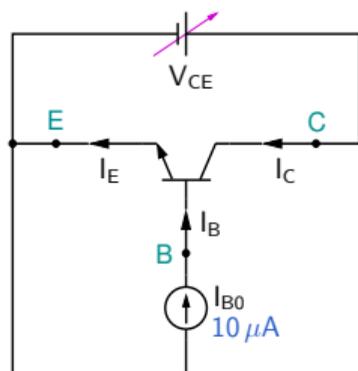
- \* Since BJT is a three-terminal device, its behaviour can be described in many different ways, e.g.,
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  - $I_C$  versus  $V_{CE}$  for different values of  $I_B$



- \* Since BJT is a three-terminal device, its behaviour can be described in many different ways, e.g.,
  - $I_C$  versus  $V_{CB}$  for different values of  $I_E$
  - $I_C$  versus  $V_{CE}$  for different values of  $V_{BE}$
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- \* The  $I$ - $V$  relationship for a BJT is not a single curve but a “family” of curves or “characteristics.”



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- \* The  $I$ - $V$  relationship for a BJT is not a single curve but a “family” of curves or “characteristics.”
- \* The  $I_C$ - $V_{CE}$  characteristics for different  $I_B$  values are useful in understanding amplifier biasing.



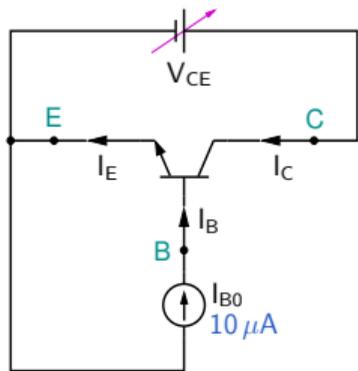
$$\alpha_F = 0.99 \rightarrow \beta_F = \frac{\alpha_F}{1 - \alpha_F} = 99$$

$$\alpha_R = 0.5 \rightarrow \beta_R = \frac{\alpha_R}{1 - \alpha_R} = 1$$

$$I_{ES} = 1 \times 10^{-14} \text{ A}$$

$$I_{CS} = 2 \times 10^{-14} \text{ A}$$

# BJT I-V characteristics

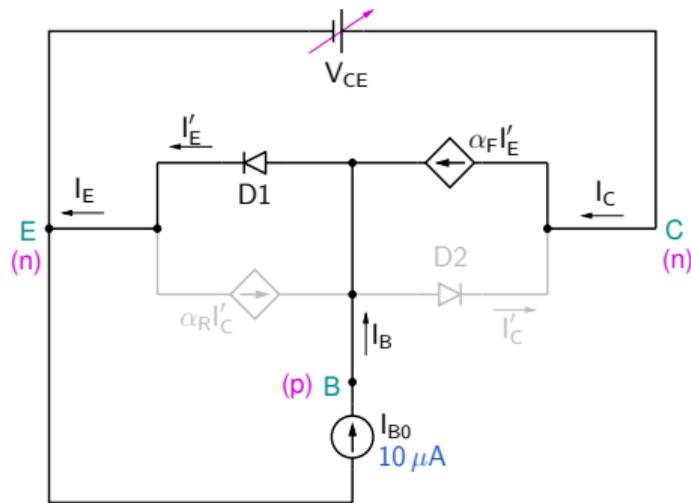


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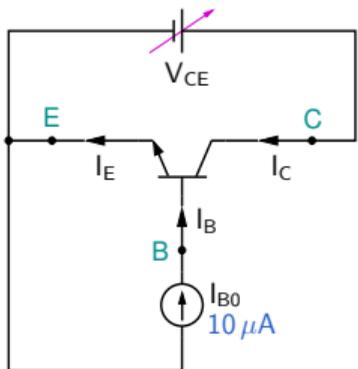


$$I'_E = I_{ES} [\exp(V_{BE}/V_T) - 1]$$

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$$I_C = \alpha_F I_E = \beta_F I_B \text{ in active mode}$$

# BJT $I$ - $V$ characteristics

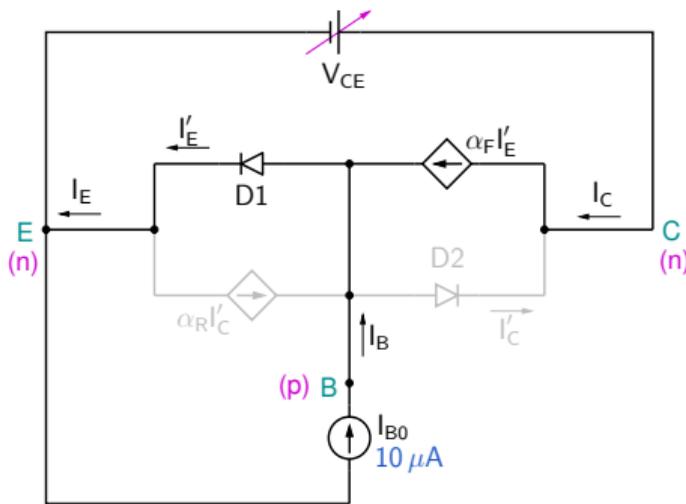


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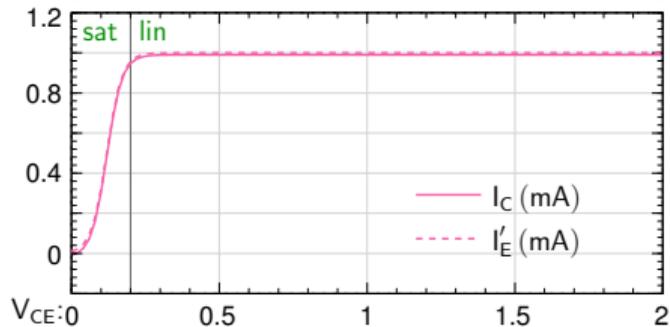
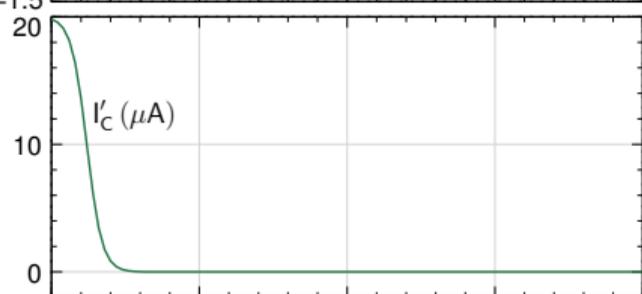
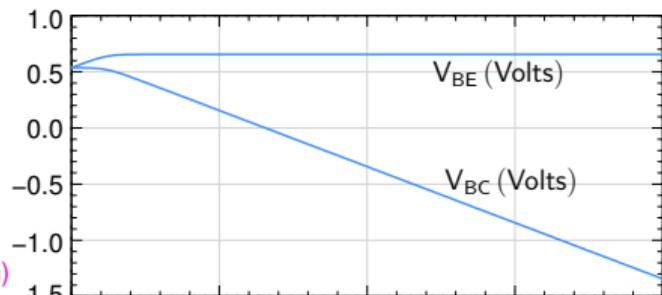
$$I_{CS} = 2 \times 10^{-14} \text{ A}$$



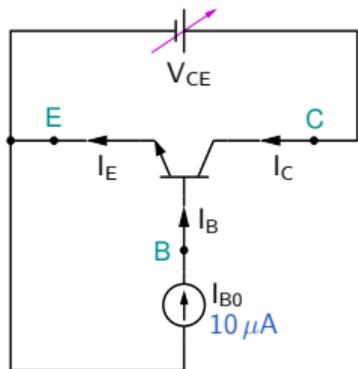
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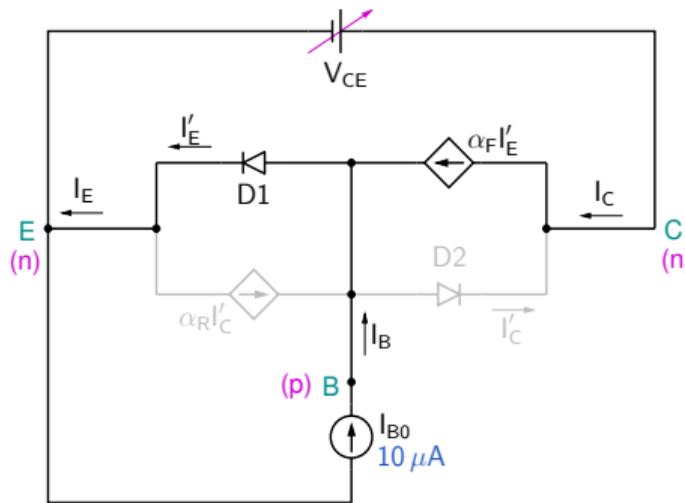


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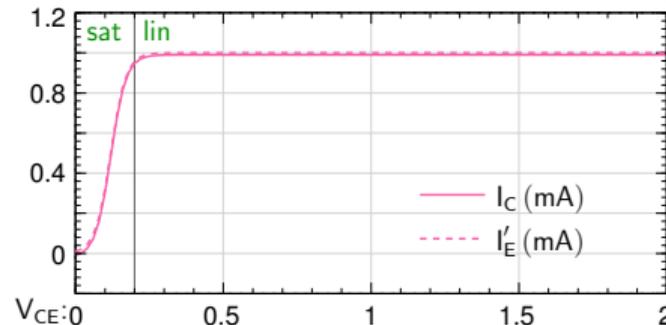
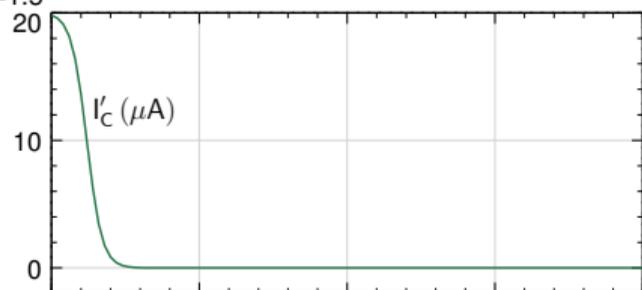
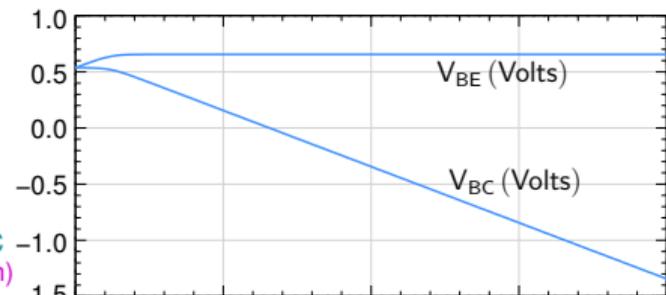
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$$I'_C = I_{CS} [\exp(V_{BC}/V_T) - 1]$$

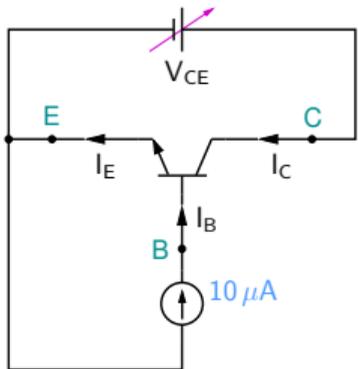
$$I_C = \alpha_F I_E = \beta_F I_B \text{ in active mode}$$

\* linear region: B-E under forward bias, B-C under reverse bias,  $I_C = \beta_F I_B$

\* saturation region: B-E under forward bias, B-C under forward bias,  $I_C < \beta_F I_B$



# BJT $I$ - $V$ characteristics

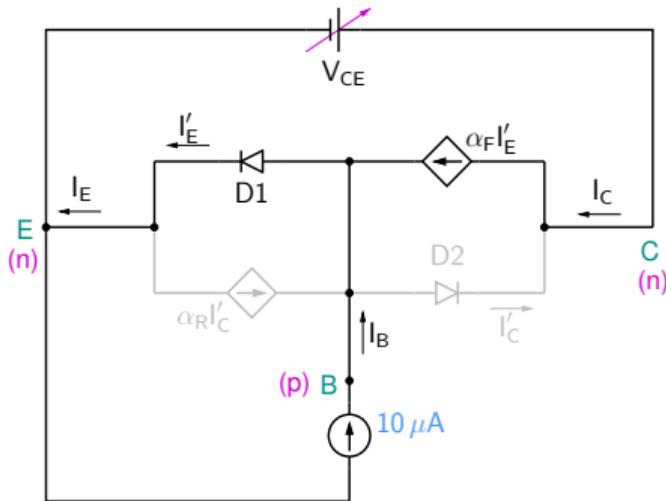


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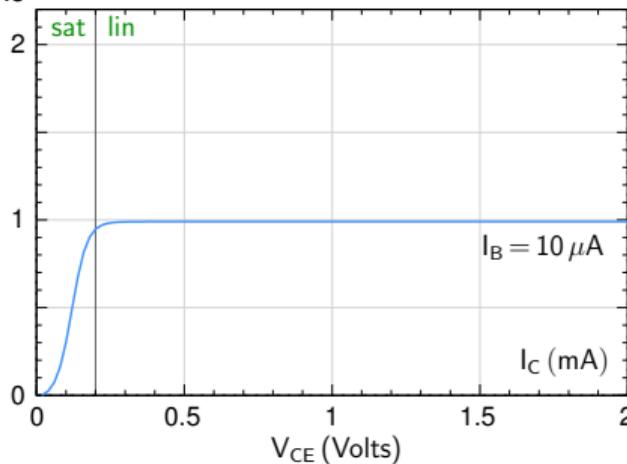
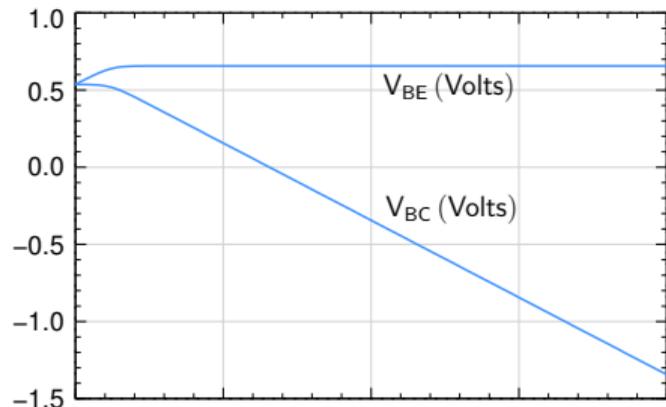
$$I_{CS} = 2 \times 10^{-14} \text{ A}$$



$$I'_E = I_{ES} [\exp(V_{BE}/V_T) - 1]$$

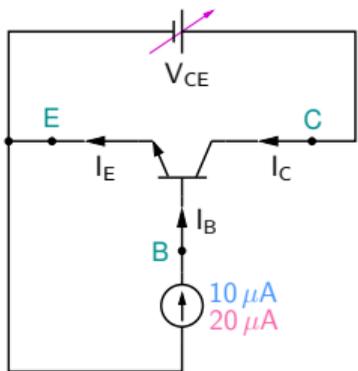
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- \* saturation region: B-E under forward bias, B-C under forward bias,  $I_C < \beta_F I_B$

# BJT I-V characteristics

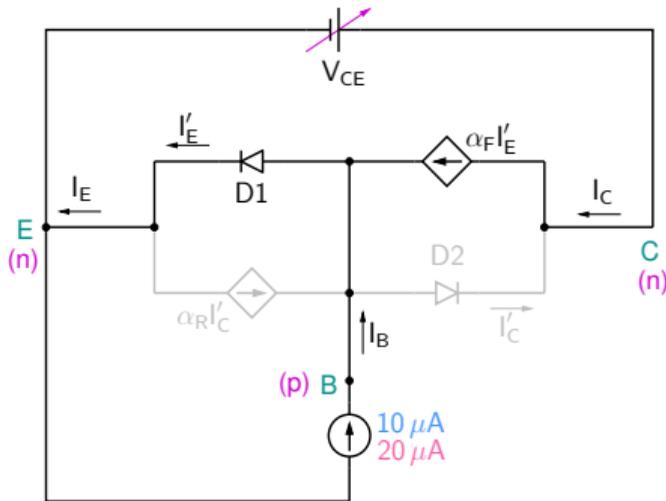


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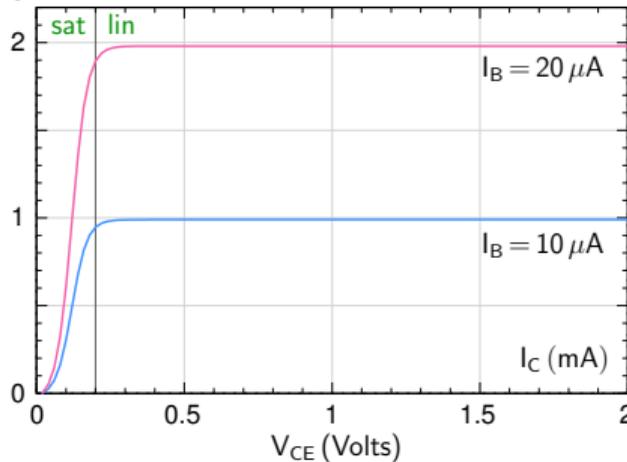
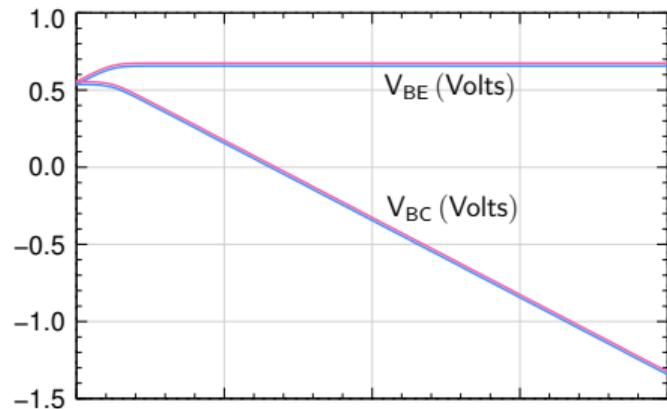
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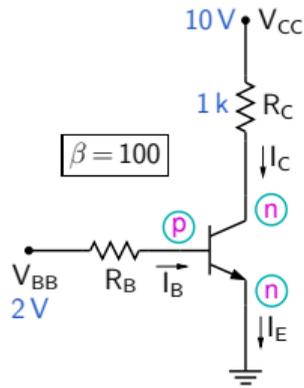
$$I_C = \alpha_F I_E = \beta_F I_B \text{ in active mode}$$



\* linear region: B-E under forward bias, B-C under reverse bias,  $I_C = \beta_F I_B$

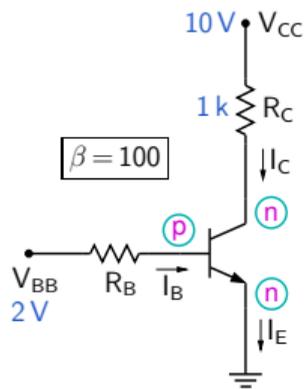
\* saturation region: B-E under forward bias, B-C under forward bias,  $I_C < \beta_F I_B$

## A simple BJT circuit (revisited)



We are now in a position to explain what happens when  $R_B$  is decreased from 100 k to 10 k in the above circuit.

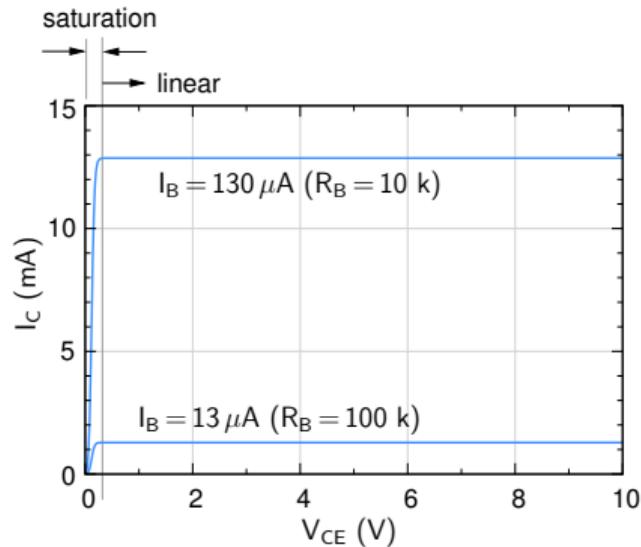
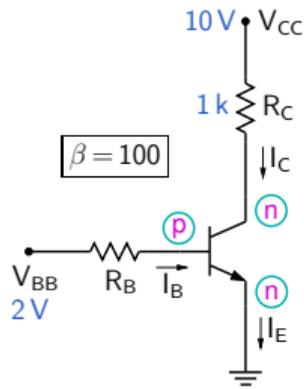
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Let us plot  $I_C - V_{CE}$  curves for  $I_B \approx \frac{V_{BB} - 0.7\text{ V}}{R_B}$  for the two values of  $R_B$ .

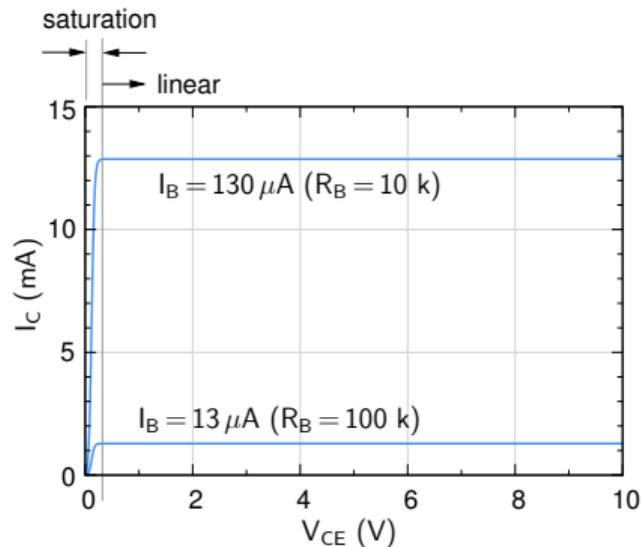
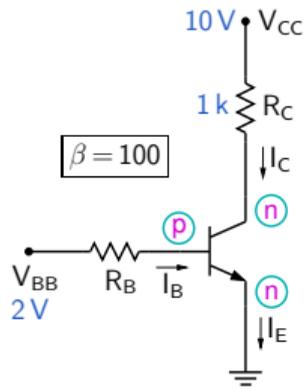
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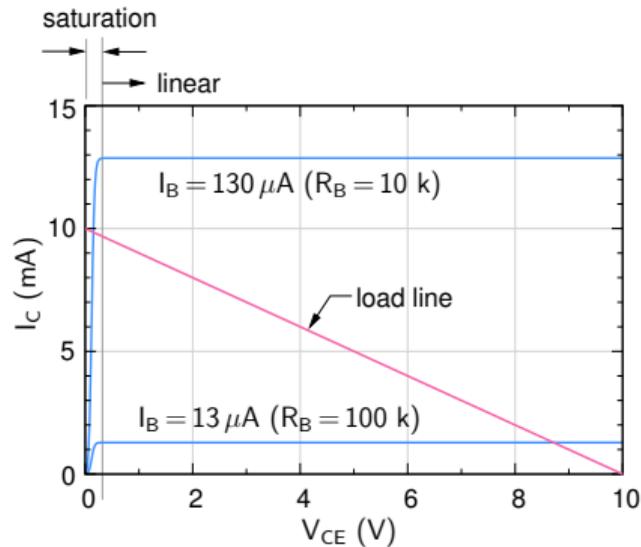
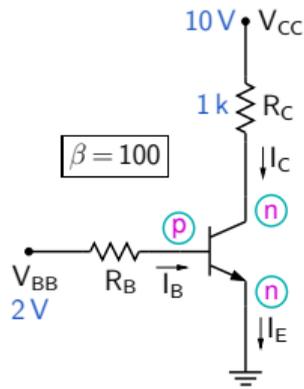


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In addition to the BJT  $I_C - V_{CE}$  curve, the circuit variables must also satisfy the constraint,  $V_{CC} = V_{CE} + I_C R_C$ , a straight line in the  $I_C - V_{CE}$  plane.

## A simple BJT circuit (revisited)

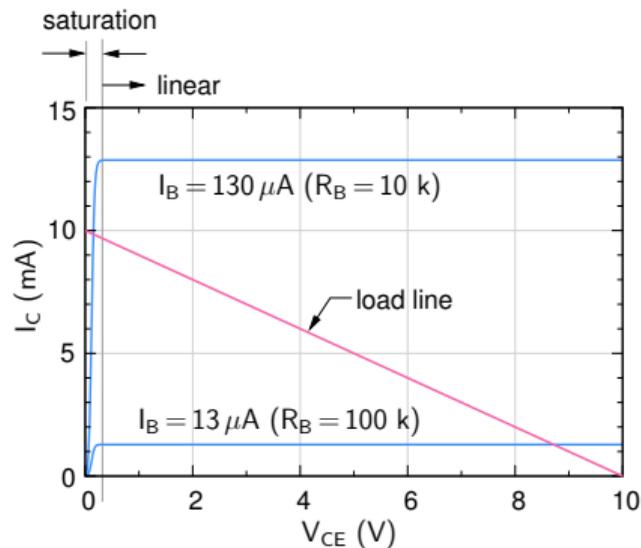
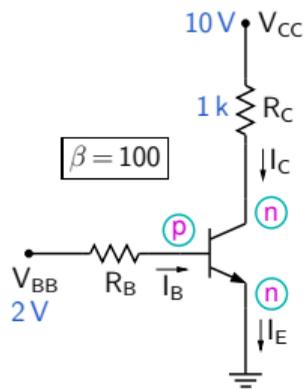


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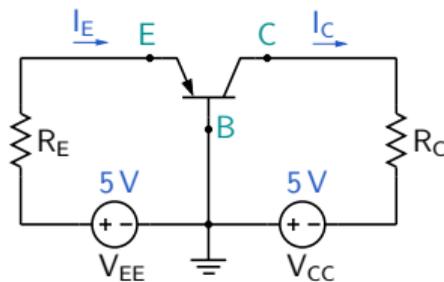
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The intersection of the load line and the BJT characteristics gives the solution for the circuit. For  $R_B = 10$  k, note that the BJT operates in the saturation region, leading to  $V_{CE} \approx 0.2$  V, and  $I_C = 9.8$  mA.

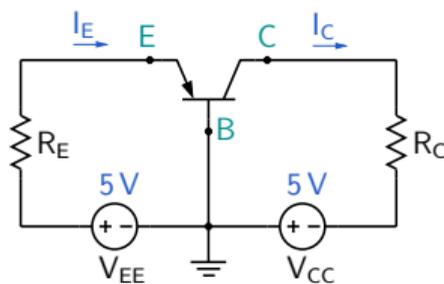
## BJT circuit example

Assuming the transistor to be operating in the active region, find  $R_E$  and  $R_C$  to obtain  $I_E = 2\text{ mA}$ , and  $V_{BC} = 1\text{ V}$  ( $\alpha \approx 1$ ).



## BJT circuit example

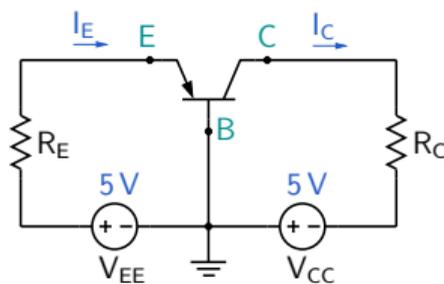
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$$V_{EB} - V_{EE} + I_E R_E = 0$$

## BJT circuit example

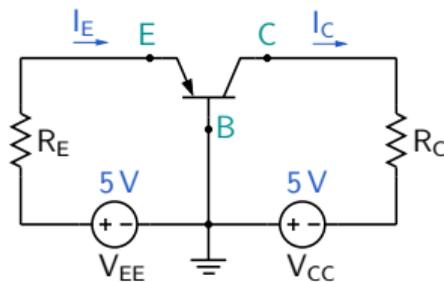
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$$V_{EB} - V_{EE} + I_E R_E = 0 \rightarrow I_E R_E = 5 - 0.7$$

## BJT circuit example

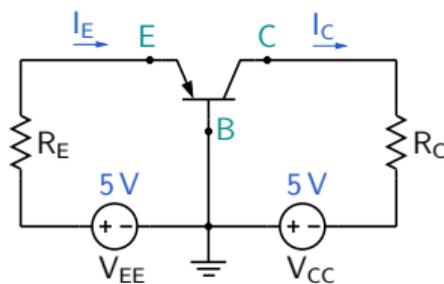
Assuming the transistor to be operating in the active region, find  $R_E$  and  $R_C$  to obtain  $I_E = 2 \text{ mA}$ , and  $V_{BC} = 1 \text{ V}$  ( $\alpha \approx 1$ ).



$$V_{EB} - V_{EE} + I_E R_E = 0 \rightarrow I_E R_E = 5 - 0.7 \rightarrow R_E = \frac{4.3 \text{ V}}{2 \text{ mA}} = 2.15 \text{ k}.$$

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Assuming the transistor to be operating in the active region, find  $R_E$  and  $R_C$  to obtain  $I_E = 2 \text{ mA}$ , and  $V_{BC} = 1 \text{ V}$  ( $\alpha \approx 1$ ).

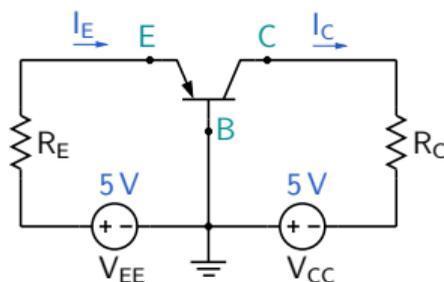


$$V_{EB} - V_{EE} + I_E R_E = 0 \rightarrow I_E R_E = 5 - 0.7 \rightarrow R_E = \frac{4.3 \text{ V}}{2 \text{ mA}} = 2.15 \text{ k}.$$

$$V_{BC} + I_C R_C - V_{CC} = 0$$

## BJT circuit example

Assuming the transistor to be operating in the active region, find  $R_E$  and  $R_C$  to obtain  $I_E = 2 \text{ mA}$ , and  $V_{BC} = 1 \text{ V}$  ( $\alpha \approx 1$ ).

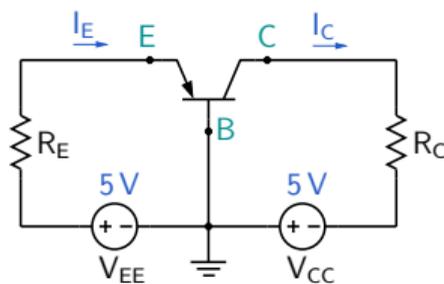


$$V_{EB} - V_{EE} + I_E R_E = 0 \rightarrow I_E R_E = 5 - 0.7 \rightarrow R_E = \frac{4.3 \text{ V}}{2 \text{ mA}} = 2.15 \text{ k}.$$

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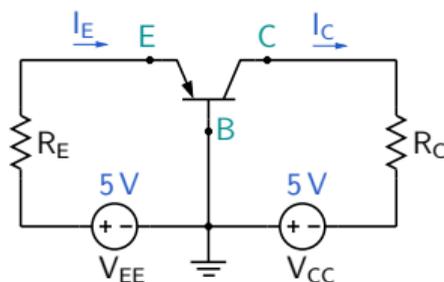
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